





Dilepton emission from magnetized quark-gluon plasma Igor Shovkovy Arizona State University



Main Reference: [X. Wang and I. Shovkovy, arXiv:2205.00276] [X. Wang, I. Shovkovy, L. Yu, and M. Huang, Phys. Rev. D 102, 076010 (2020), arXiv:2006.16254] [X. Wang and I. Shovkovy, Phys. Rev. D 104, 056017 (2021), arXiv:2103.01967]

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MAGNETIZED QUARK-GLUON PLASMA

[Miransky & Shovkovy, Phys. Rep. 576, 1 (2015)]



Heavy-ion collisions

• QGP produced at RHIC/LHC is magnetized

 -10^{18} to 10^{19} G $\sim m_{\pi}^2 \sim (100 \text{ MeV})^2$



• Using Lienard-Wiechert potential, one finds

$$e\mathbf{E}(t, \mathbf{x}) = \alpha_{\text{EM}} \sum_{n \in \text{protons}} \frac{1 - v_n^2}{R_n^3 \left(1 - [\mathbf{R}_n \times \mathbf{v}_n]^2 / R_n^2\right)^{3/2}} \mathbf{R}_n$$
$$e\mathbf{B}(t, \mathbf{x}) = \alpha_{\text{EM}} \sum_{n \in \text{protons}} \frac{1 - v_n^2}{R_n^3 \left(1 - [\mathbf{R}_n \times \mathbf{v}_n]^2 / R_n^2\right)^{3/2}} \mathbf{v}_n \times \mathbf{R}_n$$

[Rafelski & Müller, PRL, 36, 517 (1976)] [Kharzeev et al., arXiv:0711.0950] [Skokov et al., arXiv:0907.1396] [Voronyuk et al., arXiv:1103.4239] [Bzdak &. Skokov, arXiv:1111.1949] [Deng & Huang, arXiv:1201.5108] [Bloczynski et al, arXiv:1209.6594]

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Magnetic field in HIC

z=0

- Magnetic field
 - strong in magnitude $\sim m_{\pi}^2$
 - short lived
 - depends strongly on b



b/2

х

0



Magnetometer for HICs

• How to measure the magnetic field of QGP in HICs?





Old idea:

- Electromagnetic probes serve as a thermometer of QGP
 New idea:
- They can be also used as a magnetometer (direct photons or dileptons)



Previous studies: [Tuchin, Phys. Rev. C 88, 024910 (2013)] [Sadooghi, Taghinavaz, Annals Phys. 376, 218 (2017)] [Bandyopadhyay et al., Phys. Rev. D 94, 114034 (2016)] [Bandyopadhyay, Mallik, Phys. Rev. D 95, 074019 (2017)] [Ghosh, Chandra, Phys. Rev. D 95, 074019 (2017)] [Islam et al., Phys. Rev. D 98, 076006 (2018)] [Islam et al., Phys. Rev. D 99, 094022 (2019)] [Das et al., Phys. Rev. D 99, 094022 (2019)] [Ghosh et al., Phys. Rev. D 101, 096002 (2020)] [Chaudhuri et al., Phys. Rev. D 103, 096021 (2021)] **y** [Das et al., arXiv:2109.00019]

DILEPTON RATE

[Wang and Shovkovy, arXiv:2205.00276]

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Dilepton rate (1)

• The differential lepton multiplicity per unit spacetime volume reads [Weldon, Phys. Rev. D 42, 2384 (1990)]

 $dR_{l\bar{l}} = 2\pi e^2 e^{-\beta\Omega} L_{\mu\nu}(Q_1, Q_2) \rho^{\mu\nu}(\Omega, \mathbf{k}) \frac{d^3\mathbf{q}_1}{(2\pi)^3 E_1} \frac{d^3\mathbf{q}_2}{(2\pi)^3 E_2}$ where the leptonic tensor (plane-wave final states) is

$$L_{\mu\nu}(Q_1, Q_2) = Q_{1\mu}Q_{2\nu} + Q_{1\nu}Q_{2\mu} - (Q_1 \cdot Q_2 + m_l^2) g_{\mu\nu}$$

