

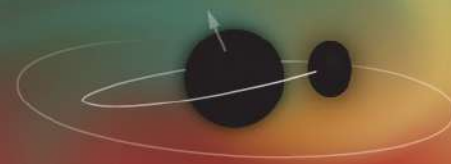
# Photon emission from strongly magnetized QCD plasma

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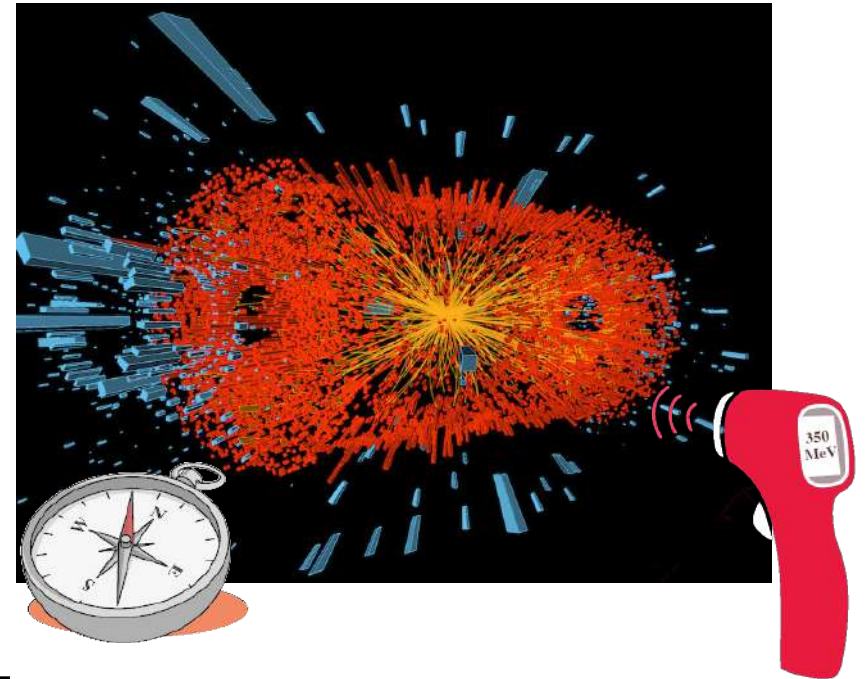
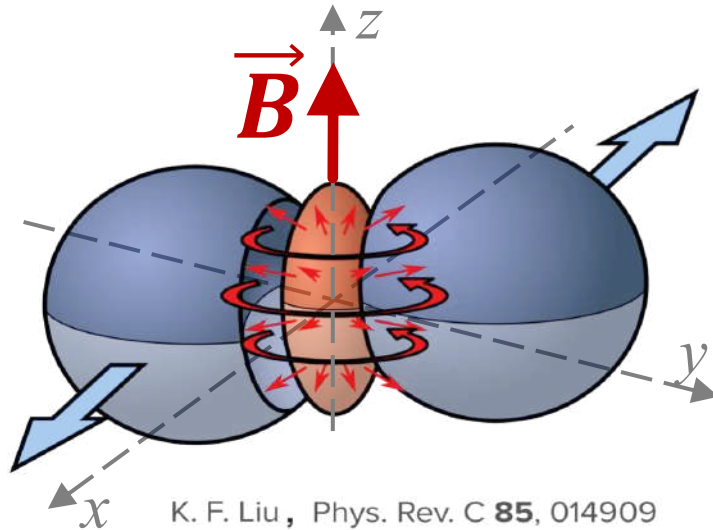
[X. Wang, I. Shovkovy, L. Yu, M. Huang, Phys. Rev. D 102, 076010 (2020)]

[X. Wang, I. Shovkovy, arXiv:2103.01967]



# Magnetic field in HICs

- QGP produced at RHIC/LHC is **magnetized**
  - $10^{18}$  to  $10^{19}$  G  $\sim m_{\pi}^2 \sim (100 \text{ MeV})^2$



## Main idea

- Photon emission is not only a **thermometer** but also **magneto**meter of QGP

# Thermal photons ( $B = 0$ )

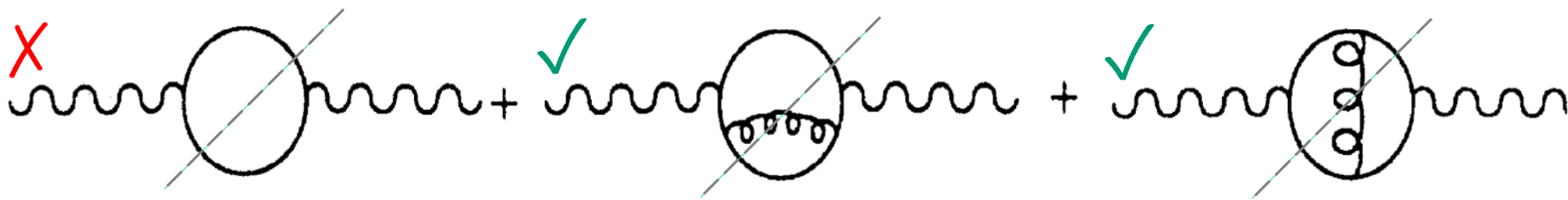
- The rate of the thermal emission of photons (more precisely, the energy loss rate) is

$$k^0 \frac{d^3 R}{dk_x dk_y dk_z} = - \frac{1}{(2\pi)^3} \frac{\text{Im} [\Pi_\mu^\mu(k)]}{\exp\left(\frac{k_0}{T}\right) - 1}$$

