

Neutron vs. Quark Stars

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Neutron stars

- **Radius:**

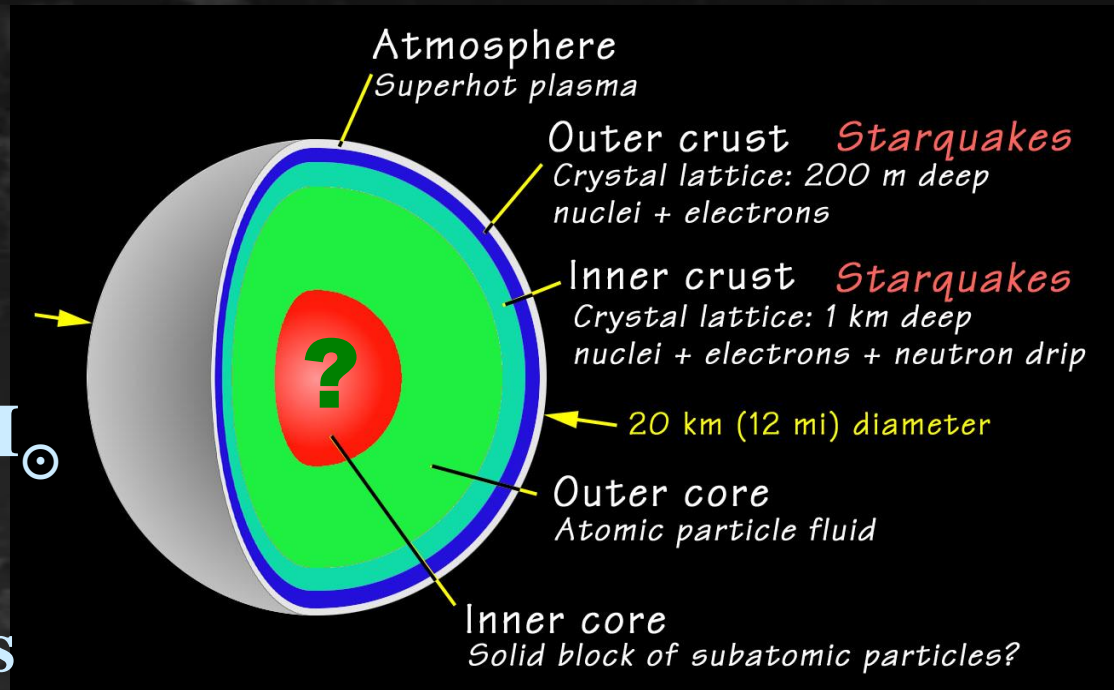
$$R \approx 10 \text{ km}$$

- **Mass:**

$$1.25M_{\odot} \lesssim M \lesssim 2M_{\odot}$$

- **Period:**

$$1.6 \text{ ms} \lesssim P \lesssim 12 \text{ s}$$

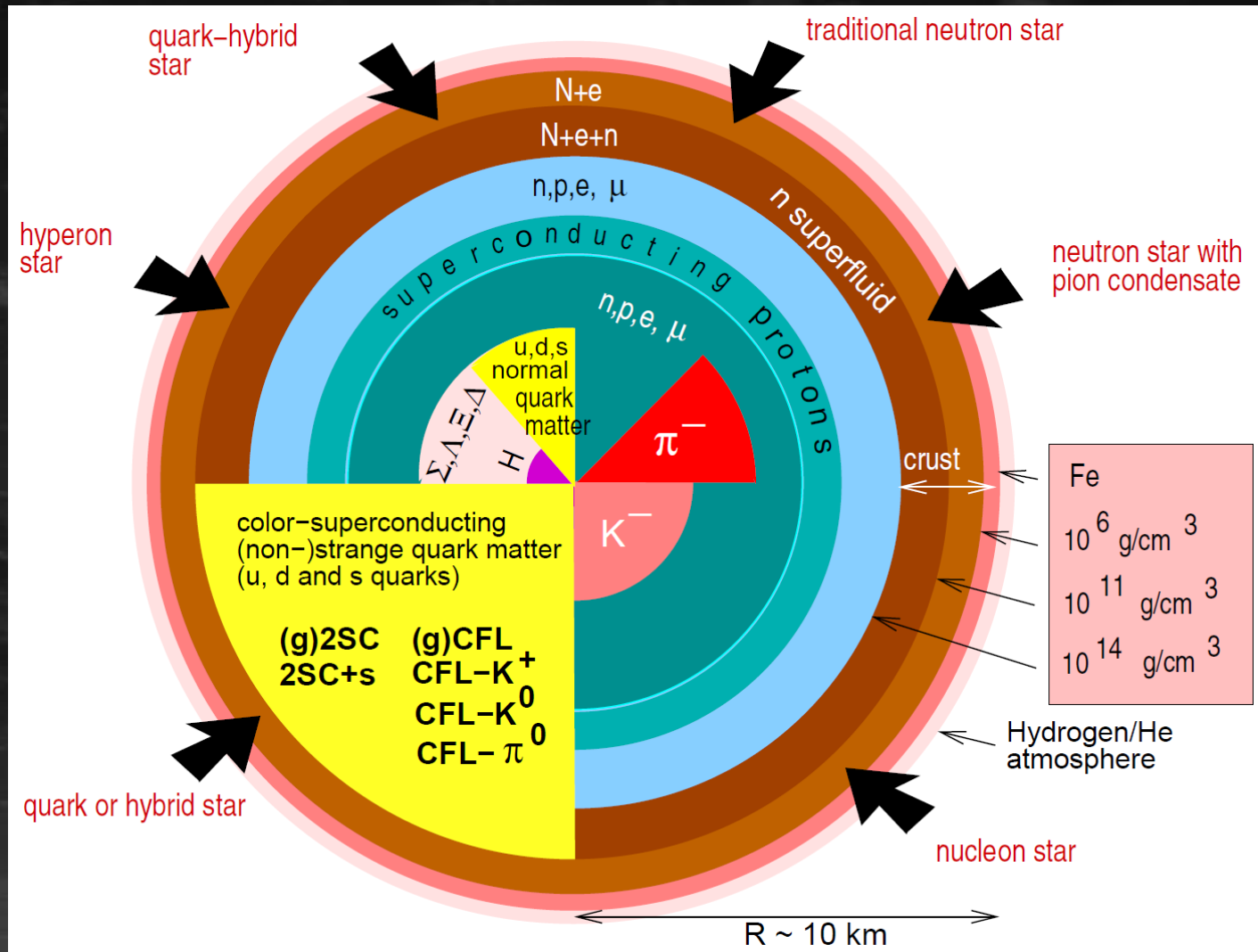


- **Surface magnetic field:**