 Note: leptons are Landau-level states |n_l> inside QGP but turn into plane waves when leaving it, i.e.,

 $\sum |n_l\rangle \langle n_l | Q \rangle = \langle Q |$

• The electromagnetic spectral function (to leading order in α) is $\rho^{\mu\nu}(\Omega, \mathbf{k}) = -\frac{1}{\pi} \frac{e^{\beta\Omega}}{e^{\beta\Omega} - 1} \frac{\operatorname{Im}\left[\Pi^{\mu\nu}(\Omega, \mathbf{k})\right]}{K^4}$ 92

R

 $(n', p_z - k_z)$



Dilepton rate (2)



[Wang, Shovkovy, Yu, Huang, Phys. Rev. D **102**, 076010 (2020), arXiv:2006.16254] [Wang and Shovkovy, Phys. Rev. D **104**, 056017 (2021), arXiv:2103.01967]

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Dilepton rate: explicit expression

• Explicit expression for the rate [Wang, Shovkovy, arXiv:2205.00276]

$$\frac{dR_{l\bar{l}}}{d^4K} = \frac{\alpha^2 N_c}{48\pi^5} \frac{n_B(\Omega)}{M^2} \sum_{f=u,d} \frac{q_f^2}{\ell_f^4} \left[\sum_{n=0}^{\infty} \frac{g_0(n)\theta\left(\sqrt{M^2 + k_\perp^2} - k_\perp^f\right)}{\sqrt{(M^2 + k_\perp^2)\left[M^2 + k_\perp^2 - (k_\perp^f)^2\right]}} \mathcal{F}_{n,n}^f(\xi) - 2 \sum_{n>n'}^{\infty} \frac{g(n,n')\left[\theta\left(k_\perp^f - \sqrt{M^2 + k_\perp^2}\right) - \theta\left(\sqrt{M^2 + k_\perp^2} - (k_\perp^f)\right)\right]}{\sqrt{\left[(k_\perp^f)^2 - (M^2 + k_\perp^2)\right]\left[(k_\perp^f)^2 - (M^2 + k_\perp^2)\right]}} \mathcal{F}_{n,n'}^f(\xi) \right]$$

where $g_0(n) = g(n, n)$ and

$$g(n,n') = 2 - \sum_{s_1,s_2=\pm} n_F \left(\frac{\Omega}{2} + s_1 \frac{\Omega(n-n')|e_f B|}{M^2 + k_\perp^2} + \frac{s_2|k_z|}{2(M^2 + k_\perp^2)} \sqrt{\left(M^2 + k_\perp^2 - (k_\perp^f)^2\right) \left(M^2 + k_\perp^2 - (k_\perp^f)^2\right)} \right)$$

- $\mathcal{F}_{n,n'}^{f}(\xi)$ are given in terms of generalized Laguerre polynomials
- Notation: $\xi = k_{\perp}^2 \ell_f^2 / 2$ and $k_{\pm}^f = \left| \sqrt{m^2 + 2n|e_f B|} \pm \sqrt{m^2 + 2n'|e_f B|} \right|$



Cross-check at k=0 & B=0

- The rate in the limit $k \to 0$ is related to optical conductivity $\frac{dR_{l\bar{l}}}{d^4K}\Big|_{|\mathbf{k}|\to 0} \simeq \frac{\alpha}{12\pi^4} \frac{n_B(M)}{M} \left[\sigma_{\parallel}(M) + 2\sigma_{\perp}(M)\right]$
- The optical conductivity in the limit $B \rightarrow 0$ reads [Wang, Shovkovy, arXiv:2205.00276]

$$\sigma_{\parallel}(\Omega)\big|_{B\to 0} = \sigma_{\perp}(\Omega)\big|_{B\to 0} \simeq \frac{\alpha N_c (q_u^2 + q_d^2)}{3} \Omega \tanh\left(\frac{\Omega}{4T}\right)$$