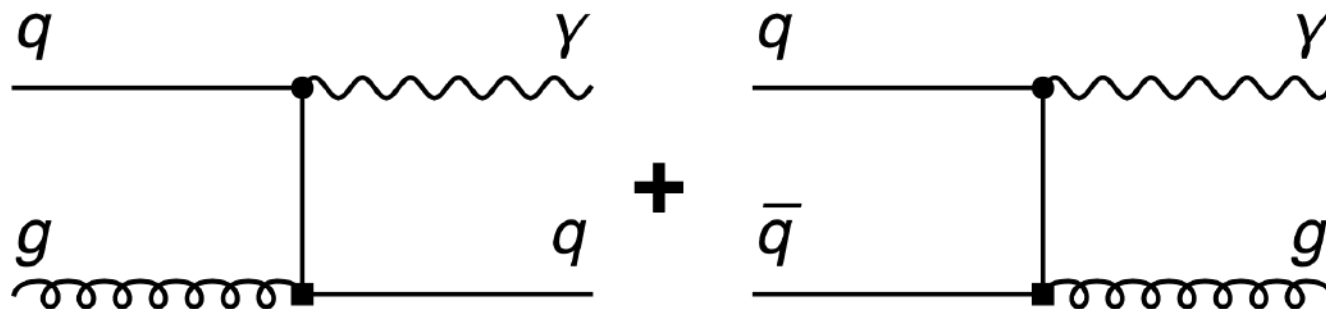
[Kapusta, Lichard, Seibert, Phys. Rev. D 44, 2774 (1991)]

[Baier, Nakkagawa, Niegawa, Redlich, Z. Physik C 53 (1992) 433]

- In the case of hot QCD plasma,



- Processes:



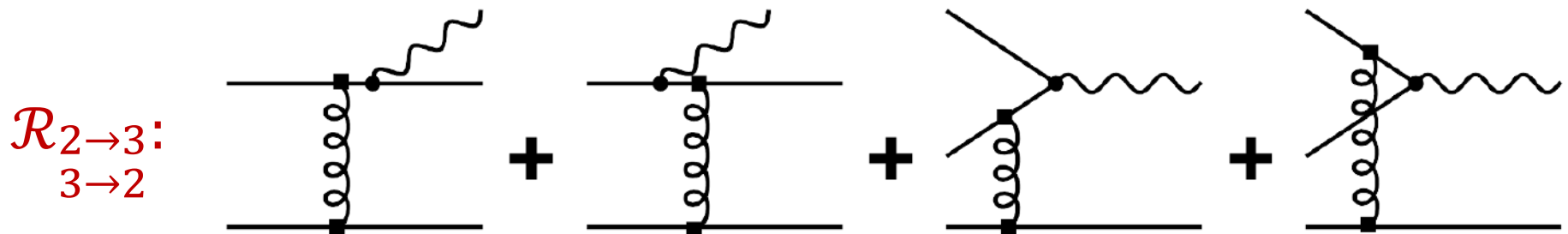
# Thermal photons ( $B = 0$ )

- The approximate result is given by

$$\mathcal{R}_{2 \rightarrow 2}: \quad E \frac{dR}{d^3p} = \frac{5}{9} \frac{\alpha \alpha_s}{2\pi^2} T^2 e^{-E/T} \ln \left( \frac{2.912 E}{g^2 T} \right)$$

[Kapusta, Lichard, Seibert, Phys. Rev. D 44, 2774 (1991)]

- There are important corrections from **bremsstrahlung** and **inelastic pair annihilation**



[Arnold, Moore, Yaffe, JHEP 12 (2001) 009; hep-ph/0111107]

- Next to leading order corrections are  $\sim 100\%$

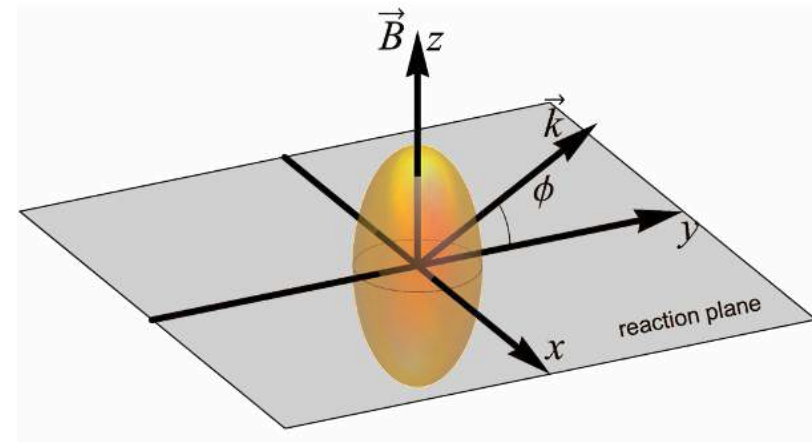
[Arnold, Moore, Yaffe, JHEP 12 (2001) 009; hep-ph/0111107]

[Ghiglieri et al., JHEP 05 (2013) 010; arXiv:1302.5970]

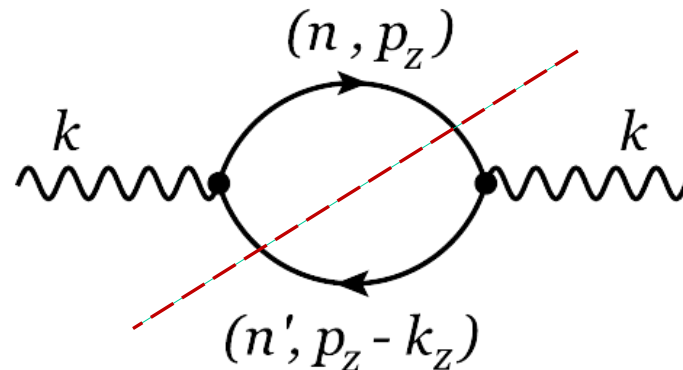
# Photon emission rate

- The expression for the rate is

$$k^0 \frac{d^3 R}{dk_x dk_y dk_z} = - \frac{1}{(2\pi)^3} \frac{\text{Im} [\Pi_\mu^\mu(k)]}{\exp\left(\frac{k_0}{T}\right) - 1}$$