$$10^8 \text{ G} \lesssim B \lesssim 10^{14} \text{ G}$$

- **Core temperature:** $10 \text{ keV} \lesssim T \lesssim 10 \text{ MeV}$

Dense matter at the core



[adapted from F. Weber, Prog. Part. Nucl. Phys. **54** (2005) 193]

Extremely dense matter

Nuclear matter → quark matter

• **Asymptotic freedom:**

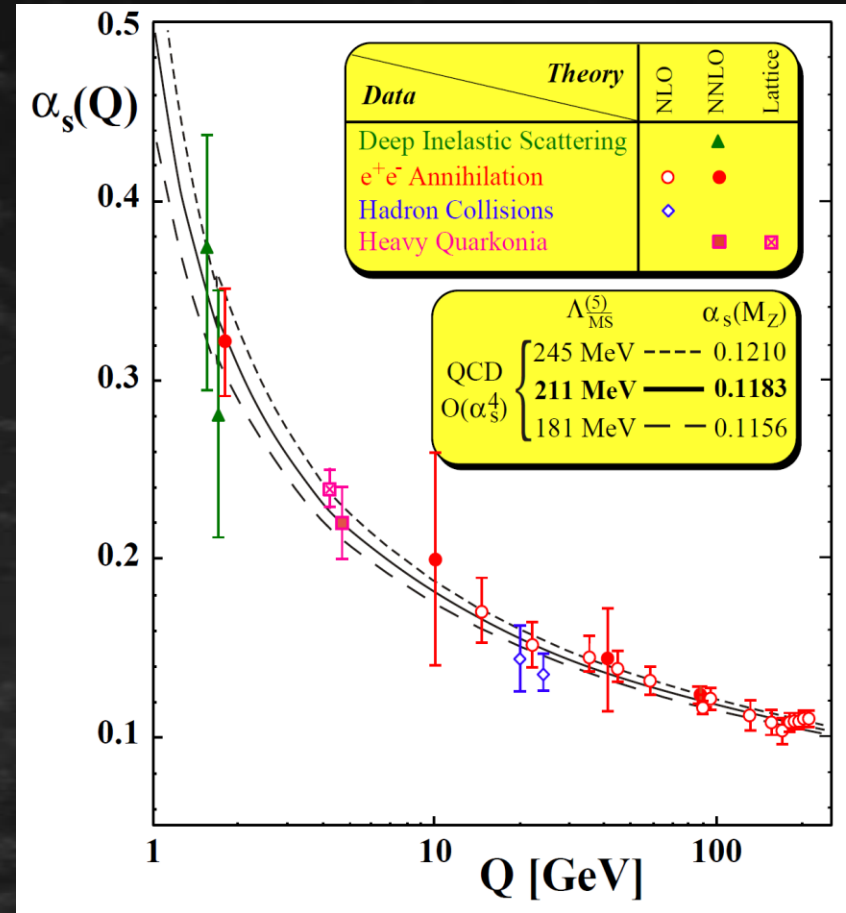
$$\alpha_s(\mu) \ll 1 \text{ when } \mu \gg \Lambda_{\text{QCD}}$$

