

MAE 578, Spring 2019, HW5 solution

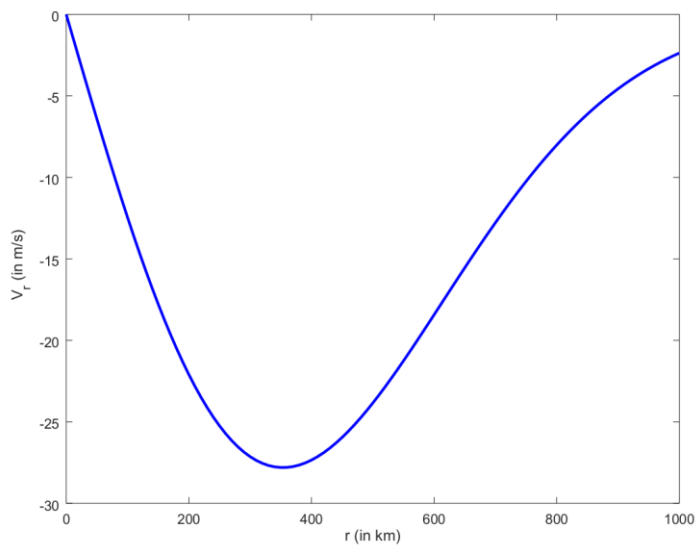
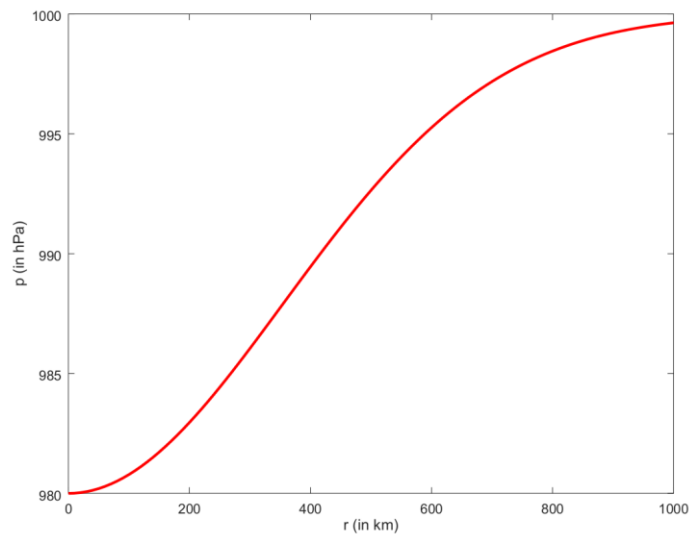
Prob 1

The flow is axially symmetric with the tangential velocity

$$V_r = \left( \frac{2\Delta p}{f\rho R^2} \right) r \exp[-(r/R)^2],$$

where  $f = 2\Omega \sin(-45^\circ)$  and  $\Omega = 2\pi/(86400 \text{ s})$ . Since  $f < 0$ , we have  $V_r < 0$ . The circulation is clockwise around the low-pressure center. The maximum wind speed occurs at  $r = R/\sqrt{2} = 353.5 \text{ km}$ . At that radius, the magnitude of velocity is 27.8 m/s if the density of air is given as  $1.2 \text{ kg/m}^3$  (typical value at lower troposphere).

Plots:



Prob 2

$$\Delta Z = 1412 \text{ m}, \quad u = 40.4 \text{ m/s}$$

Prob 3

The  $u$ -velocity at the 1-mb level is 127.9 m/s.

Prob 4

The depth of the river at the eastern boundary exceeds that at the western boundary by 0.52 mm.