

## LIMDEP TUTORIAL BY MIN AHN

### INSTRUCTION FOR ACCESSING AN INSTRUCTOR VOLUME

1. At the ASU PC Network logon you will get a message: "Click OK for the next two requests."

Click on the **OK** button here.

Click **OK** and wait 1-2 minutes while the logon scripts execute.

Click **OK** to get to the sign on screen with the ASU logo displayed over an ASU photograph back ground.

2. At the sign on screen enter your **ASURITE ID** and **password**. Enter both items in lower case.

Click on **OK**.

Wait during the message "Mounting AFS volumes." Soon the Window 95 desktop will be displayed.

3. Double click on the **Applications** folder icon on the desktop.
4. Double click on the **Instructor Volumes** folder icon on the desktop.
5. Find the icon named **ECN527**, and double click on it.
6. The U: drive instructor volume is now mounted but you can not see it until the current window is closed. Close the instructor volume window by clicking on **X** in the upper right corner of the window.
7. Double click on the **U: drive** icon on the desktop.
8. Go to the directory Limdep/Program. Click on the **LIMDEP** icon.
9. Now you entered the LIMDEP program (Version 7.0 for windows).

When you have finished using the instructors volume, be sure to LOG OUT so that the next computer user does not have access to your files.

10. Double click on the **Log Out** icon on the desktop. Click on **Log Me Out**. DO NOT turn the computer off.

## HOW TO READ DATA

### Basic Format:

```
READ ; NOBS = ...
      ; NVAR = ...
      ; NAMES = ... (THE NAMES OF VARIABLES)
      ; FILE = ... (THE FILE CONTAINING RAW DATA)
      ; FORMAT = ... (SEE LIMDEP MANUAL)      $
```

### Example: Using MWPSID82.DB (MW\_READ.LIM)

```
READ ; NOBS=1962; NVAR=25
      ; FILE=MWPSID82.DB
      ; NAMES=  NLF,      EMP,      WRATE,  LRATE,  ED,
                URB,      MINOR,   AGE,     TENURE, EXP,
                REGS,     OCCW,     OCCB,   INDUMG, INDUMN,
                UNION,    UNEMPR,   OFINC,  LOFINC, KIDS,
                WUNE80,   HWORK,    USPELL,  SEARCH, KIDS5 $

CREATE; LF = 1 - NLF $
```

- (1) This problem is available in MW\_READ.LIM. Run the program to read the data, MWPSID82.DB
- (2) To save the data, click **File/Project save as**.

## PROBIT ESTIMATION

### Example: (MW\_PROB.LIM)

```
/* Basic Program */

title ; Employment Probability $
probit ; lhs = emp
        ; rhs = one,ed,urb,minor,lofinc
        ; maxit = 1000
        ; start = 0,0,0,0,0
        ; tlf = 0.00001 ; tlb = 0.00001 ; tlg = 0.00001
        ; alg = newton ? Can choose bhhh, bfgs, dfp, stedes
        ; margin $ ? estimate p = Pr(y=1) at sample mean

? Saving estimates and covariance matrix
```

```

matrix ; prb = b ; prc = varb $

? Saving the value of likelihood function

calc ; plogl = logl $

/* Testing hypotheses */

/*
Wald tests can be computed for any restriction
LM or LR tests can be computed for certain restrictions:
    equality between parameters or zero restriction

For example,

    Hypo 1: b(1) = 0, b(2) = b(3)
    Hypo 2: b(1) = 0, b(2) = b(3), b(4) = b(2)+ b(3)
    Hypo 3: b(1) = 0, b(2) = b(3), b(4)^2 = b(5)

Wald can be used for any of these hypotheses.
LR or LM can be used only for Hypo 1.

*/

/* Testing hypo 1 */

? Unrestricted Model

namelist ; x = one,ed,urb,minor,lofinc $
probit ; lhs = emp
        ; rhs = x
        ; maxit = 1000 $

matrix ; uprb = b ; uprc = varb $
calc ; ulogl = logl $

? Restricted Model

probit ; lhs = emp
        ; rhs = x
        ; maxit = 1000
        ; rst = 0,b2,b2,b4,b5 $

matrix ; rprb = b $
calc ; rlogl = logl $

```

? [Wald Test]

```
title; Wald test for b1 = 0 and b2 = b3 $
wald ; labels = b1,b2,b3,b4,b5
      ; start = uprb; var = uprc ;
      ; fn1    = b1
      ; fn2    = b2 - b3      $
```

? [LR test]

```
title; LR test for b1 = 0 and b2 = b3 $
calc ; list
      ; lrt  = 2*(ulogl - rlogl)
      ; pval = 1 - chi(lrt,2) $
```

? [LM test]

```
probit ; lhs  = emp; rhs  = x
        ; start = rprb ; maxit = 0 $
```

```
title ; LM test for b1 = 0 and b2 = b3 $
calc  ; list
        ; lmt = lmstat
        ; pval = 1 - chi(lmt,2)  $
```

/\* Wald for hypo 3 \*/

```
title; Wald test for b1 = 0, b2 = b3 and b4^2 = b5  $
wald ; labels = b1,b2,b3,b4,b5
      ; start  = uprb
      ; var    = uprc
      ; fn1    = b1 ;fn2 = b2 - b3; fn3 = b4^2-b5 $
```

/\* Estimating Pr(y=1) and dPr(y=1)/dx\_j \*/

? Estimating Pr(y=1) at mean of x  
? Based on unrestricted probit

```
matrix ; mx  = mean(x) $ ? It is a column vector
calc   ; xb1 = mx(1,1) ; xb2 = mx(2,1); xb3 = mx(3,1)
        ; xb4 = mx(4,1) ; xb5 = mx(5,1)  $
```

```
title ; Pr(emp=1) at means of regressors $
wald  ; labels = b1,b2,b3,b4,b5; start = uprb; var = uprc;
      ; fn1    = phi(xb1*b1+xb2*b2+xb3*b3+xb4*b4+xb5*b5) $
```

? Estimating  $dPr(y=1)/dx$

```
title ; Marginal effects $
wald ; labels = b1,b2,b3,b4,b5
      ; start = uprb
      ; var = uprc
      ; fn1 = xb1*b1+xb2*b2+xb3*b3+xb4*b4+xb5*b5
      ; fn2 = n01(fn1)*b1
      ; fn3 = n01(fn1)*b2
      ; fn4 = n01(fn1)*b3 $
```

### Output:

```
--> RESET
--> LOAD;file="C:\Aaschool\ECON727\DATA\MW.lpj"$
LOAD has reconstructed your previous session.
--> title ; Employment Probability
probit ; lhs = emp
      ; rhs = one,ed,urb,minor,lofinc
      ; maxit = 1000
      ; start = 0,0,0,0,0
      ; tlf = 0.00001 ; tlb = 0.00001 ; tbg = 0.00001
      ; alg = newton ? Can choose bhhh, bfgs, dfp, stedes
      ; margin $ ? estimate p = Pr(y=1) at sample mean
--> matrix ; prb = b ; prc = varb $
--> calc ; plogl = logl $
--> namelist ; x = one,ed,urb,minor,lofinc $
--> probit ; lhs = emp
      ; rhs = x
      ; maxit = 1000 $
```

```
+-----+
| Dependent variable is binary, y=0 or y not equal 0
| Ordinary least squares regression Weighting variable = none
| Dep. var. = EMP Mean= .4704383282 , S.D.= .4992525893
| Model size: Observations = 1962, Parameters = 5, Deg.Fr.= 1957
| Residuals: Sum of squares= 474.9962035 , Std.Dev.= .49266
| Fit: R-squared= .028211, Adjusted R-squared = .02622
| Model test: F[ 4, 1957] = 14.20, Prob value = .00000
| Diagnostic: Log-L = -1392.4945, Restricted(b=0) Log-L = -1420.5675
| LogAmemiyaPrCrt.= -1.413, Akaike Info. Crt.= 1.425
+-----+
```