- At  $\vec{B} \neq 0$ , the imaginary part of the polarization tensor

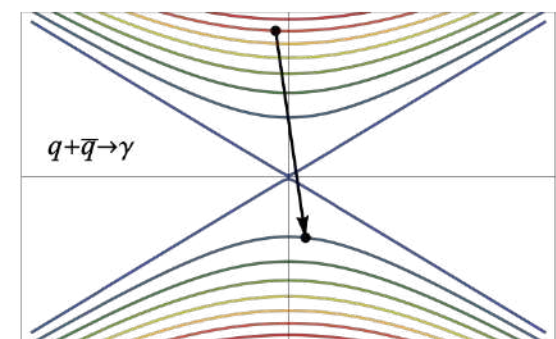
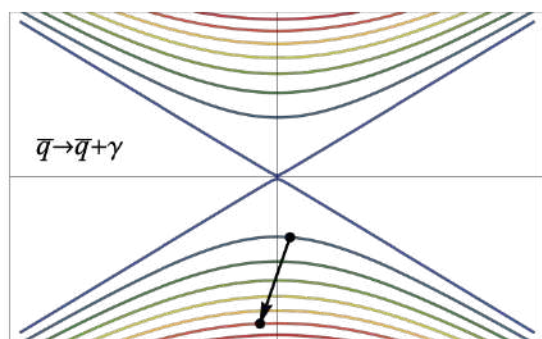
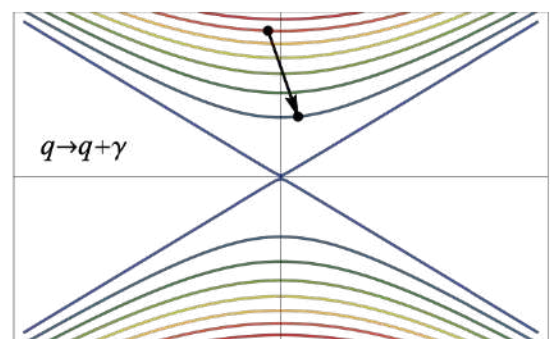
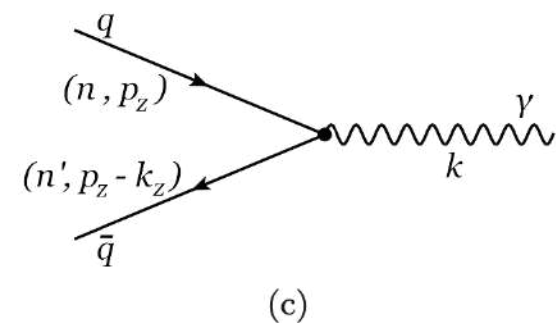
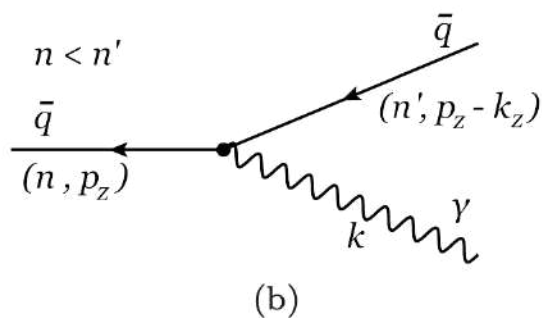
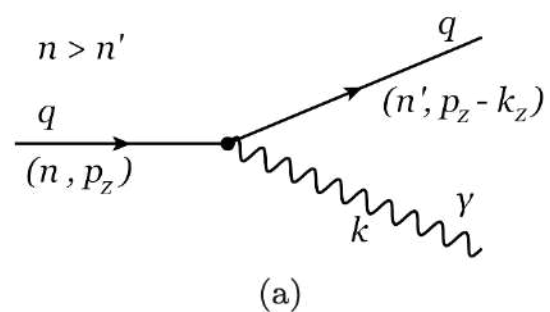


is nonzero at leading order in  $\alpha_s$ !

[Wang, Shovkovy, Yu, Huang, Phys. Rev. D 102, 076010 (2020), arXiv:2006.16254]

# Physics processes

- Relevant physics processes ( $0^{\text{th}}$  order in  $\alpha_S$ ):



The energy momentum conservation

$$E_{n,p_z,f} - \lambda E_{n',p_z-k_z,f} + \eta\Omega = 0$$

is satisfied for these  $1 \rightarrow 2$  and  $2 \rightarrow 1$  processes

[Wang, Shovkovy, Yu, Huang, Phys. Rev. D 102, 076010 (2020), arXiv:2006.16254]

# Photon emission rate

The explicit expression for  $\text{Im}[\Pi_{R,\mu}^{\mu}(\Omega, \mathbf{k})]$  is

$$\begin{aligned} \text{Im}[\Pi_{R,\mu}^{\mu}] &= \sum_{f=u,d} \frac{N_c \alpha_f}{2\pi l_f^4} \sum_{n>n'}^{\infty} \frac{g(n, n') \left[ \theta(k_-^f - |k_y|) - \theta(|k_y| - k_+^f) \right]}{\sqrt{[(k_-^f)^2 - k_y^2][(k_+^f)^2 - k_y^2]}} (\mathcal{F}_1^f + \mathcal{F}_4^f) \\ &- \sum_{f=u,d} \frac{N_c \alpha_f}{4\pi l_f^4} \sum_{n=0}^{\infty} \frac{g_0(n) \theta(|k_y| - k_+^f)}{\sqrt{k_y^2 [k_y^2 - (k_+^f)^2]}} (\mathcal{F}_1^f + \mathcal{F}_4^f), \end{aligned}$$

where  $g(n, n')$  and  $g_0(n)$  are combinations of the Fermi-Dirac distribution functions.