[Gross & Wilczek, 1973; Politzer, 1973]

• **High density quark matter is weakly interacting**

[Collins & Perry, 1975]

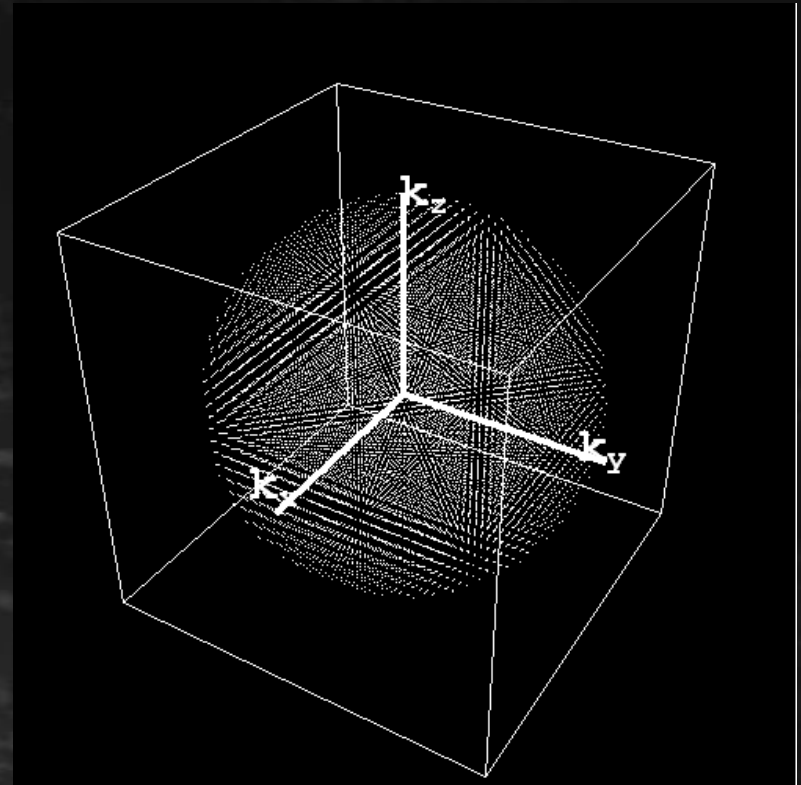
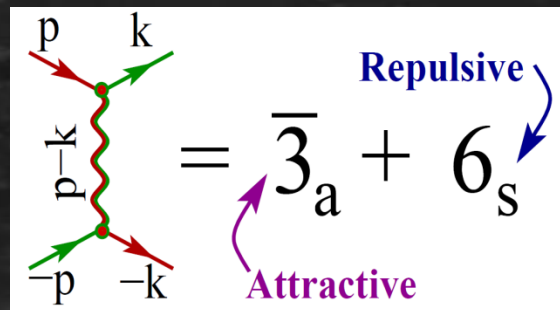
• **Note:** realistic densities in stars are not large enough...



$$\rho \lesssim 10\rho_0 \text{ where } \rho_0 \simeq 0.15 \text{ fm}^{-3} \implies \mu \lesssim 0.5 \text{ GeV} \implies \alpha_s(\mu) \gtrsim 1$$

Ground state of dense matter




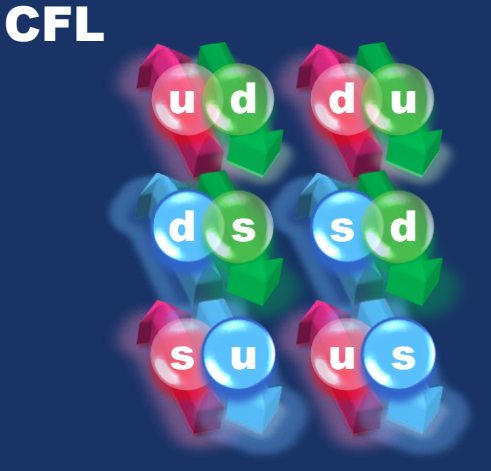

- Quarks are fermions ($s=1/2$)
- Free quarks occupy all states with $k \leq k_F$
- Real quarks interact



Because of the **Cooper theorem**, such a degenerate quark system is unstable

The ground state is a **(color) superconductor**

Many color superconductors

1 quark flavor (spin-1) (e.g., only up)		2 quark flavors (up & down)	3 quark flavors (up, down & strange)
CSL		2SC	CFL
Planar			
A/Polar			
Meissner effect: Yes		Meissner effect: No	Meissner effect: No
Superfluidity: Yes		Superfluidity: No	Superfluidity: Yes