• Thus, at $k \to 0$ and $B \to 0$, one has

$$\left. \frac{dR_{l\bar{l}}}{d^4K} \right|_{|\boldsymbol{k}|\to 0, B\to 0} \simeq \frac{5\alpha^2}{36\pi^4} n_B \left(M \right) \tanh\left(\frac{M}{4T}\right)$$

• This agrees with the Born rate at B = 0, i.e.,

$$\frac{dR_{l\bar{l},\text{Born}}}{d^4K} = \frac{5\alpha^2 T}{18\pi^4 |\boldsymbol{k}|} n_B(\Omega) \ln\left(\frac{\cosh\frac{\Omega + |\boldsymbol{k}|}{4T}}{\cosh\frac{\Omega - |\boldsymbol{k}|}{4T}}\right)$$

[Cleymans, Fingberg, Redlich, Phys. Rev. D 35, 2153 (1987)]



NUMERICAL RESULTS

[Wang and Shovkovy, arXiv:2205.00276]

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Results: integrated rate



- Overall, dilepton rate grows with temperature
- Large enhancement is seen at small invariant masses, $M \leq \sqrt{|eB|}$

[Wang, Shovkovy, arXiv:2205.00276]



• Dilepton rate tends to decrease with increasing k_T



- The angular dependence indicates a possible nonzero v_2
- A nonvanishing v_2 is most prominent at small M and large k_T

[Wang, Shovkovy, arXiv:2205.00276]



Ellipticity of dilepton emission

• Definition:

 $v_2(M, k_T) = \frac{\int_0^{2\pi} d\phi \cos(2\phi) \left(dR_{l\bar{l}}/d^4k \right)}{\int_0^{2\pi} d\phi \left(dR_{l\bar{l}}/d^4k \right)}$



- Ellipticity is large $(v_2 \leq 0.2)$ for $M \leq \sqrt{|eB|}$ and $k_T \gg \sqrt{|eB|}$
- On the other hand, $v_2 \approx 0$ for $M \gg \sqrt{|eB|}$ and all k_T

[[]Wang, Shovkovy, arXiv:2205.00276]



Angular dependence @ small M

 $k_T = 0.5 \text{ GeV}, T = 0.2 \text{ GeV}, |eB| = m_{\pi}^2$

• The ellipticity is well pronounced at small M and large k_T

 $|eB| = m_{\pi}^2$



• Note: magnetic field strongly enhances the rate at small M



Angular dependence @ small M

 $k_T = 0.5 \text{ GeV}, T = 0.2 \text{ GeV}, |eB| = 5m_\pi^2$

• The ellipticity is well pronounced at small M and large k_T

 $|eB| = 5m_{\pi}^2$



• Note: magnetic field strongly enhances the rate at small M

Angular dependence @ large M

 $k_T = 0.5 \text{ GeV}, T = 0.2 \text{ GeV}, |eB| = m_{\pi}^2$

The ellipticity is approximately vanishing at large M

 $|eB| = m_{\pi}^2$



• Note: magnetic field does not affect much dilepton rate M

Angular dependence @ large M

 $k_T = 0.5 \text{ GeV}, T = 0.2 \text{ GeV}, |eB| = 5m_{\pi}^2$

The ellipticity is approximately vanishing at large M

 $|eB| = 5m_{\pi}^2$



• Note: magnetic field does not affect much dilepton rate at large M

=0.5 Ge



Summary

- Magnetic field strongly enhances the dilepton rate at small invariant masses, $M \leq \sqrt{|eB|}$
- Dilepton emission rate is non-isotropic when $B \neq 0$

 $v_2 \lesssim 0.2$ when $M \lesssim \sqrt{|eB|}$ and $k_T \gg \sqrt{|eB|}$

 $v_2 \simeq 0$ when $M \gg \sqrt{|eB|}$ all k_T

• Dilepton rate and ellipticity together can provide indirect measurements of the magnetic field in HICs