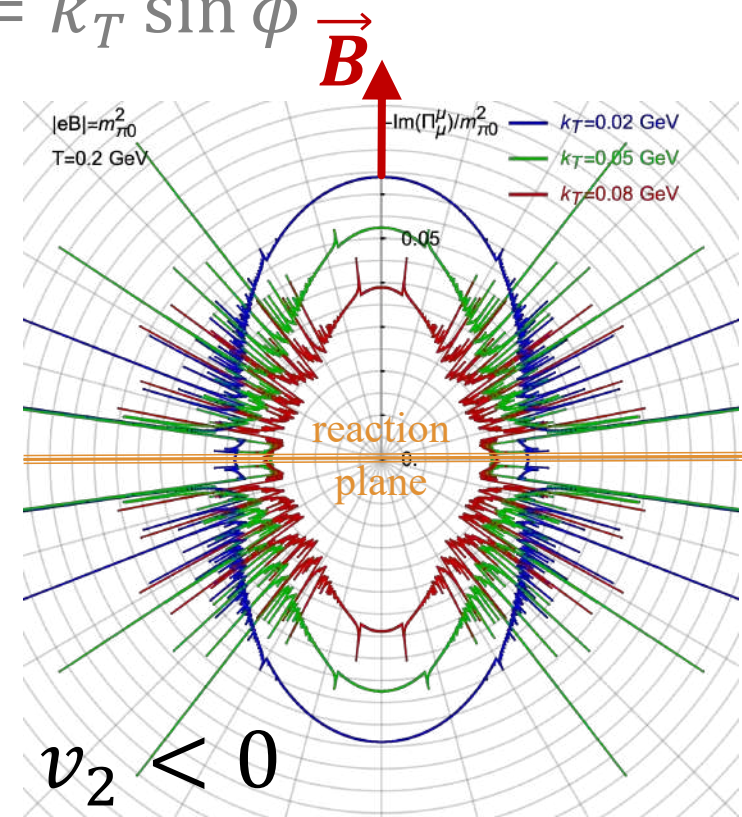
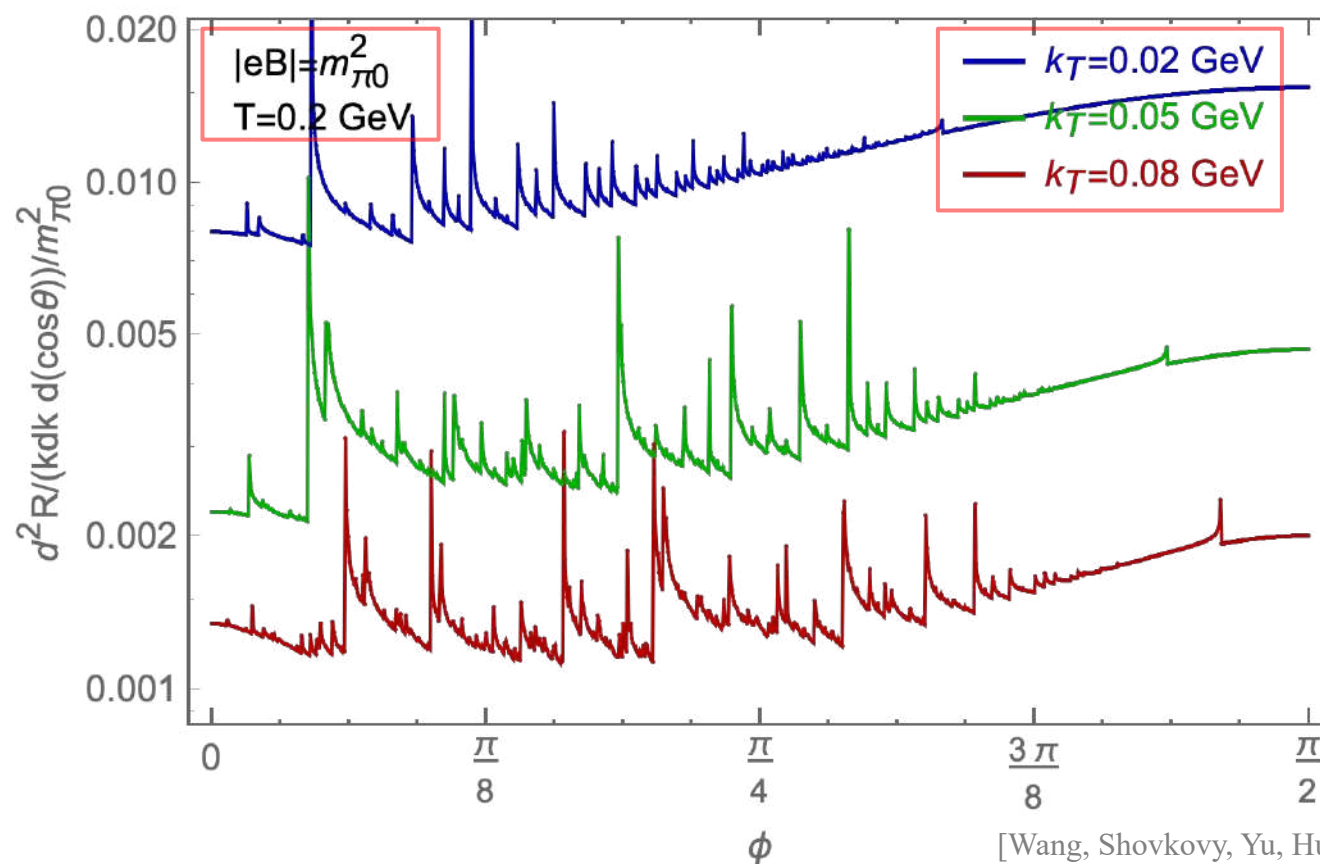
The momentum *thresholds* are determined by

$$k_{\pm}^f = \left| \sqrt{m^2 + 2n|e_f B|} \pm \sqrt{m^2 + 2n'|e_f B|} \right|$$

[Wang, Shovkovy, Yu, Huang, Phys. Rev. D 102, 076010 (2020), arXiv:2006.16254]

# Angular dependence (1)

- At small  $k_T$ , the emission rate is maximal at  $\phi = \frac{\pi}{2}$  (i.e., perpendicular to the reaction plane)
- Effectively, this gives photon “flow” with  $v_2 < 0$
- Note:  $k_x = 0$ ,  $k_y = k_T \cos \phi$  and  $k_z = k_T \sin \phi$