- **The actual composition of quark matter depends on its density: q_i is present if $\mu_i > m_i$**
- **For $\mu \lesssim 0.5$ GeV, c-, b- and t-quarks have no chance**

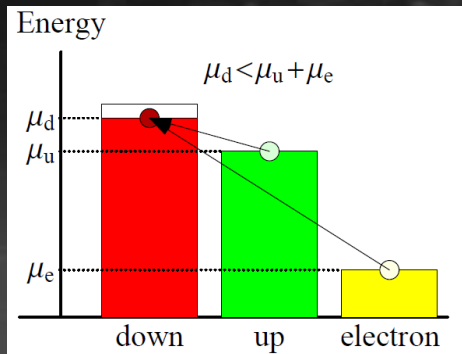
Color superconductivity in stellar matter

- **Stellar matter is**

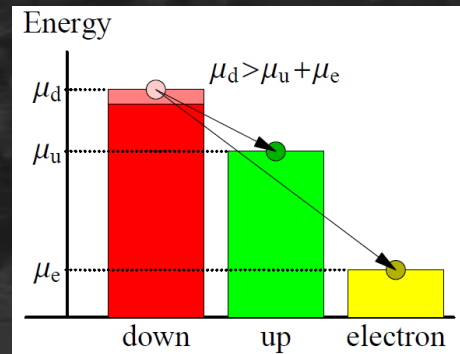
- (i) **neutral** (to avoid large Coulomb energy price, $E_{\text{Coulomb}} \propto n_Q^2 R^5 \gg M_\odot c^2$)

- (ii) **in β -equilibrium:** $\mu_d = \mu_u + \mu_e = \mu_s$

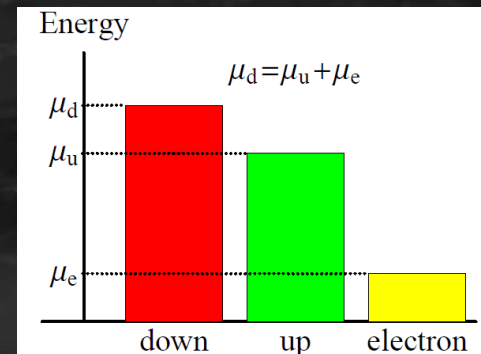
Too few d-quarks



Too many d-quarks



β -equilibrium



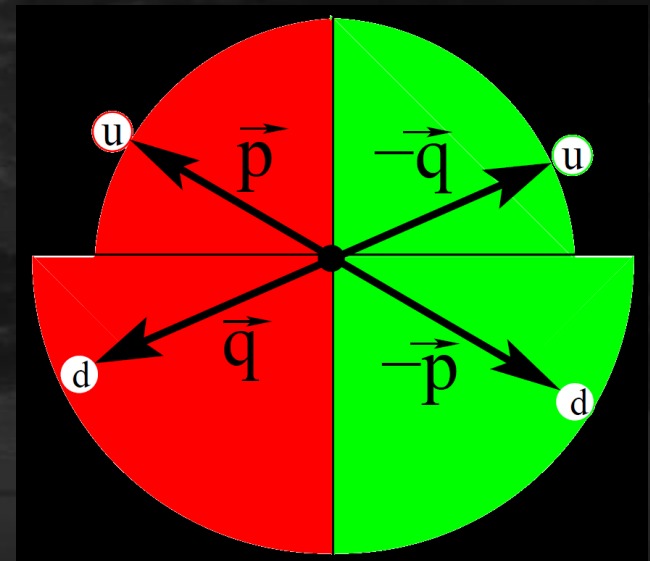
Unconventional Cooper pairing in stellar matter

- **Bottom line:** Fermi momenta of all quarks are different: $p_{F,u} \neq p_{F,d} \neq p_{F,s}$

(note that $p_{F,u} \approx \mu_u$, $p_{F,d} \approx \mu_d$ & $p_{F,s} = \sqrt{\mu_s^2 - m_s^2}$)

Thus, Cooper pairing is “stressed” by the mismatch, $\delta p_F \neq 0$

What happens then?



Gapless phases (2 flavors)

[I.S. & M. Huang, Phys. Lett. **564** (2003) 205; Nucl. Phys. **729** (2003) 835.]

