Prob 1. Plot


Prob 2. Plot



Prob 3.(a)

$$
u(z, t)=\frac{L U}{\sqrt{L^{2}+4 v t}} \exp \left(-\frac{z^{2}}{L^{2}+4 v t}\right) ; \quad M=\rho L U \pi^{1 / 2}=\text { constant }
$$

Prob 3.(b)
The heating rate is

$$
\frac{d T}{d t}=-\frac{v}{C_{p}}\left(\frac{1}{0.4 m}\right) \int_{-0.2 m}^{0.2 m} u \frac{\partial^{2} u}{\partial z^{2}} d z \quad, \text { where } u(z, t) \text { is given in Part (a). }
$$

The numerical values are $2.23 \times 10^{-10}{ }^{\circ} \mathrm{C} / \mathrm{s}$ at $t=0$ and $1.617 \times 10^{-10}{ }^{\circ} \mathrm{C} / \mathrm{s}$ at $t=10 \mathrm{~min}$. Over 30 minutes, the box of water is heated up by only $2.65 \times 10^{-7}{ }^{\circ} \mathrm{C}$ which is insignificant.

Prob 4.
The velocity is around $37.7 \mathrm{~m} / \mathrm{s}$