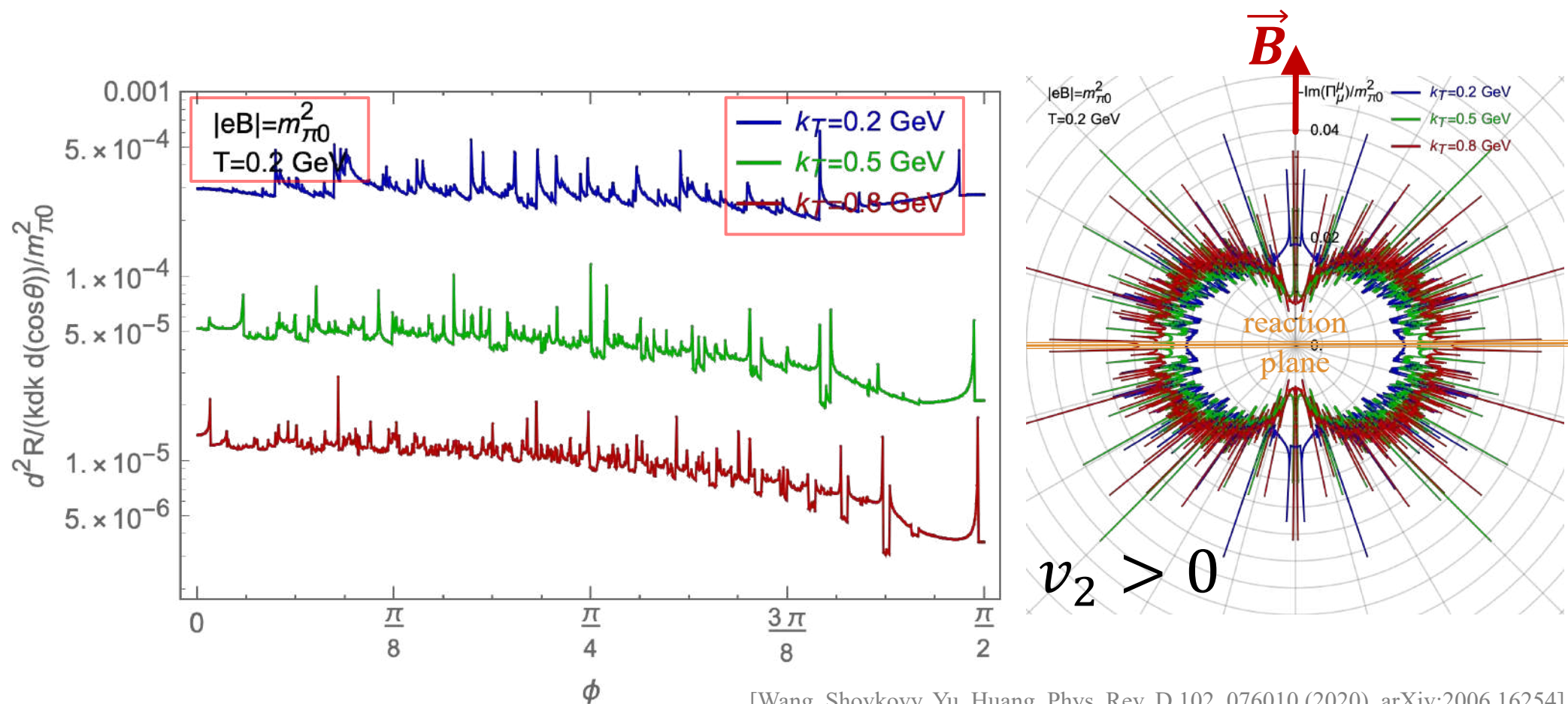


[Wang, Shovkovy, Yu, Huang, Phys. Rev. D 102, 076010 (2020), arXiv:2006.16254]