Variable	Coefficient	Standard Error	b/St.Er.	P[ Z >z]	Mean of X
Constant	.9170578290	.17362375	5.282	.0000	
ED	.2915849316E-01	.51513883E-02	5.660	.0000	12.205403
URB	.6459244774E-01	.24441441E-01	2.643	.0082	.68654434
MINOR	.2566128748E-01	.26742220E-01	.960	.3373	.27166157
LOFINC	-.8619967756E-01	.17367289E-01	-4.963	.0000	9.9052275

Normal exit from iterations. Exit status=0.

```

+-----+
| Binomial Probit Model
| Maximum Likelihood Estimates
| Dependent variable           EMP
| Weighting variable           ONE
| Number of observations       1962
| Iterations completed         4
| Log likelihood function      -1327.781
| Restricted log likelihood     -1356.524
| Chi-squared                  57.48581
| Degrees of freedom           4
| Significance level            .0000000
+-----+

```

```

+-----+-----+-----+-----+-----+-----+
| Variable | Coefficient | Standard Error | b/St.Er. | P[|Z|>z] | Mean of X |
+-----+-----+-----+-----+-----+-----+
|          |             |                |           |           |           |
| Index function for probability
| Constant 1.228085188 .47320614 2.595 .0095
| ED .7629799963E-01 .13446644E-01 5.674 .0000 12.205403
| URB .1708719958 .63111585E-01 2.707 .0068 .68654434
| MINOR .5968648873E-01 .68899573E-01 .866 .3863 .27166157
| LOFINC -.2390755461 .48122027E-01 -4.968 .0000 9.9052275

```

Frequencies of actual & predicted outcomes  
 Predicted outcome has maximum probability.

```

          Predicted
-----+-----+-----+-----+
Actual   0    1  | Total
-----+-----+-----+-----+
    0     740 299 | 1039
    1     527 396 |  923
-----+-----+-----+-----+
Total    1267 695 | 1962

```

```

--> matrix ; uprb = b ; uprc = varb $
--> calc   ; ulogl = logl           $
--> probit ; lhs = emp
          ; rhs = x
          ; maxit = 1000
          ; rst = 0,b2,b2,b4,b5 $

```

```

+-----+
| Dependent variable is binary, y=0 or y not equal 0
| Ordinary least squares regression Weighting variable = none
| Dep. var. = EMP Mean= .4704383282 , S.D.= .4992525893
| Model size: Observations = 1962, Parameters = 5, Deg.Fr.= 1957
| Residuals: Sum of squares= 474.9962035 , Std.Dev.= .49266
| Fit: R-squared= .028211, Adjusted R-squared = .02622
| Model test: F[ 4, 1957] = 14.20, Prob value = .00000
| Diagnostic: Log-L = -1392.4945, Restricted(b=0) Log-L = -1420.5675
| LogAmemiyaPrCrt.= -1.413, Akaike Info. Crt.= 1.425
+-----+

```

```

+-----+-----+-----+-----+-----+-----+
| Variable | Coefficient | Standard Error | b/St.Er. | P[|Z|>z] | Mean of X |
+-----+-----+-----+-----+-----+-----+
| Constant .9170578290 .17362375 5.282 .0000
| ED .2915849316E-01 .51513883E-02 5.660 .0000 12.205403
| URB .6459244774E-01 .24441441E-01 2.643 .0082 .68654434
| MINOR .2566128748E-01 .26742220E-01 .960 .3373 .27166157
| LOFINC -.8619967756E-01 .17367289E-01 -4.963 .0000 9.9052275

```

Normal exit from iterations. Exit status=0.

```

+-----+
| Binomial Probit Model
| Maximum Likelihood Estimates
| Dependent variable           EMP
| Weighting variable          ONE
| Number of observations      1962
| Iterations completed        4
| Log likelihood function     -1331.862
| Restricted log likelihood   -1356.524
| Chi-squared                 49.32278
| Degrees of freedom          2
| Significance level          .0000000
+-----+

```

```

+-----+
|Variable | Coefficient | Standard Error |b/St.Er.| P[|Z|>z] | Mean of X|
+-----+
|
| Index function for probability
| Constant .0000000000 .....(Fixed Parameter).....
| ED .8579347233E-01 .12778130E-01 6.714 .0000 12.205403
| URB .8579347233E-01 .12778130E-01 6.714 .0000 .68654434
| MINOR .1336072788 .63756953E-01 2.096 .0361 .27166157
| LOFINC -.1233762049 .17163930E-01 -7.188 .0000 9.9052275
+-----+

```

Frequencies of actual & predicted outcomes  
 Predicted outcome has maximum probability.

```

          Predicted
-----+-----+
Actual   0   1 | Total
-----+-----+
   0     756 283 | 1039
   1     571 352 |  923
-----+-----+
Total    1327 635 | 1962

```

```

--> matrix ; rprb = b      $
--> calc   ; rlogl = logl $
--> title; Wald test for b1 = 0 and b2 = b3 $
--> wald ; labels = b1,b2,b3,b4,b5
      ; start = uprb
      ; var   = uprc
      ; fn1  = b1
      ; fn2  = b2 - b3      $

```

```

+-----+
| WALD procedure. Estimates and standard errors
| for nonlinear functions and joint test of
| nonlinear restrictions.
| Wald Statistic           =      8.06527
| Prob. from Chi-squared[ 2] =      .01773
+-----+

```

```

+-----+
|Variable | Coefficient | Standard Error |b/St.Er.| P[|Z|>z] | Mean of X|
+-----+
| Fncn( 1) 1.228085188 .47320614 2.595 .0095
| Fncn( 2) -.9457399616E-01 .65465798E-01 -1.445 .1486
+-----+

```

```

--> title; LR test for b1 = 0 and b2 = b3 $
--> calc ; list
      ; lrt = 2*(ulogl - rlogl)
      ; pval = 1 - chi(lrt,2) $
      LRT   = .81630295544032380D+01
      PVAL  = .16881874007718900D-01

```

```
--> probit ; lhs = emp
; rhs = x
; start = rprb
; maxit = 0 $
```

```
+-----+
| Dependent variable is binary, y=0 or y not equal 0
| Ordinary least squares regression Weighting variable = none
| Dep. var. = EMP Mean= .4704383282 , S.D.= .4992525893
| Model size: Observations = 1962, Parameters = 5, Deg.Fr.= 1957
| Residuals: Sum of squares= 474.9962035 , Std.Dev.= .49266
| Fit: R-squared= .028211, Adjusted R-squared = .02622
| Model test: F[ 4, 1957] = 14.20, Prob value = .00000
| Diagnostic: Log-L = -1392.4945, Restricted(b=0) Log-L = -1420.5675
| LogAmemiyaPrCrt.= -1.413, Akaike Info. Crt.= 1.425
+-----+
```

Variable	Coefficient	Standard Error	b/St.Er.	P[ Z >z]	Mean of X
Constant	.9170578290	.17362375	5.282	.0000	
ED	.2915849316E-01	.51513883E-02	5.660	.0000	12.205403
URB	.6459244774E-01	.24441441E-01	2.643	.0082	.68654434
MINOR	.2566128748E-01	.26742220E-01	.960	.3373	.27166157
LOFINC	-.8619967756E-01	.17367289E-01	-4.963	.0000	9.9052275

Maximum iterations reached. Exit iterations with status=1.  
Maxit = 0. Computing LM statistic at starting values.  
No iterations computed and no parameter update done.

```
+-----+
| Binomial Probit Model
| Maximum Likelihood Estimates
| Dependent variable EMP
| Weighting variable ONE
| Number of observations 1962
| Iterations completed 1
| LM Stat. at start values 8.027283
| LM statistic kept as scalar LMSTAT
| Log likelihood function -1331.862
| Restricted log likelihood -1356.524
| Chi-squared 49.32278
| Degrees of freedom 4
| Significance level .0000000
+-----+
```

Variable	Coefficient	Standard Error	b/St.Er.	P[ Z >z]	Mean of X
Index function for probability					
Constant	.0000000000	.46145275	.000	1.0000	
ED	.8579347233E-01	.13444274E-01	6.381	.0000	12.205403
URB	.8579347233E-01	.62895744E-01	1.364	.1725	.68654434
MINOR	.1336072788	.68714027E-01	1.944	.0518	.27166157
LOFINC	-.1233762049	.46617697E-01	-2.647	.0081	9.9052275

Frequencies of actual & predicted outcomes  
Predicted outcome has maximum probability.

