

## Syntax of $\mathcal{A}$ : Observation and Queries?

- Observations (O):
  - **f after**  $a_1, \dots, a_n$ .
    - \*  $f$  was observed to be true after  $a_1, \dots, a_n$  is executed in the initial situation.
    - \* We are told that  $f$  would be true if  $a_1, \dots, a_n$  were to be executed in the initial situation.
  - **initially**  $f$ .
- Queries (Q): **f after**  $a_1, \dots, a_n$ .
  - Will  $f$  be true after executing  $a_1, \dots, a_n$  in the initial situation.
  - Would  $f$  be true if  $a_1, \dots, a_n$  were executed in the initial situation.
- Main reasoning relation  $(D, O) \models Q$ .

Defining the above is our next goal. (Semantics!)

Semantics of  $\mathcal{A}$ : motivating examples.

- $D1 = \{ \text{load } \mathbf{causes} \text{ loaded; shoot } \mathbf{causes} \neg \text{alive } \mathbf{if} \text{ loaded} \}$
- $D2 = \{ \text{load } \mathbf{causes} \text{ loaded; shoot } \mathbf{causes} \neg \text{alive; } \mathbf{executable} \text{ shoot } \mathbf{if} \text{ loaded} \}$
- $O1 = \{ \mathbf{initially} \neg \text{loaded; } \mathbf{initially} \text{ alive} \}$
- $O2 = \{ \mathbf{initially} \text{ alive} \}$
- $O3 = \{ \mathbf{initially} \text{ alive; } \neg \text{alive } \mathbf{after} \text{ load, shoot} \}$
- Plan verification (hypothetical reasoning):  $(D1, O1) \models \neg \text{alive } \mathbf{after} \text{ load, shoot?}$
- Simple planning:  $(D1, O1) \models \neg \text{alive } \mathbf{after} \alpha?$
- Conformant planning:  $(D1, O2) \models \neg \text{alive } \mathbf{after} \alpha?$
- Observation assimilation:  $(D1, O3) \models \mathbf{initially} \text{ loaded?}$
- Exercise: Replace D1 by D2 in the above reasoning tasks.

Semantics of  $\mathcal{A}_0$ : lead-in to the definition of  $\models$

- Domain descriptions in  $\mathcal{A}_0$  do not have executability conditions.
- Our goal: To define  $(D, O) \models Q$ .
- *Lets first consider  $O$  such that it is of the form **initially**  $f$ .*
- Q1: What kind of information does such an  $O$  encode.
- Q2: What kind of information  $D$  encodes.
- Hint for Q1: initial state.
- Hint for Q2: Each effect proposition: a **causes**  $f$  **if**  $p_1, \dots, p_n$   
means a transition  $p_1, \dots, p_n \xrightarrow{a} f$
- Ans1:  $O$  tells us what the initial state of the world is. (If  $O$  is not complete – does not have information about all the fluents – it leads us to multiple initial states.)  
Given  $O$ , what is an initial state ( $\sigma$ ) corresponding to  $O$ ? Define? (What is a good representation of a state?)

- Ans2:  $D$  defines the transition between states due to actions.  
Given a  $D$ , define the transition function  $\Phi_D$  implied by  $D$ ?
- What is  $\Phi_{D_1}$ ? What are initial states corresponding to  $O_1$  and  $O_2$ ?
- The set of states:  $\{ \{ \}, \{ \text{alive} \}, \{ \text{loaded} \}, \{ \text{alive}, \text{loaded} \} \}$ .
  - $\Phi_{D_1}(\text{load}, \{ \}) = \{ \text{loaded} \}$ .
  - $\Phi_{D_1}(\text{load}, \{ \text{alive} \}) = \{ \text{alive}, \text{loaded} \}$ .
  - $\Phi_{D_1}(\text{load}, \{ \text{loaded} \}) = \{ \text{loaded} \}$ .
  - $\Phi_{D_1}(\text{load}, \{ \text{alive}, \text{loaded} \}) = \{ \text{alive}, \text{loaded} \}$ .
  - $\Phi_{D_1}(\text{shoot}, \{ \}) = \{ \}$ .
  - $\Phi_{D_1}(\text{shoot}, \{ \text{alive} \}) = \{ \text{alive} \}$ .
  - $\Phi_{D_1}(\text{shoot}, \{ \text{loaded} \}) = \{ \text{loaded} \}$ .
  - $\Phi_{D_1}(\text{shoot}, \{ \text{alive}, \text{loaded} \}) = \{ \text{loaded} \}$ .
- Initial state corresponding to  $O_1$ :  $\{ \text{alive} \}$
- Initial states corresponding to  $O_2$ :  $\{ \text{alive} \}; \{ \text{alive}, \text{loaded} \}$
- How to define  $(D_1, O_1) \models Q$ .