# Angular dependence (2)

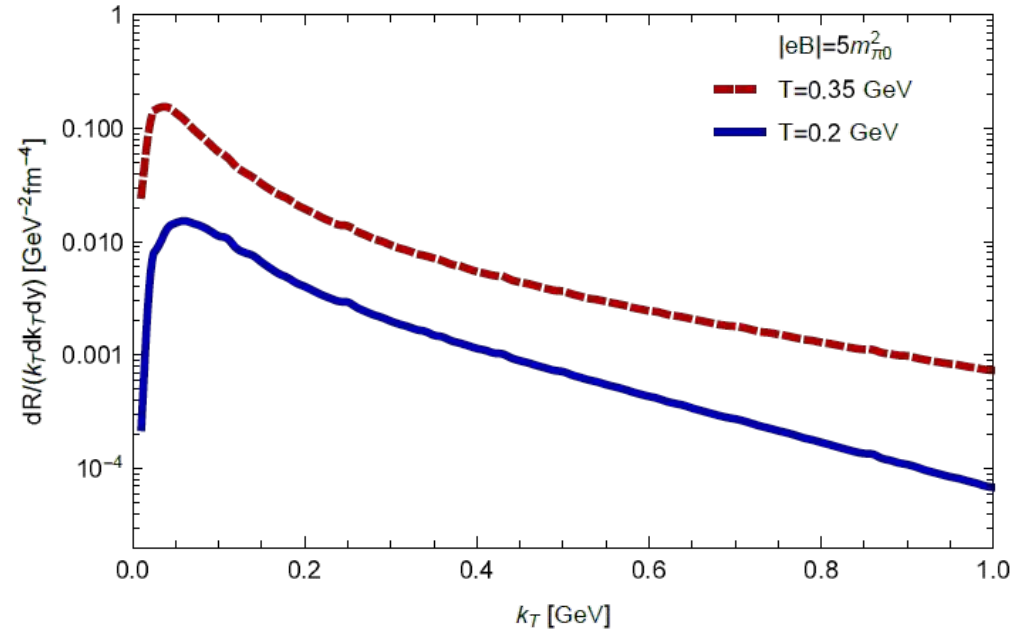
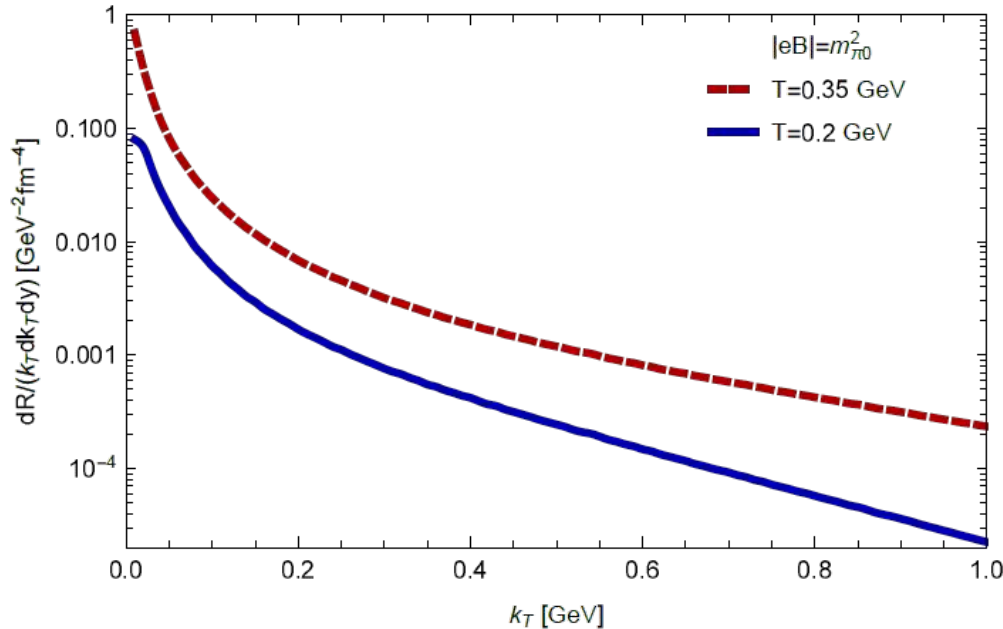
- At large  $k_T$ , the emission rate is maximal at  $\phi = 0$  (i.e., **parallel** to the reaction plane)
- Effectively, this gives photon “flow” with  $v_2 > 0$



[Wang, Shovkovy, Yu, Huang, Phys. Rev. D 102, 076010 (2020), arXiv:2006.16254]