Actual	Predicted		Total
	0	1	
0	756	283	1039
1	571	352	923
Total	1327	635	1962

```

--> title ; LM test for b1 = 0 and b2 = b3 $
--> calc ; list
; lmt = lmstat
; pval = 1 - chi(lmt,2) $

LMT = .80272833001843540D+01
PVAL = .18067479861156980D-01

--> title; Wald test for b1 = 0, b2 = b3 and b4^4 = b5 $
--> wald ; labels = b1,b2,b3,b4,b5
; start = uprb
; var = uprc
; fn1 = b1
; fn2 = b2 - b3
; fn3 = b4^2 - b5 $

```

```

+-----+
| WALD procedure. Estimates and standard errors |
| for nonlinear functions and joint test of    |
| nonlinear restrictions.                      |
| Wald Statistic = 52.38105                   |
| Prob. from Chi-squared[ 3] = .00000        |
+-----+

```

```

+-----+-----+-----+-----+-----+
|Variable | Coefficient | Standard Error | b/St.Er. | P[|Z|>z] | Mean of X|
+-----+-----+-----+-----+-----+
Fncn( 1) | 1.228085188 | .47320614      | 2.595     | .0095    |
Fncn( 2) | -.9457399616E-01 | .65465798E-01 | -1.445    | .1486    |
Fncn( 3) | .2426380230   | .46728575E-01 | 5.192     | .0000    |

```

```

--> matrix ; mx = mean(x) $ ? It is a column vector
--> calc ; xb1 = mx(1,1)
; xb2 = mx(2,1)
; xb3 = mx(3,1)
; xb4 = mx(4,1)
; xb5 = mx(5,1) $
--> title ; Pr(emp=1) at means of regressors $
--> wald ; labels = b1,b2,b3,b4,b5
; start = uprb
; var = uprc
; fn1 = phi(xb1*b1+xb2*b2+xb3*b3+xb4*b4+xb5*b5) $

```

```

+-----+
| WALD procedure. Estimates and standard errors |
| for nonlinear functions and joint test of    |
| nonlinear restrictions.                      |
| Wald Statistic = 1710.21762                 |
| Prob. from Chi-squared[ 1] = .00000        |
+-----+

```

```

+-----+-----+-----+-----+-----+
|Variable | Coefficient | Standard Error | b/St.Er. | P[|Z|>z] | Mean of X|
+-----+-----+-----+-----+-----+
Fncn( 1) | .4700122978   | .11365369E-01 | 41.355    | .0000    |

```

```

--> title ; Marginal effects $
--> wald ; labels = b1,b2,b3,b4,b5
; start = uprb
; var = uprc
; fn1 = xb1*b1+xb2*b2+xb3*b3+xb4*b4+xb5*b5
; fn2 = n01(fn1)*b1
; fn3 = n01(fn1)*b2
; fn4 = n01(fn1)*b3 $

```

```

+-----+
| WALS procedure. Estimates and standard errors |
| for nonlinear functions and joint test of    |
| nonlinear restrictions.                      |
| Wald Statistic = 60.67600                   |
| Prob. from Chi-squared[ 4] = .00000        |
+-----+

```

Variable	Coefficient	Standard Error	b/St.Er.	P[ Z >z]	Mean of X
Fncn( 1)	-.7523894869E-01	.28569505E-01	-2.634	.0084	
Fncn( 2)	.4885503289	.18831825	2.594	.0095	
Fncn( 3)	.3035246511E-01	.53493381E-02	5.674	.0000	
Fncn( 4)	.6797539012E-01	.25106007E-01	2.708	.0068	

[EXERCISE] Use MWPSID82.DB. Do probit for:

LHS=EMP,  
RHS=ONE, ED, URB, MINOR, AGE, REGS, UNEMPR, LOFINC, KIDS5,  
EXP.

Construct Wald, LR and LM statistics for  $H_0$ : no effect of other family income, and the effect of AGE = the effect of EXP.

[EXERCISE] Use MWPSID82.DB. Do PROBIT as you did above. Estimate the same model by BHHH. Compare your new result with the result from the above program.

## INFORMATION ON MWPSID82.DB

This is the data set of married women in 1981 sampled from PSID. Total number of observations are 1962, and 25 variables are observed.

VARIABLES	DEFINITION
NLF	NLF=1 IF NON-LABOR-FORCE (HOUSEWIFE)
EMP	EMP=1 IF EMPLOYED
WRATE	HOURLY WAGE RATE (\$)
LRATE	Log of WRATE = LOG(WRATE+1)
ED	YEARS OF EDUCATION
URB	URB=1 IF RESIDENT IN SMSA
MINOR	MINOR=1 IF BLACK AND HISPANIC
AGE	YEARS OF AGE
TENURE	MONTHS UNDER THE CURRENT EMPLOYER
EXP	NUMBER OF YEARS WORKED SINCE AGE 18
REGS	REGS=1 IF LIVES IN THE SOUTH OF U.S.
OCCW	OCCW=1 IF WHITE COLOR
OCCB	OCCB=1 IF BLUE COLOR
INDUMG	INDUMG=1 IF IN THE MANUFACTURING INDUSTRY
INDUMN	INDUMN=1 IF NOT IN MANUFACTURING SECTOR
UNION	UNION=1 IF UNION MEMBER
UNEMPR	% UNEMPLOYMENT RATE IN THE RESIDENT'S COUNTY, 1980
OFINC	OTHER FAMILY MEMBER'S INCOME IN 1980 (\$)
LOFINC	LOG OF (OFINC+1)
KIDS	NUMBER OF CHILDREN 17 YEARS OF AGE
HWORK	HOURS OF HOMEWORK PER WEEK
USPELL	UNEMPLOYED WEEKS FOR EMPLOYED WIFE
SEARCH	WEEKS LOOKING FOR JOB IN 1980
WUNE80	ACTUAL UNEMPLOYED HOURS
KIDS5	NUMBER OF CHILDREN 5 YEARS OF AGE

## MAXIMUM SCORE ESTIMATION

MSE is designed for relatively small problems. The initial limits are 15 parameters and 2,000 observations.