Semantics of  $\mathcal{A}_0$ : defining  $\models$

- Given:  $D$ ,  $O$  and the language of  $D$  and  $O$ . The language consists of a set of actions  $Act$  and a set of fluents  $Fl$ . A *state* is a subset of  $Fl$ .
- A fluent  $f$  holds in a state  $\sigma$  if  $f \in \sigma$ . A fluent literal  $\neg f$  holds in a state  $\sigma$  if  $f \notin \sigma$ .
- *Characterizing  $O$  when it consists of only observations about the initial state:*  
A set of fluents  $\sigma$  is an initial state corresponding to  $O$ , if for all observations of the form **initially**  $g$  (where  $g$  is a fluent literal),  $g$  holds in  $\sigma$ .
- Given a domain description  $D$  in  $\mathcal{A}_0$  its transition function is defined as follows:
  - For all actions  $a$ , fluents  $f$ , and states  $\sigma$ :
    - \* If  $a$  **causes**  $f$  **if**  $p_1, \dots, p_n \in D$  and  $p_1, \dots, p_n$  hold in  $\sigma$  then  $f$  must be in  $\Phi(a, \sigma)$ .
    - \* If  $a$  **causes**  $\neg f$  **if**  $p_1, \dots, p_n \in D$  and  $p_1, \dots, p_n$  hold in  $\sigma$  then  $f$  must not be in  $\Phi(a, \sigma)$ .
    - \* If  $D$  does not include such effect propositions (about  $a$  and  $f$ ) then  $f \in \Phi(a, \sigma)$  iff  $f \in \sigma$ .

\* For any domain description  $D$ , there is at most one such function and we refer to it as  $\Phi_D$ . If  $\Phi_D$  exists we say  $D$  is consistent.

– If  $\Phi_D$  exists then it is defined as follows:

\*  $E_D^+(a, \sigma) = \{f : a \text{ causes } f \text{ if } p_1, \dots, p_n \in D \text{ and } p_1 \dots p_n \text{ hold in } \sigma\}$

\*  $E_D^-(a, \sigma) = \{f : a \text{ causes } \neg f \text{ if } p_1, \dots, p_n \in D \text{ and } p_1 \dots p_n \text{ hold in } \sigma\}$

\*  $\Phi_D(a, \sigma) = \sigma \cup E_D^+(a, \sigma) \setminus E_D^-(a, \sigma)$

• **For general observations:** A set  $\sigma_0$  is said to be an initial state corresponding to a consistent domain description  $D$  and a set of observations  $O$  if for all observations of the form  $f$  **after**  $a_1, \dots, a_m$ ,  $f$  holds in  $\Phi_D(a_m, \Phi_D(a_{m-1}, \dots \Phi_D(a_1, \sigma_0) \dots))$ .

$\Phi_D(a_m, \Phi_D(a_{m-1}, \dots \Phi_D(a_1, \sigma_0) \dots))$  will be denoted by  $[a_m, \dots, a_1]\sigma_0$ .

• **Models of  $(D, O)$ :**  $(\sigma_0, \Phi)$  is a model of  $(D, O)$  iff  $\Phi$  is the transition function of  $D$  and  $\sigma_0$  is an initial state corresponding to  $D$  and  $O$ .

•  $(D, O)$  is said to be consistent if it has a model.

•  $(D, O)$  is said to be complete if it has a unique model.

•  $(D, O) \models f$  **after**  $a_1, \dots, a_m$  if for all models  $(\sigma_0, \Phi)$  of  $(D, O)$ ,  $f$  holds in  $[a_m, \dots, a_1]\sigma_0$ .

How hard is it to implement  $\models$  : summary of complexity results

- R1: Given  $D$ , deciding whether  $\Phi_D$  exists or not is polynomial.
- R2: Given a consistent  $D$  and a set of fluents  $\sigma_0$ , deciding whether  $\sigma_0$  is an initial state with respect to  $(D, O)$ , is polynomial.
- R3: Deciding if  $(D, O)$  is consistent is NP-complete.
- R4: Deciding if  $(D, O) \models f$  **after**  $a_1, \dots, a_n$  is coNP complete.
- R5: Given a  $D$ , a complete set of observations about the initial state  $O$ , and a fluent  $f$ , finding a polynomial sequence of actions  $a_1, \dots, a_m$  such that  $(D, O) \models f$  **after**  $a_1, \dots, a_m$  is NP-complete. (i.e., Feasible planning in  $\mathcal{A}_0$  with a complete initial state, and simple goal, is NP-complete.)