MAE384 Fall 2011 Homework #3

1. The set of the following 4 data points is given:

$$\begin{array}{ccc}
x & y \\
-2 & 0 \\
1 & -1.95 \\
3 & -1.25 \\
5 & -1.75
\end{array}$$

- (a) Using <u>Lagrange interpolation method</u>, perform interpolation by first determining the 3rd order polynomial that passes through the data points. Provide the detail of the four <u>Lagrange functions</u> used in the intermediate steps. Use the result to determine the value of y at x = 2.
- **(b)** Make the following plots: (i) The original data points and the 3rd order polynomial obtained in (a) (together, in a single plot), (ii) The four <u>Lagrange functions</u> used in (a).

[2 points]

2. The set of the following 5 data points is given:

- **(a)** Following the procedure in Sec. 5.6.2 in the textbook, determine the <u>quadratic splines</u> that fit the data. Show your procedure.
- **(b)** Plot the quadratic splines obtained in (a) and the original data points in a single figure, in the fashion of the figure in Example 5-7 in the textbook.

[4 points]