### Example 1: (MSE1.LIM)

```
namelist ; x = one,ed,urb,minor,lofinc $
```

```
MSCORE ; LHS = emp; RHS = X; NBT = 100; MAXIT=1000 $
```

### Output

```
+-----+
| Maximum Score Estimates of Linear Quantile                               |
| Regression Model from Binary Response Data                             |
| Quantile          .500      Number of Parameters =      5           |
| Observations input = 1962      Maximum Iterations   = 1000        |
| End Game Iterations = 100      Bootstrap Estimates   = 20         |
| Check Ties?          No                                           |
| Save bootstraps?     No                                           |
| Start values from MSCORE (normalized)                                 |
| Normal exit after 100 iterations.                                     |
| Score functions:      Naive   At theta(0)      Maximum             |
|           Raw         .05912   .05912         .17533                    |
|           Normalized  .52956   .52956         .58767                    |
| Estimated MSEs from 20 bootstrap samples                             |
| (Nonconvergence in 0 cases)                                         |
| Angular deviation (radians) of bootstraps from estimate             |
| Mean square = .881535      Mean absolute = .760578                 |
| Standard errors below are based on bootstrap mean squared          |
| deviations. These and the t-ratios are only approximations.        |
+-----+
+-----+-----+-----+-----+-----+-----+
|Variable | Coefficient | Standard Error |b/St.Er.|P[|Z|>z] | Mean of X|
+-----+-----+-----+-----+-----+-----+
Constant - .7094313341      .80360150      - .883   .3773
ED        .3659168155      .12119087      3.019   .0025  12.205403
URB       .4329113018      .15678261      2.761   .0058   .68654434
MINOR    - .1325863919      .29330609      - .452   .6512   .27166157
LOFINC   - .3972665601      .16375789      -2.426   .0153   9.9052275
```

Frequencies of actual & predicted outcomes  
 Predicted outcome is the sign of  $x(i) \cdot \theta$ .

Actual	Predicted		Total
	0	1	
0	558	481	1039
1	328	595	923
Total	886	1076	1962

**Example 2: (MSE2.LIM)**

/\*

This program is for Monte Carlo Simulation:

Model:  $ys = b1 + b2 \cdot x2 + e$ ,  $b1 = b2 = 1/\text{SQR}(2)$

Compare the finite-sample biases

in estimates  $b2$  by MSE(MSCORE) and Probit.

\*/

? Define Sample Size

CALC ; SS = 100 \$

SAMPLE ; 1 - SS \$

? Define # of simulations

CALC ; SN = 10 \$

? VALUE FOR B2

CALC ; TB2 = 1/SQR(2) \$

? INITIAL VALUE FOR BIAS BY MSE, PROBIT AND LOGIT

CALC ; BIASMB2 = 0; BIASPB2 = 0 \$

```
? BEGIN THE PROCEDURE
```

```
PROCEDURE
```

```
CREATE      ; X2 = RNN(1,1) ; E = RNN(0,1) $  
CREATE      ; YS = (1/SQR(2)) + (1/SQR(2))*X2 + E $  
CREATE      ; Y = YS>0      $
```

```
NAMELIST    ; X = ONE,X2 $
```

```
? MSE
```

```
MSCORE      ; LHS=Y ; RHS=X $  
CALC        ; BIASMB2 = BIASMB2 + (B(2,1)-TB2) $
```

```
? PROBIT
```

```
PROBIT      ; LHS=Y ; RHS=X $  
CALC        ; BIASPB2 = BIASPB2 + (B(2,1)-TB2) $
```

```
ENDPROCEDURE
```

```
EXECUTE ; SILENT ; I = 1, SN $
```

```
CALC ; LIST  
      ; BIASM = BIASMB2/SN  
      ; BIASP = BIASPB2/SN $
```

[EXERCISE] Run the program with  $SN = 100$ . Which estimator has smaller bias? Changing  $SS = 50, 100$  and  $1000$ , see how the biases of MSE and Probit estimates change.

## ORDERED PROBIT

**Program for reading ORD\_DATA.DB: (ORD\_READ.LIM )**

```

READ ; NVAR=3 ; NOBS=500
      ; FILE = ORD_DATA.DB; FORMAT=(6G13.6)
      ; NAMES = X1,X2,Y $
  
```

**Program for Ordered Probit: (ORD\_PROB.LIM)**

```

NAMELIST ; X = ONE,X1,X2 $
ORDERED ; LHS=Y ; RHS=X ; MARGIN ; PAR $
  
```

### Output:

```

+-----+
| Ordered Probit Model
| Maximum Likelihood Estimates
| Dependent variable           Y
| Weighting variable           ONE
| Number of observations       500
| Iterations completed         13
| Log likelihood function      -62.40438
| Restricted log likelihood    -512.2856
| Chi-squared                  899.7625
| Degrees of freedom           2
| Significance level           .0000000
|   Cell frequencies for outcomes
|   Y Count Freq  Y Count Freq  Y Count Freq
|   0   197 .394  1   35 .070  2   19 .038
|   3   249 .498
+-----+
  
```

```

+-----+-----+-----+-----+-----+
| Variable | Coefficient | Standard Error | b/St.Er. | P[|Z|>z] | Mean of X |
+-----+-----+-----+-----+-----+
|           | Index function for probability
| Constant | 1.910662552 | .41836551      | 4.567    | .0000    |
| X1       | 2.070909800 | .32510834      | 6.370    | .0000    | .91768402
| X2       | .5310649242 | .96543109E-01 | 5.501    | .0000    | .76713340
|           | Threshold parameters for index
| Mu( 1)   | 3.319234065 | .66037247      | 5.026    | .0000    |
| Mu( 2)   | 4.917539009 | .90157315      | 5.454    | .0000    |
+-----+-----+-----+-----+-----+
  
```

```

+-----+-----+-----+-----+-----+
| Marginal Effects for OrdProbt
+-----+-----+-----+-----+-----+
| Variable | Y=0      | Y=1      | Y=2      | Y=3      |
+-----+-----+-----+-----+-----+
| ONE     | -.0001   | -.5086   | -.0883   | .5970    |
| X1      | -.0001   | -.5513   | -.0957   | .6471    |
| X2      | .0000    | -.1414   | -.0245   | .1659    |
+-----+-----+-----+-----+-----+
  
```

Frequencies of actual & predicted outcomes  
 Predicted outcome has maximum probability.

Actual	Predicted				Total
	0	1	2	3	
0	194	3	0	0	197
1	4	25	6	0	35
2	0	5	8	6	19
3	0	0	4	245	249
Total	198	33	18	251	500

**Program for Ordered Probit with HET: (ORD\_PROB.LIM)**

```

NAMELIST ; X = ONE,X1,X2 $
ORDERED ; LHS=Y ; RHS=X ; HET ; RH2 = X1,x2 ; MARGIN ; PAR $

```

**Output:**

```

+-----+
| Ordered Probit Model
| Maximum Likelihood Estimates
| Dependent variable                Y
| Weighting variable                ONE
| Number of observations            500
| Iterations completed              21
| Log likelihood function           -61.69838
| Restricted log likelihood          -512.2856
| Chi-squared                       901.1745
| Degrees of freedom                4
| Significance level                 .0000000
| Cell frequencies for outcomes
| Y Count Freq Y Count Freq Y Count Freq
| 0   197 .394 1   35 .070 2   19 .038
| 3   249 .498
| Terms 4 to 5 are for variance.
+-----+

```

```

+-----+-----+-----+-----+-----+-----+
| Variable | Coefficient | Standard Error | b/St.Er. | P[|Z|>z] | Mean of X |
+-----+-----+-----+-----+-----+-----+
| Index function for probability
| Constant | 1.952765793 | .50647697 | 3.856 | .0001 |
| X1        | 2.202009071 | .42735794 | 5.153 | .0000 | .91768402
| X2        | .5724646749 | .13028472 | 4.394 | .0000 | .76713340
| Variance function
| X1        | -.3920695036E-01 | .15416593 | -.254 | .7993 | .91768402
| X2        | .2509306915E-01 | .47567677E-01 | .528 | .5978 | .76713340
| Threshold parameters for index
| Mu( 1)   | 3.507495686 | .81328128 | 4.313 | .0000 |
| Mu( 2)   | 5.161587990 | 1.1134873 | 4.636 | .0000 |
+-----+-----+-----+-----+-----+-----+

```

```

+-----+-----+-----+-----+-----+
| Marginal Effects for OrdProbt
+-----+-----+-----+-----+-----+
| Variable | Y=0 | Y=1 | Y=2 | Y=3 |
+-----+-----+-----+-----+-----+
| ONE      | .0000 | -.5186 | -.0741 | .5928 |
| X1       | .0000 | -.5848 | -.0836 | .6684 |
| X2       | .0000 | -.1520 | -.0217 | .1738 |
| X1       | .0001 | .4693 | -.9134 | .4439 |
| X2       | .0002 | .5292 | -1.0300 | .5006 |
+-----+-----+-----+-----+-----+

```

Frequencies of actual & predicted outcomes  
 Predicted outcome has maximum probability.