Strength of pairing (Δ_0) vs. mismatch ($\delta\mu$)

1. Weak coupling

$$\Delta_0 \lesssim \delta\mu$$

\Rightarrow normal quark matter phase

2. Strong coupling

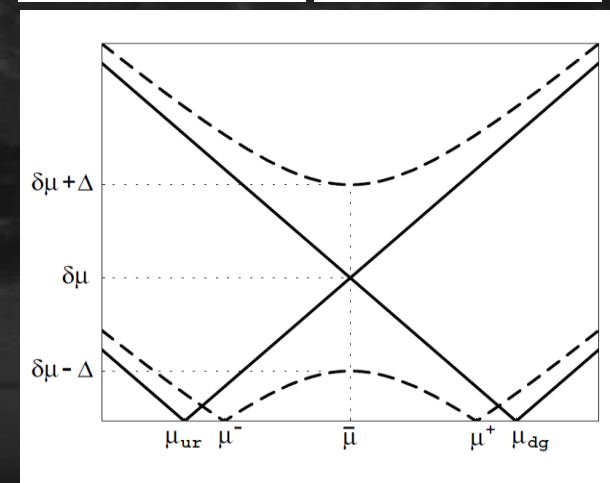
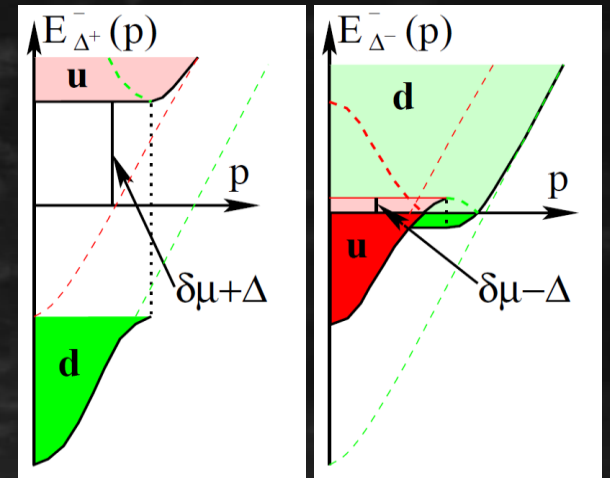
$$\Delta_0 \gtrsim 2 \delta\mu$$

\Rightarrow “usual” superconducting phase

3. Intermediate strength

$$\delta\mu \lesssim \Delta_0 \lesssim 2 \delta\mu$$

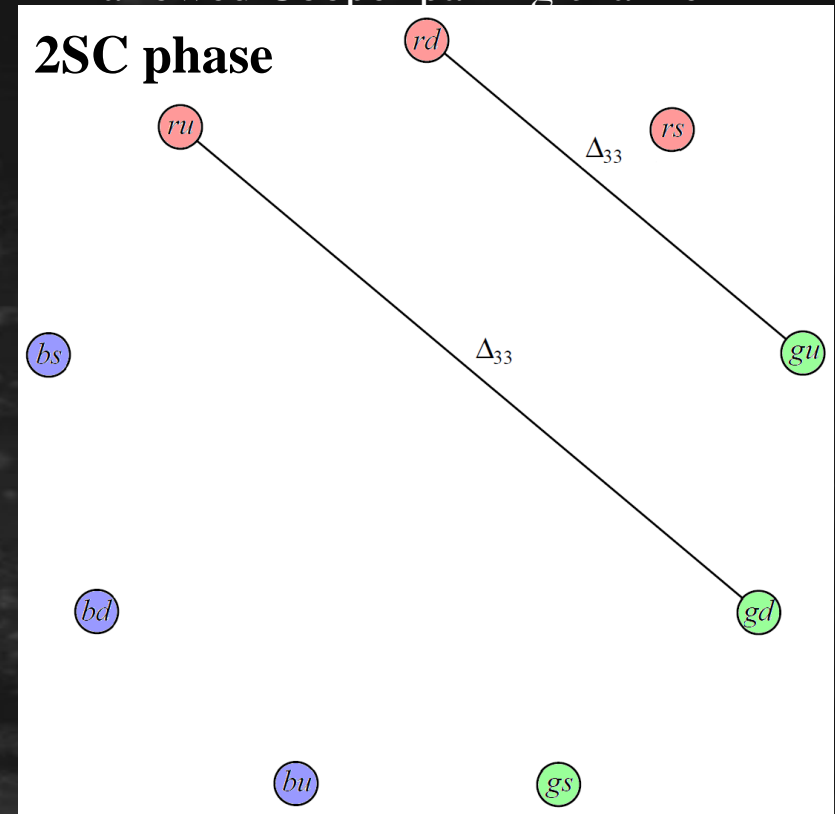
\Rightarrow gapless superconducting phase



“No-go” theorem

- **Stressed pairing is unavoidable**
[Schmitt & Rajagopal, PRD 73 (2006) 045003]
- **Using graph theory, 511 pairing patterns (including all 148 inequivalent ones) were analyzed**
- **None of them is stress-free**
- **So, what does it mean?**