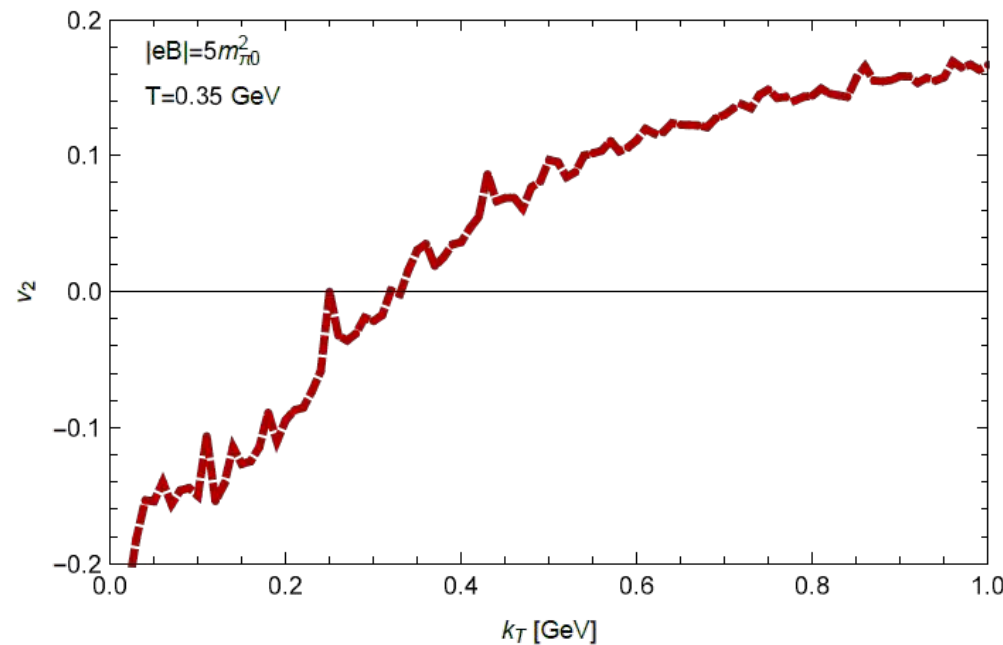
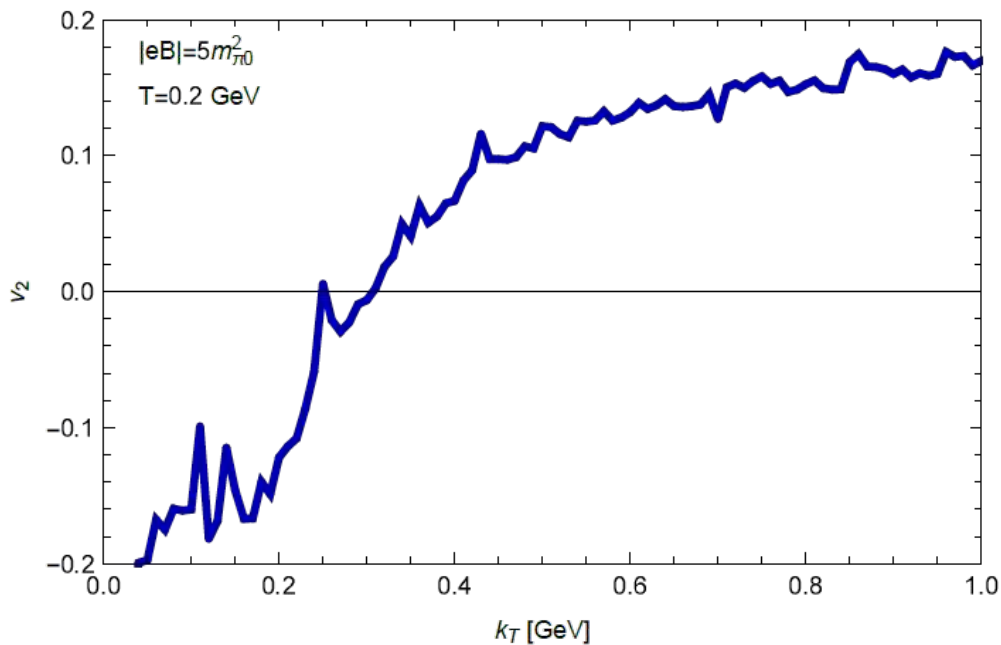
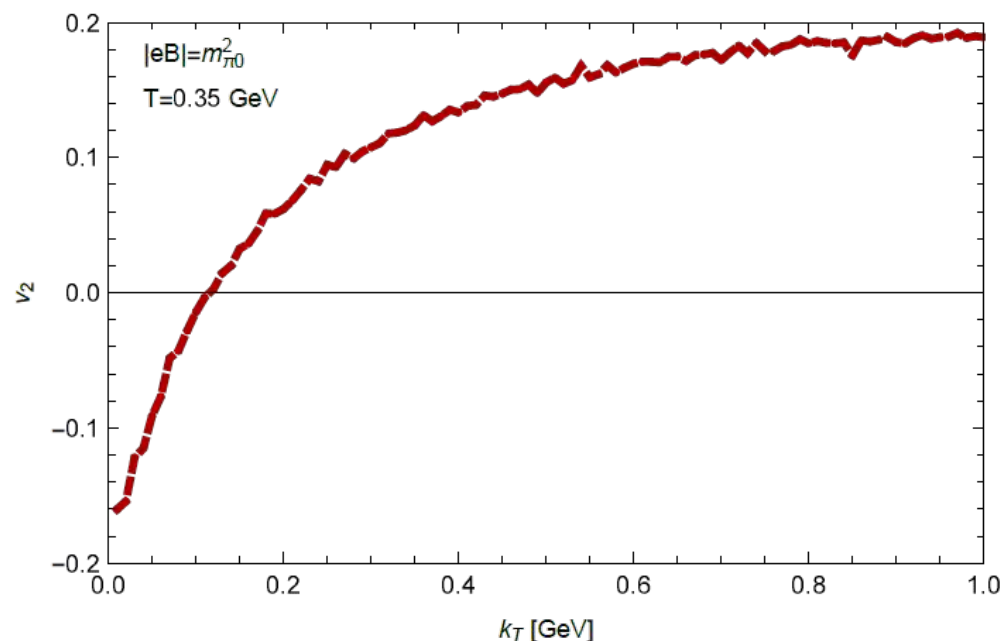
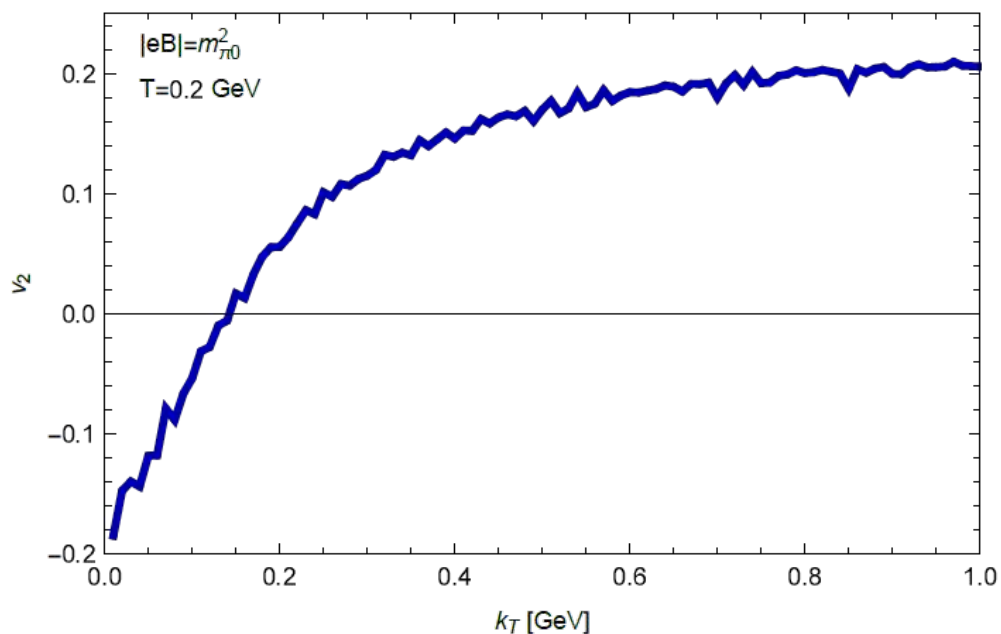
# Thermal rate at $\vec{B} \neq 0$

- The photon production rate
  - decreases with energy ( $k_T$ ) at large  $k_T$
  - increases with temperature
  - goes to zero when  $k_T \rightarrow 0$  (quantization effects)
  - has a peak at a small nonzero  $k_T$



[Wang, Shovkovy, Yu, Huang, Phys. Rev. D 102, 076010 (2020), arXiv:2006.16254]