Actual	Predicted				Total
	0	1	2	3	
0	194	3	0	0	197
1	4	25	6	0	35
2	0	5	8	6	19
3	0	0	4	245	249
Total	198	33	18	251	500

[EXERCISE]

- 1) Use ORD\_DATA.DB. Test for the existence of HET by Wald, LR and LM.
- 2) Make a program which computes the marginal effects of X1 on Pr(y=1) at the sample means of X1 and X2.

**MULTINOMIAL LOGIT**

**Example:** (MW\_MLM.LIM)

```
? Creating variable for occupation
? OCC = 0, if service; = 1, if white; = 2, if blue.
```

```
CREATE ; OCC = OCCW + 2*OCCB $
```

```
? Choose employed only
```

```
REJECT; EMP = 0 $
```

```
? Do MLM
```

```
? Coefficients for OCC = 0 are set to zeros.
```

```
NAMELIST; X = ONE,ED,URB,MINOR,LOFINC $
LOGIT ; LHS = OCC ; RHS = X ; MARGIN $
```

```
? MLM with restriction b_1 = b_2
```

```
CALC ; K = COL(X) $
LOGIT ; LHS = OCC ; RHS = X
; RST = K_B,K_B $
```

```
SAMPLE ; ALL $
```

**Output:**

```

+-----+
| Multinomial Logit Model
| Maximum Likelihood Estimates
| Dependent variable           OCC
| Weighting variable           ONE
| Number of observations       923
| Iterations completed         7
| Log likelihood function      -671.8235
| Restricted log likelihood     -841.1677
| Chi-squared                  338.6885
| Degrees of freedom           8
| Significance level            .0000000
+-----+

```

Variable	Coefficient	Standard Error	b/St.Er.	P[ Z >z]	Mean of X
Characteristics in numerator of Prob[Y = 1]					
Constant	-7.718311837	1.7357637	-4.447	.0000	
ED	.6675239548	.70670487E-01	9.446	.0000	12.457205
URB	.2777434765	.21712192	1.279	.2008	.71614301
MINOR	-.9495632405	.20731454	-4.580	.0000	.28494041
LOFINC	.7928185795E-01	.15593235	.508	.6111	9.8432227
Characteristics in numerator of Prob[Y = 2]					
Constant	4.661300540	1.7791433	2.620	.0088	
ED	-.1317677880	.58362277E-01	-2.258	.0240	12.457205
URB	-.5636828799	.23791127	-2.369	.0178	.71614301
MINOR	-.4166512440	.23969726	-1.738	.0822	.28494041
LOFINC	-.2989224821	.17310528	-1.727	.0842	9.8432227

```

+-----+
| Partial derivatives of probabilities with
| respect to the vector of characteristics.
| They are computed at the means of the Xs.
| Observations used for means are All Obs.
| A full set is given for the entire set of
| outcomes, OCC = 0 to OCC = 2.
| Probabilities at the mean vector are
| 0= .188 1= .692 2= .120
+-----+

```

Variable	Coefficient	Standard Error	b/St.Er.	P[ Z >z]	Mean of X
Marginal effects on Prob[Y = 0]					
Constant	.8970085202	.25111906	3.572	.0004	
ED	-.8369597078E-01	.95455832E-02	-8.768	.0000	12.457205
URB	-.2335294950E-01	.31386949E-01	-.744	.4569	.71614301
MINOR	.1326770374	.29953771E-01	4.429	.0000	.28494041
LOFINC	-.3554697100E-02	.22870034E-01	-.155	.8765	9.8432227
Marginal effects on Prob[Y = 1]					
Constant	-2.032158327	.31222880	-6.509	.0000	
ED	.1531730201	.13409235E-01	11.423	.0000	12.457205
URB	.1060726545	.39922710E-01	2.657	.0079	.71614301
MINOR	-.1676263157	.39497910E-01	-4.244	.0000	.28494041
LOFINC	.4176258361E-01	.26774137E-01	1.560	.1188	9.8432227
Marginal effects on Prob[Y = 2]					
Constant	1.135149806	.16732040	6.784	.0000	
ED	-.6947704936E-01	.71452164E-02	-9.724	.0000	12.457205
URB	-.8271970500E-01	.22400671E-01	-3.693	.0002	.71614301
MINOR	.3494927833E-01	.23443352E-01	1.491	.1360	.28494041
LOFINC	-.3820788651E-01	.14389635E-01	-2.655	.0079	9.8432227

Frequencies of actual & predicted outcomes  
 Predicted outcome has maximum probability.

Actual	Predicted			Total
	0	1	2	
0	33	131	24	188
1	14	557	12	583
2	27	85	40	152
Total	74	773	76	923

Normal exit from iterations. Exit status=0.

Multinomial Logit Model	
Maximum Likelihood Estimates	
Dependent variable	OCC
Weighting variable	ONE
Number of observations	923
Iterations completed	5
Log likelihood function	-930.7384

Variable	Coefficient	Standard Error	b/St.Er.	P[ Z >z]	Mean of X
Characteristics in numerator of Prob[Y = 1]					
Constant	-2.246577102	1.4168164	-1.586	.1128	
ED	.2945460414	.44213261E-01	6.662	.0000	12.457205
URB	-.6619168682E-01	.19853983	-.333	.7388	.71614301
MINOR	-.7559059112	.18812078	-4.018	.0001	.28494041
LOFINC	-.3209143823E-01	.14166104	-.227	.8208	9.8432227
Characteristics in numerator of Prob[Y = 2]					
Constant	-2.246577102	1.4168164	-1.586	.1128	
ED	.2945460414	.44213261E-01	6.662	.0000	12.457205
URB	-.6619168682E-01	.19853983	-.333	.7388	.71614301
MINOR	-.7559059112	.18812078	-4.018	.0001	.28494041
LOFINC	-.3209143823E-01	.14166104	-.227	.8208	9.8432227

Frequencies of actual & predicted outcomes  
 Predicted outcome has maximum probability.

Actual	Predicted			Total
	0	1	2	
0	50	138	0	188
1	16	567	0	583
2	48	104	0	152
Total	114	809	0	923

[Exercise] Use MWPSID82.DB. Do MLM for:

LHS = OCC

RHS = ONE, ED,URB,MINOR,LOFINC,AGE,EXP,KIDS5.

- 1) Test  $H_0$ : Each women is equally likely to be a white- or blue-collar worker. Use LM, LR and Wald.
- 2) Estimate the probability of being a white collar at sample means of regressors.

