MAE384 Fall 2009 Final Exam - December 10, 2009 9:50-11:40 AM Open book, No laptop Allowed: Basic calculator with no programming/graphics functions

Key sections and slides (\star = most important)

Ch 6 Numerical differentiation

- 6.2 Basic concept of finite difference approximation
- \star 6.3-6.4 Derivation of finite difference schemes by Taylor series expansion
 - 6.10 Numerical partial differentiation
- Ch 7 Numerical integration
 - 7.2 Rectangle/Mid-point methods
- ★7.3 (Composite) Trapezoidal method
- \star 7.4 (Composite) Simpson's 1/3 and 3/8 methods (Focus on how to use the methods)
 - 7.5 Gauss quadrature

Ch. 8 Initial value problem

- \star 8.2 Euler's explicit method, Euler's implicit method (Skip sub-section 8.2.2)
- ★8.3 Modified Euler's method (which is a 2nd order Runge-Kutta method)
- ★8.5 Runge-Kutta methods (Focus on the 3rd order and 4th order R-K methods; sub-section 8.5.2, 8.5.3)
 - 8.6 Multi-step methods
 - 8.13 Numerical stability

Ch. 9 Boundary value problem

- ★9.3 Finite difference method (matrix formulation)
- ★ Slides for BVP; More examples on finite difference method

Introduction to partial differential equation

- ★PDE Slides (II) Method of separation of variables (First two examples only)
- ★ PDE Slides (III) Case 2: Numerical solution for PDE with an open domain
- ★ PDE Slides (III) Case 1 + Slides (IV): Numerical solution for Laplace equation with a closed domain

Likely distribution of # of questions

Ch. 6 1-2

- Ch. 7 1
- Ch. 8 1-2
- Ch. 9 1 PDE 1-2
- FDL 1-2

Total 5-6

Note: Expect a format similar to our midterm. Most of the problems will not require time-consuming computations but a calculator with basic math functions (sin, cos, exp, ln, \sqrt{x} , x^{ν} , etc.) will be very useful. Make sure to bring one.