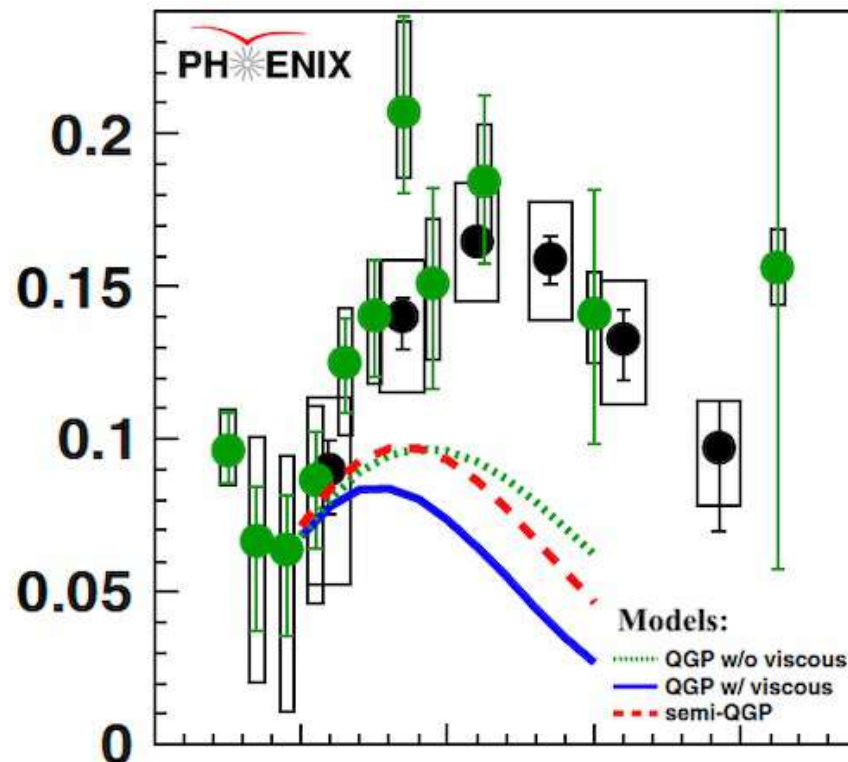
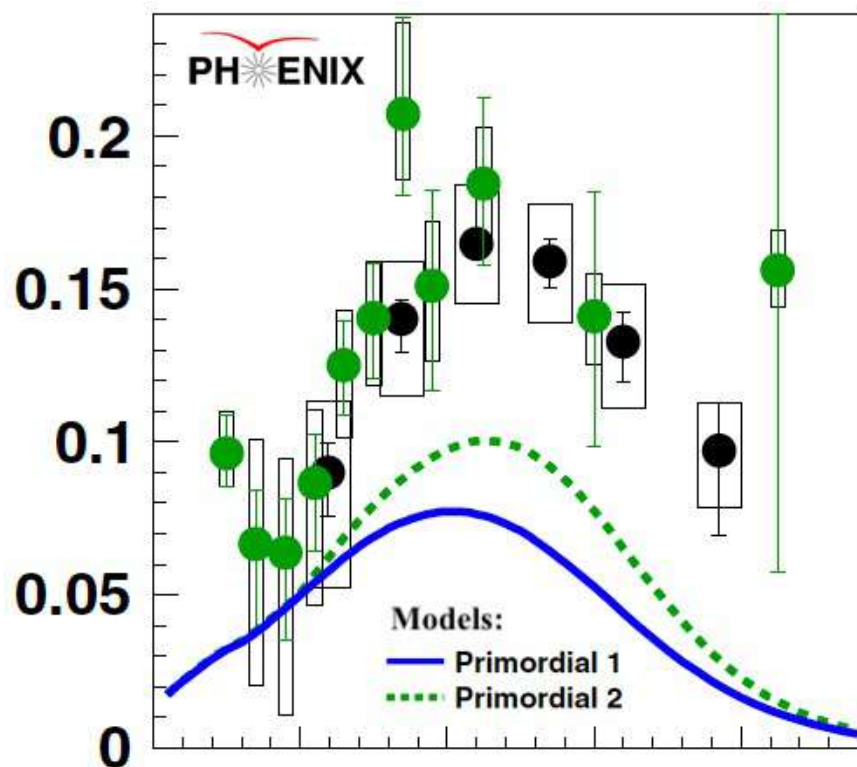
# Nonzero elliptic “flow” ( $v_2$ )



[Wang, Shovkovy, Yu, Huang, Phys. Rev. D 102, 076010 (2020), arXiv:2006.16254]

# Photon $v_2$ puzzle

- Most photons are produced early (before flow develops)
- Thus,  $v_2$  for photons should be very small



[Adare et al (PHENIX Collaboration), Phys. Rev. C **94**, 064901 (2016)]

- Estimate of  $v_2$  in a hot magnetized QGP

$$\mathcal{R}_{2 \rightarrow 1}^{1 \rightarrow 2}: \quad v_2 \sim 20\%$$

- Noting that

$$\mathcal{R}_{2 \rightarrow 1}^{1 \rightarrow 2} \sim \mathcal{R}_{2 \rightarrow 2} \sim \mathcal{R}_{2 \rightarrow 3}^{3 \rightarrow 2}$$

- Naïve estimate at  $p_T \sim 1$  GeV gives

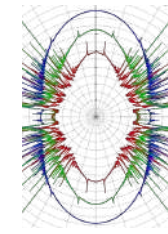
$$6.7\% \lesssim v_2 \lesssim 20\%$$

- A more realistic estimate should consider non-isotropic expansion & non-thermal processes

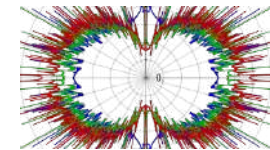
- $\vec{B} \neq 0$ : photons are produced at 0<sup>th</sup> order in  $\alpha_s$ 
  - (i)  $q \rightarrow q + \gamma$ , (ii)  $\bar{q} \rightarrow \bar{q} + \gamma$ , (iii)  $q + \bar{q} \rightarrow \gamma$

- Photon emission has pronounced ellipticity

$-v_2 < 0$  at small  $k_T$  ( $k_T \lesssim \sqrt{|eB|}$ )



$-v_2 > 0$  at large  $k_T$  ( $k_T \gtrsim \sqrt{|eB|}$ )



- A nonzero ellipticity of thermal emission is a “measure” of the magnetic field in collisions