## BIVARIATE PROBIT MODEL

Consider the following model: (same as in the class)

$$Y1^* = \beta_{11} + \beta_{12}X12 + \beta_{13}X13$$
$$Y2^* = \beta_{21} + \beta_{22}X22 + \beta_{23}X23$$

$$Y1 = 1 \text{ IF } Y1^* \geq 0; Y1 = 0, \text{ OTHERWISE}$$
$$Y2 = 1 \text{ IF } Y2^* \geq 0; Y2 = 0, \text{ OTHERWISE}$$

### Full Observability:

```
NAMELIST ; X1 = ONE, X12, X13
          ; X2 = ONE, X22, X23 $

? CREATE INITIAL VALUES FOR BIVARIATE PROBIT

PROBIT   ; LHS = Y1 ; RHS = X1 $
MATRIX   ; BT = B $
PROBIT   ; LHS = Y2 ; RHS = X2 $
MATRIX   ; BP = B $

? MLE FOR FULL OBSERVABILITY MODEL

BIVA ; LHS = Y1, Y2 ; RH1 = X1 ; RH2 = X2
      ; START = BT, BP, 0
      ; TLF = 0.00001 ; TLB = 0.00001 ; TLG = 0.00001
      ; MAXIT = 1000
      ; PAR $
```

**COMMENT:** The first part of the program creates initial values for the bivariate Probit. In BIVA command, you have to specify the initial values using Subcommand, "START = ...". If you omit "PAR", LIMDEP store the estimates of  $\beta$ 's and  $\rho$  Separately.  $\rho$  is stored as a scalar in the name of "RHO". This is not good when you want to test some hypotheses using all estimates. If you use "PAR", all estimates of  $\beta$  are stored in the matrix, B, and covariance matrix of all the estimated parameters in VARB. It is better idea to use "PAR". Whether you use "PAR" or not,  $\rho$  is stored as a scalar.

### Censored Probit

Y2 is observed only if Y1 = 1.

```
NAMELIST ; X1 = ONE, X12, X13
          ; X2 = ONE, X22, X23 $
```

? CREATE INITIAL VALUES FOR BIVARIATE PROBIT

```
PROBIT ; LHS = Y1 ; RHS = X1 $
MATRIX ; BT = B $
REJECT ; Y1 # 1 $
PROBIT ; LHS = Y2 ; RHS = X2 $
MATRIX ; BP = B $
SAMPLE ; ALL $
```

? CENSORED PROBIT MODEL

```
BIVA ; LHS = Y2,Y1 ; RH1 = X2 ; RH2 = X1
; START = BP,BT,0
; SELECTION
; TLF = 0.00001 ; TLB = 0.00001 ; TLG = 0.00001
; MAXIT = 1000
; PAR $
```

**COMMENT:** The initial values for 's are created by separate Probits. These Probit estimates are efficient if  $\sigma$  is equal to zero. For the censored Probit, You just include "SELECTION" in the bivariate Probit command. You also note that LIMDEP reports the estimates in order of  $\sigma_2$ ,  $\sigma_1$  and  $\sigma$ . In the case of full observability, Poirier, Abowd-Farber, LIMDEP Reports  $\sigma_1$ ,  $\sigma_2$  and  $\sigma$ .

### Poirier probit

Only  $Y = Y1*Y2$  are observed.

```
NAMELIST ; X1 = ONE,X12,X13
; X2 = ONE,X22,X23 $
PROBIT ; LHS = Y ; RH1 = X1 ; RH2 = X2
; TLF = 0.00001 ; TLB = 0.00001 ; TLG = 0.00001
; MAXIT = 1000
; PAR $
```

**Comment:** You don't have to give initial values.

### Abowed-Farber Probit

```
NAMELIST ; X1 = ONE,X12,X13
; X2 = ONE,X22,X23 $
PROBIT ; LHS = Y ; RH1 = X1 ; RH2 = X2 ; SELECTION
; TLF = 0.00001 ; TLB = 0.00001 ; TLG = 0.00001
; MAXIT = 1000 $
```

### SURE (Seemingly Uncorrelated Regression Model)

Suppose you observe  $Y1^*$ (=YY1) AND  $Y2^*$  (=YY2). Then, you can estimate 's by SURE method. FOR this, use following commands:

```

NAMELIST ; X1 = ONE, X12, X13
          ; X2 = ONE, X22, X23 $
SURE     ; LHS = YY1, YY2
          ; EQ1 = X1
          ; EQ2 = X2 $

```

### Information on BIV.DB

Data in BIV.DB is generated by following:

```

SAMPLE ; 1-500 $
CALC   ; SS=SQR(3)/2 $
CREATE ; V1=RNN(0,1)
        ; V2=RNN(0,SS)
        ; V3=RNN(0,2)
        ; E1=V1 ; E2=V1/2+V2 ; E3=V3+V1
        ; X1=RNN(-1,2) ; X2=RNN(0,2) ; X3=RNN(3,2)
        ; YY1=1+2*X1+E1 ; YY2=2+3*X2+E2 ; YY3=3+4*X3+E3$

```

? CREATE DUMMY VARIABLES FOR FULL OBSERVABILITY

```

CREATE ; FY1=YY1>0; FY2=YY2>0 $

```

? CREATE DUMMY VARIABLES FOR CENSORED PROBIT

```

CREATE ; CY1=YY1>0 $
CREATE ; IF (FY1=1 & FY2=1) CY2=1; (ELSE) CY2=0$

```

? CREATE DUMMY VARIABLES FOR POIRIER'S PROBIT

```

CREATE ; Y = FY1*FY2 $

```

? CREATE Y3

```

CREATE ; Y3 = Y>0*YY3 $

```

As you see from the program, YY1 and YY2 amount to  $y_{1i}^*$  and  $y_{2i}^*$  in the class; FY1 and FY2 amount to  $y_{1i}$  and  $y_{2i}$  in full observability model; CY1 and CY2 amount to dummies in censored probit model; and  $Y = FY1 \times FY2$ . You can ignore the existence of YY3. Using BIV1.DB, You can check how important the quality of given information is. In order to read the data set, use the following commands (BIV\_READ.LIM):

```

READ ; NVAR=12 ; NOBS=500
      ; FILE = BIV.DB
      ; NAMES = X1,X2,X3,YY1,YY2,YY3,FY1,FY2,CY1,CY2,Y,Y3 $

```

[EXERCISE] Use BIV.DB. The model is given:

$$y_{1i}^* = \beta_{11} + \beta_{12}x_{1i} + \epsilon_{1i}$$

$$y_{2i}^* = \beta_{21} + \beta_{22}x_{2i} + \epsilon_{2i}$$

Do SURE, full observability, censored, Poirier, and Abowd-Farber MLE. Which method generates the best results in terms of efficiency? (You may fail to get a converged MLE result for Poirier's probit. Read your output carefully. If LIMDEP fails to locate MLE, it will say "abnormal exit from iterations.")

[EXERCISE] Use MWPSID82.DB. Consider the joint estimation of labor-force participation and employment decisions. For the labor-force participation, the explanatory variables are:

ONE,ED,MINOR,URB,REGS,AGE,EXP,KIDS5,OFINC,UNEMPR.

For the employment decision, the explanatory variables are the same except that AGE is excluded. Estimate the model by the censored probit. Using your estimates, estimate  $\Pr(y_{1i}^* > 0 \text{ and } y_{2i}^* > 0)$  at means of regressors, and compute its standard error.

### TOBIT

The model is given:  $y_i^* = x_i + \varepsilon_i$ ;  $\varepsilon_i \text{ iid } N(0, \sigma^2)$ .

#### Basic Command

(1)  $y_i = \max(0, y_i^*)$ :

TOBIT; LHS = Y ; RHS = ONE,X1,X2,... ; MARGIN ; PAR \$

(2)  $y_i = \min(0, y_i^*)$ :

TOBIT; LHS = Y ; RHS = ONE,X1,X2,... ; UPPER ; MARGIN ; PAR \$

(3)  $y_i = \min(L_i, y_i^*)$

TOBIT; LHS = Y ; RHS = ONE,X1,X2,... ; UPPER ; LIMIT = L ; MARGIN ; PAR \$

NOTE: For truncation model, replace TOBIT by TRUNC.