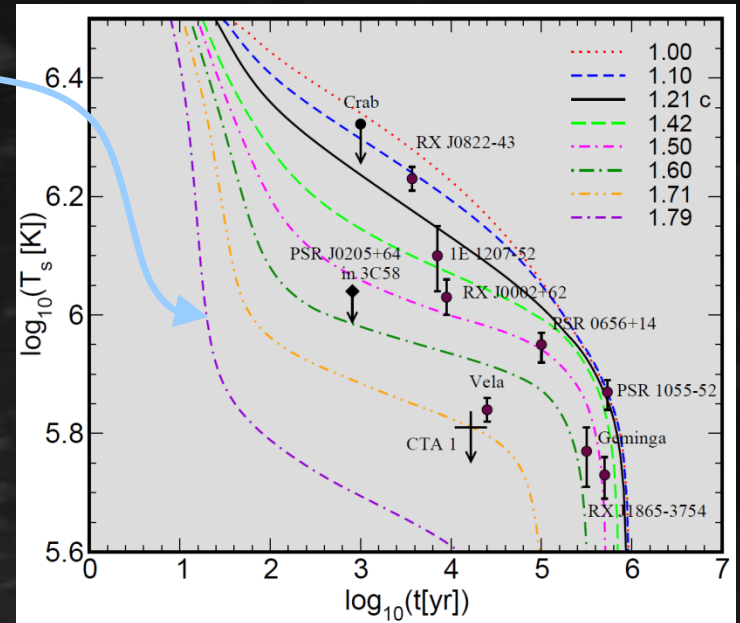
Each line in the graph represents an allowed Cooper pairing channel



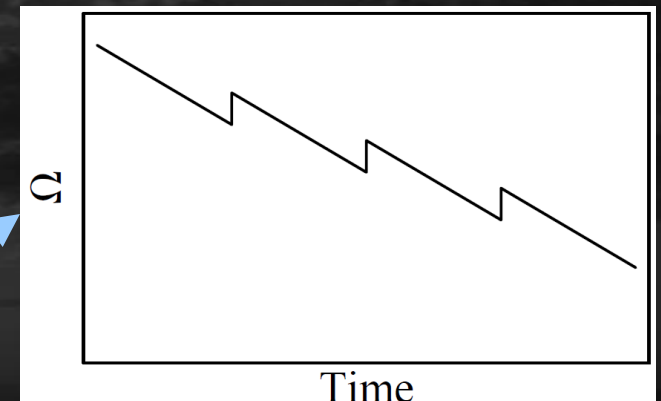
[adapted from Schmitt & Rajagopal, Phys. Rev. D 73 (2006) 045003]

Observational data as a tool

1. Neutron star cooling
2. Stellar “glitches”
3. Gravitational waves & r-mode instability
4. Magnetic properties
5. Transient signals from protoneutron stars
6. ...



[Blaschke et al, Phys.Rev.C71 (2005) 045801]



Future direction: Transport

- **Conductivities**

[I.S. & Ellis, PRC 66 (2002) 015802; *ibid.* 67 (2003) 048801]

- Heat
- Electric

- **Viscosities**

[Manuel et al, JHEP 0509 (2005) 76]

[Sa'd et al, PRD75 (2007) 065016], [Alford & Schmitt, JPG 34 (2007) 67],

[Dong et al, astro-ph/0701104], [Alford et al, nucl-th/0701067]

- Bulk
- Shear

- **Mean free paths**

[Carter & Reddy, PRD 62 (200) 103002],

[Kundu & Reddy, PRC 70 (2004) 055803], ...