NOTE: MARGIN computes  $E(y_i | x_i) / x_i$ .

NOTE: The estimate of  $\sigma$  is stored in S. Can retrieve it using the CALC command.

[EXERCISE] Use MWPSID82.DB. Consider the housework supply of employed married women:

$$HWORK_i = X_i + \varepsilon_i$$

where  $X_i$  includes ONE, ED, URB, AGE, UNEMPR, OFINC, EXP, OCCW, OCCB, TENURE, WRATE. Estimate this model by Tobit. (Some women reported zero hours on homework.)

### SIMPLE SELECTION MODEL

Consider the model:

$$y_{1i} = x_{1i} \beta_1 + \epsilon_{1i}; y_{2i}^* = x_{2i} \beta_2 + \epsilon_{2i}$$

$$y_{2i} = 1 \text{ if } y_{2i}^* > 0; 0 \text{ otherwise.}$$

$$y_{1i} \text{ are observed only if } y_{2i}=1.$$

The model can be estimated by following commands:

```
PROBIT; LHS = Y2 ; RHS = list for x2i ; HOLD (IMR = LAM) $
SELECT; LHS = Y1 ; RHS = list for x1i $
```

This program returns result for the two-stage estimation. B contains  $\beta_1$  and  $\beta_2$  where  $\beta_2 = \beta_1$ ; VARB contains the corrected covariance matrix. LIMDEP also calculates  $\text{Cov}(\beta_1, \beta_2)$  and store it in the name of RHO.

If you want to do MLE, then, use:

```
SELECT; LHS = Y1 ; RHS = list for x1i ; MLE $
```

[EXERCISE] Consider the market wage equation of married women. The model is given:

$$\text{LRATE}_i = X_{1i} \beta_1 + \epsilon_{1i}$$

$$\text{EMP}_i^* = X_{2i} \beta_2 + \epsilon_{2i},$$

where  $\text{EMP}_i^*$  denotes the latent variable which represents the  $i$ 'th woman's willingness to work. We assume that the woman can get a job immediately if she wants.  $W_i$  is observed only if  $\text{EMP}_i^* > 0$ . Both of  $X_{1i}$  and  $X_{2i}$  contain ONE, ED, URB, MINOR, AGE, REGS, UNEMPR, LOFINC, KIDS5, EXP. Estimate this model by two-stage and MLE. Can you find some efficiency gains by using MLE?

## MOVER/STAYER MODEL

$$y_{1i} = x_{1i} \beta_1 + u_{1i}, \quad u_{1i} \sim N(0, \sigma_1^2)$$

$$y_{0i} = x_{0i} \beta_0 + u_{0i}, \quad u_{0i} \sim N(0, \sigma_0^2)$$

$$I_i^* = z_i \gamma + u_i, \quad u_i \sim N(0, 1)$$

$$u_1 = \text{cov}(u, 1); \quad u_0 = \text{cov}(u, 0)$$

$$u_1 = \text{corr}(z, u) = \sigma_1^{-1} \gamma; \quad u_0 = \text{corr}(z, u).$$

$I_i = 1$  if  $I_i^* > 0$ ; 0, otherwise.

$y_{1i}$  are observed if  $I_i = 1$ .

$y_{0i}$  is observed if  $I_i = 0$ .

This model is estimated by following commands:

```

PROBIT      ; LHS = I ; RHS = Z ; HOLD $
SELECT      ; LHS = Y ; RHS = X1 $
MATRIX      ; BETA1 = BSR1 $ ? BSR1 = (b1,s1,rho_{u1})
SELECT      ; LHS = Y ; RHS = X0 ; LIMITS = 1 $
MATRIX      ; BETA0 = BSR0 $ ? BSR0 = (b0,s0,rho_{u2})
SELECT      ; LHS = Y ; RH1 = X1 ; RH2 = X0
              ; MLE ; ALL ; START = BETA1,BETA0
              ; TLF = 0.00001 ; TLB = 0.00001 ; TLG = 0.00001
              ; MAXIT = 1000 $

```

If you run the program, you get following results:

- (1) probit .
- (2) two-stage  $\beta_1, u_1$  (LIMDEP denotes this as coefficient of LAMBDA.)
- (3) two-stage  $\beta_0, u_0$  (LIMDEP denotes this as coefficient of LAMBDA.)
- (4) MLE results:  $\gamma, \beta_1, \beta_0, \sigma_1, \sigma_0, \rho_1, \rho_2$ .

[EXERCISE] Use MWPSID82.DB. Choose the employed only. You want to estimate union and nonunion wages by LEE's method. In this case, Y is LRATE; all of  $x_{1i}$ ,  $x_{2i}$ , and  $z_i$  contain ONE, ED, URB, MINOR, AGE, EXP, REGS, UNEMPR, OCCW, OCCB. Estimate the model by the MOVER/STAYER model. Test  $H_0$ : The wage equation is the same for both union and nonunion job. Use a LR test.

## MULTIPLE SELECTION MODEL

Consider the double selection model you learned in the class. Assume that  $y_{1i}$  and  $y_{2i}$  are observed. (Full Observability Model.) The model can be estimated by following commands (MW\_SEL1.LIM):

```
PROBIT      ; LHS = Y1 ; RHS = list for X1 $
MATRIX      ; BA = B $
PROBIT      ; LHS = Y2 ; RHS = list for X2 $
MATRIX      ; BB = B $
BIVA        ; LHS = Y1,Y2 ; RH1 = list for X1 ; RH2 = list for X2
              ; START = BA,BB,0 ; HOLD $
SELE        ; LHS = Y3; RHS = list for X3 $
```