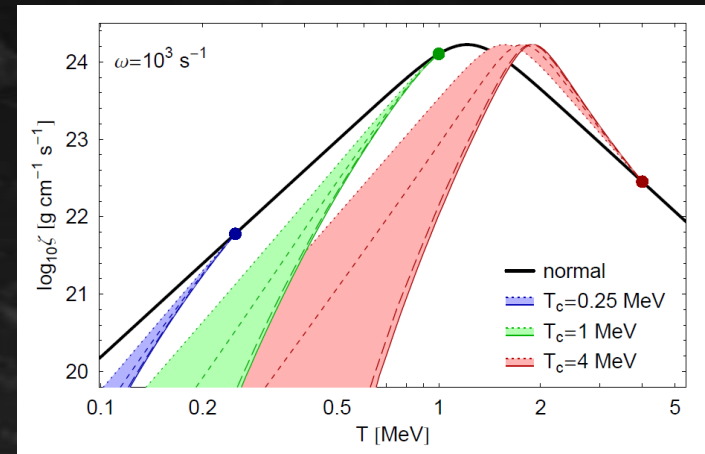
- Neutrinos
- Photons

- **Emission rates**

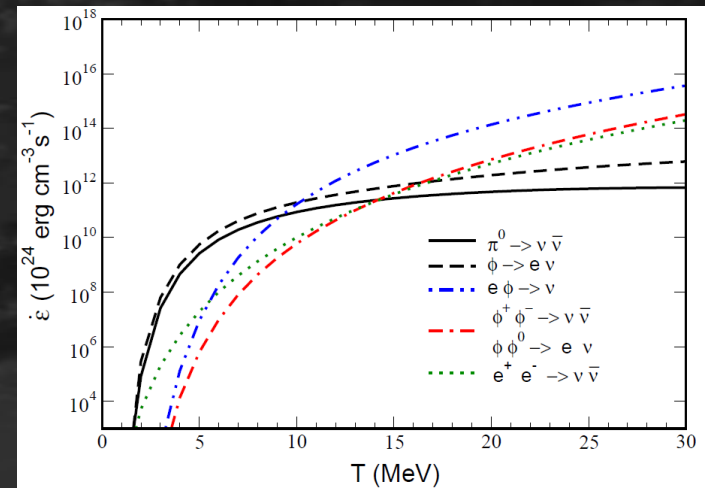
[Jaikumar et al, PRD 66 (2002) 063003],

[Reddy et al, NPA 714 (2003) 337],

[Schmitt et al, PRD 73 (2006) 034012], ...



[Sad, I.S. & Rischke, PRD 75 (2007) 065016]



[from Reddy et al, NPA 714 (2003) 337]

Future direction: Thermodynamics

- **Equation of state**

- **Pressure**

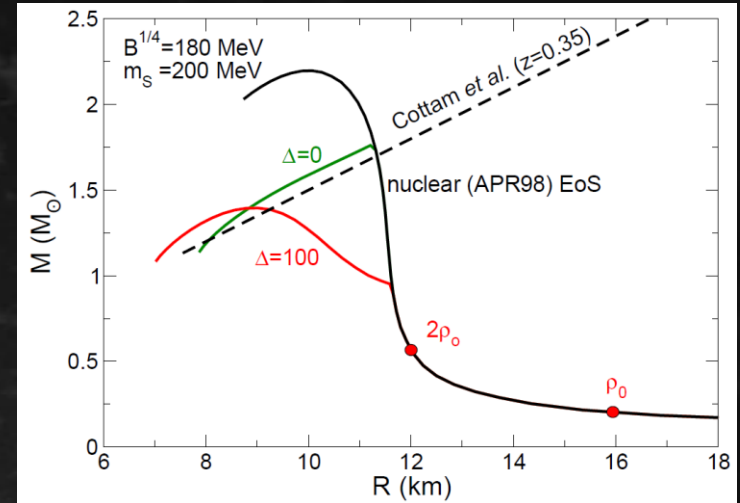
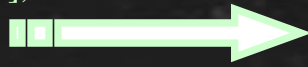
- **Energy density**

[Lugones & Horvath, PRD **66** (2002) 074017],

[Alford & Reddy, PRD **67** (2003) 074024],

[Baldo et al, 562 (2003) 163],

[Banik & Bandyopadhyay, PRD **67** (2003) 123003], ...

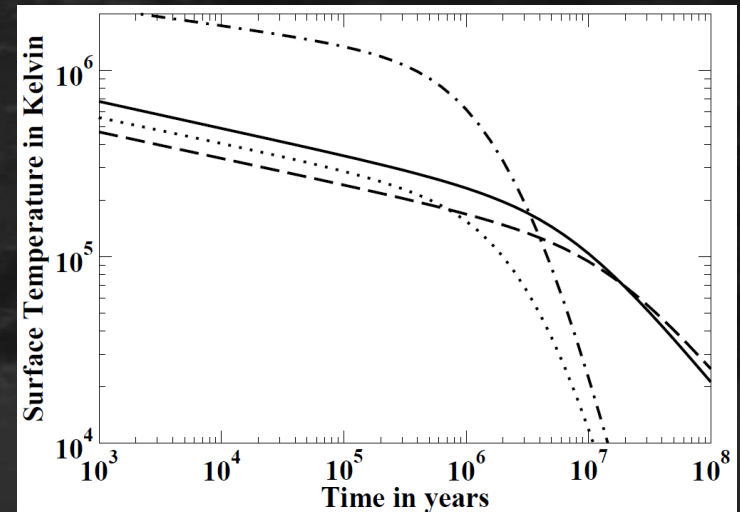
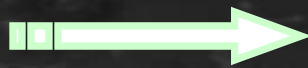


- **Specific heat**

[Alford et al, PRD **71** (2005) 114011], ...

- **Important for cooling**

- **Sensitive to gapless modes**



Detour: Atomic systems

- **Dense quark matter may be modeled in a tabletop experiment (using cold gas of ${}^6\text{Li}$ or ${}^{40}\text{K}$ atoms)**

[Zwierlein et. al., Science 311 (2006), 492], [Partridge et. al., Science 311 (2006) 503]

BEC-Side

|1⟩

B = 812 G
 $1/k_F a = 0.19$

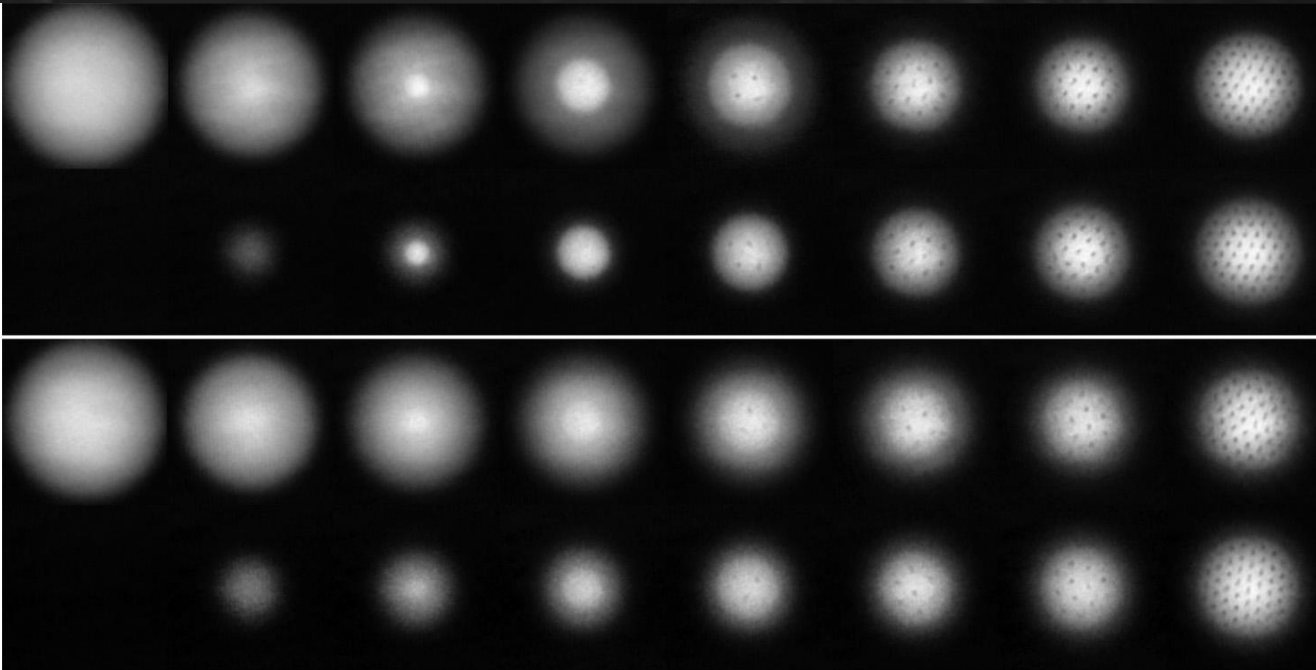
|2⟩

BCS-Side

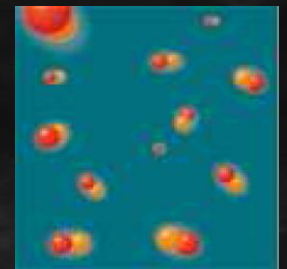
|1⟩

B = 853 G
 $1/k_F a = -0.15$

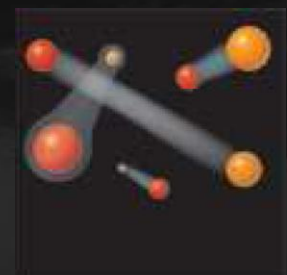
|2⟩



BEC pairs



BCS pairs



[from the web page of Ketterle's group]

Current research directions

- **Weak processes in various phases of dense quark matter**
- **Systematic study of transport properties of quark matter**
- **The study of quark matter in strong external fields**
- **Analysis of the observational data and search for signatures of new states of matter**
- **Development of non-perturbative techniques for studying quark matter**
- **High temperature quark matter (RHIC & LHC)**
- **Cross-disciplinary insight into quark dynamics (e.g., from physics of cold atoms, graphene, high- T_c superconductivity, etc.)**

Summary

- **Deconfined quark matter is likely to exist in stars**
- **β -equilibrium plays an important role in shaping the ground state**
- **Such matter is an unconventional color superconductor**
- **Phase structure of dense matter is very rich**
- **Observational data may help to shed light on the phase diagram**

Thank you