**Note:** You can use full-observability, censored or Poirior probits

**Note:** I'm not sure this program is correct.

Here is a sample program which computes two-stage estimates using bivariate probit results: (MW\_SELE.LIM)

```
NAMELIST; X1=ONE, ED, MINOR, URB, REGS, AGE, EXP, KIDS5, OFINC, UNEMPR
          ; X2=ONE, ED, MINOR, URB, REGS, EXP, KIDS5, OFINC, UNEMPR $

REJECT   ; LF # 1 $
PROBIT   ; LHS = EMP
          ; RHS = X2 $
MATRIX   ; BP = B $
SAMPLE   ; ALL $
PROBIT   ; LHS = LF
          ; RHS = X1 $
MATRIX   ; BT = B $
BIVARIATE ; LHS = EMP, LF
          ; RH1 = X2; RH2 = X1
          ; START = BP,BT,0 ; TLF = 0.1E-15
          ; SELECTION
          ; PAR
          ; MAXIT = 1000 $

MATRIX   ; BIVCOV = VARB
          ; BIVB = B
          ; B1 = PART(B,10,19)
          ; B2 = PART(B,1,9) $
CALC     ; RHO = RHO $

? CHOOSE THE GROUP WITH OBSERVED Y3.
? YOU HAVE TO GIVE SELECTION VARIABLE.

REJECT; EMP # 1 $

? GENERATE SELECTIVITY REGRESSORS
? B1,B2 COME FROM BIVARIATE PROBIT.
```

```

? X1 IS FOR FIRST SELECTION RULE, AND X2 FOR SECOND.

CREATE; Z1 = B1'X1
      ; Z2 = B2'X2 $

NAMELIST; Z = Z1,Z2 $

CALC ; PII = PI $
CREATE; H1 = (Z2-RHOU*Z1)/SQR(1-RHOU^2)
      ; H2 = (Z1-RHOU*Z2)/SQR(1-RHOU^2)
      ; S1 = N01(Z1)*PHI(H1)/BVN(Z,RHOU)
      ; S2 = N01(Z2)*PHI(H2)/BVN(Z,RHOU)
      ; S3 = 1/(2*PII*SQR(1-RHOU^2))
           *EXP(-0.5*(Z1^2-2*RHOU*Z1*Z2+Z2^2)/(1-RHOU^2))
           /BVN(Z,RHOU) $

? DEFINE REGRESSORS IN Y3

NAMELIST; X = ONE, ED, MINOR, URB, REGS,
           AGE, EXP, UNEMPR $

? DEFINE # OF REGRESSORS IN Y3

CALC ; KX = COL(X) $

? DEFINE SELECTIVITY REGRESSORS

NAMELIST; SELX = X, S1, S2 $

? OLS REGRESSION WITH SELECTIVITY REGRESSORS

REGRESS; LHS = LRATE; RHS= SELX; RES = E $

MATRIX; NOLIST
      ; SELB = B $

? CALCULATING CORRECTED VARIANCE OF ERRORS IN EQ. 3
? DEFINE SIG13 AND SIG23. THEY ARE THE LAST TWO
? ENTRIES OF SELB.

CALC ; C1 = SELB(KX+1)
      ; C2 = SELB(KX+2) $

CREATE; SSSIG33 = C1*C1*(Z1*S1+S1^2+RHOU*S3)
           + C2*C2*(Z2*S2+S2^2+RHOU*S3)
           - 2*C1*C2*(S3-S1*S2)
      ; EE = E^2$

TYPE; CORRECTED VARIANCE OF ERROR IN THIRD EQUATION$

CALC ; LIST
      ; SIG33 = XBR(SSSIG33) + XBR(EE) $

CREATE; KK = SIG33-SSSIG33 $

```

```

MATRIX; SELMAT1 = SELX' [KK] SELX $
DELETE; SSSIG33, KK, EE, E$
? GENERATE THE CORRECT COVARIANCE MATRIX OF ERRORS
CALC ; FO = 1/SQR(1-RHOU^2) $
CREATE; WT1 = C1*(-Z1*S1-S1^2-RHOU*S3) + C2*(S3-S1*S2)
      ; WT2 = C1*(S3-S1*S2) + C2*(-Z2*S2-S2^2-RHOU*S3)
      ; WT3 = C1*(-FO*H2*S3-S1*S3) + C2*(-FO*H1*S3-S2*S3) $
MATRIX; SMAT21 = X1' [WT1] SELX
      ; SMAT22 = X2' [WT2] SELX
      ; SSMAT23 = SELX' [WT3] ONE
      ; SMAT23 = SSMAT23'
      ; SELMAT2 = [SMAT22 / SMAT21 / SMAT23] $
TYPE ; CORRECTED TWO-STAGE ESTIMATION RESULT FOT DOUBLE
SELECTIVITY$
MATRIX; SELMAT = SELMAT1 + SELMAT2'*BIVCOV*SELMAT2
      ; CORCOV = <SELX' SELX>*SELMAT*<SELX' SELX> $
MATRIX; LIST
      ; STAT (SELB, CORCOV) $
SAMPLE; ALL$
CLOSE

```

If you run this program correctly, you will get:

Variable	Coefficient	Standard Error	z=b/s.e.	P[ Z	z]
Mean of X					
SELB _ 1	0.49166	0.14487	3.394	0.00069	
SELB _ 2	0.74413E-01	0.69689E-02	10.678	0.00000	
:	:	:	:	:	
:	:	:	:	:	

#### [EXERCISE]

- 1) Explain line by line what the above program does.
- 2) Run the above program.
- 3) Estimate the same model using the SELE command. Compare the results with those from 2).
- 4) Test the hypothesis of no selection by LM statistic.

## PANEL DATA MODELS:

### Data Configuration

A panel data set is usually arranged in blocks of observations T for a given i. (Your data set may be arranged in blocks of observation N for a given t. In this case, see LIMDEP manual.) Before estimation, you have to give a number for each cross-sectional units and specify a period for each observation in i'th cross-sectional unit. For this, do following:

```
CREATE; IND = TRN(T,0) ; PER = TRN(-T,0) $
```

where T is the time periods in your data set. (T=1,2,3,...) IND is a variable which indicates a specific integer number for a cross-sectional unit, and PER is the variable which indicates periods. LIMDEP's panel data estimator requires a sequential, complete set of indices for the stratification. (Especially, IND is most needed.) Once you do this, you are ready.

### Basic Command for Static Model

The basic command for a static model is given:

```
REGRESS      ; LHS = dependent variable  
              ; RHS = list of regressors  
              ; STR = IND  
              ; FIXED ; PANEL ; OUTPUT = 4 $
```

The above command will generate within estimator assuming that the individual effects are fixed effects. **You should not include any time-invariant regressor.** Intercept term is regarded as a time-invariant regressor, and therefore, you should not include ONE either. If you want to estimate the model by GLS, replace ;FIXED by ;RANDOM. When you use random-effects model, you can also estimate the coefficients of time-invariant regressors. Therefore, you may include any regressors you want in the list of regressors. For GLS, **you again should not include ONE.** If you do, LIMDEP will fail to give GLS result. This is because LIMDEP automatically include intercept term for GLS estimation.

If you omit both ;FIXED and ;RANDOM, LIMDEP computes both within and GLS estimators. It also report Hausman test result. This may be a good choice only if your model does not contain any time-invariant regressor other than the overall intercept term. If your model includes time-invariant regressors, the estimation results should be questioned.

The subcommand, ;OUTPUT = 4, is not necessary. I advise you to use it, because it will send a lot of information to the output file.

## Outcomes from Estimation of Static Model

### For the Case of Fixed-Effects Model

LIMDEP estimates 4 different models:

- 1)  $y_{it} = \alpha + \epsilon_{it}$  (no regressor and no individual effects)
- 2)  $y_{it} = \alpha_i + \epsilon_{it}$  (individual effects but no regressors)
- 3)  $y_{it} = x_{it} + \alpha + \epsilon_{it}$  (regressors but no individual effects)
- 4)  $y_{it} = x_{it} + \alpha_i + \epsilon_{it}$  (fixed-effects model)

First, LIMDEP will report a table of means for individual observations. (If you have more than 20 individuals, LIMDEP will not show these results on the screen. But those results will be sent to the output file.) The first row of the table is the overall, full sample means, denoted by group '0'.

Second, LIMDEP reports the results for the model 3) above. Output consists of the standard results for OLS regression.

Third, LIMDEP reports results for the model 4), the within estimation results. The estimates of individual effects and standard errors will be listed in your output file.

Fourth, LIMDEP will report some LR and F statistics for the restrictions of:

- Model 1) vs. Model 2)
- Model 1) vs. Model 3)
- Model 1) vs. Model 4)
- Model 2) vs. Model 4)
- Model 3) vs. Model 4)

The first four statistics are not interesting. The last test statistic is somewhat interesting. If the statistic is small (accepting hypothesis), it implies that all the individual effects are the same. This means that you need only overall intercept term.) If the statistic is large, it means that individual effects differ across  $i$ .

Fifth, LIMDEP will store, in the name of SUMSQDEV, SSE (sum of squared residuals) from within estimation. You will need this to make programs for the IV estimation of Hausman-Taylor models. Therefore, DON'T FORGET THIS!!!

### For the Case of Random-Effects Model

First, LIMDEP will report estimates of  $\sigma^2(1/T) + \sigma^2$ ,  $\sigma^2$ ,  $\sigma^2$ , and  $\rho = \text{corr}(\alpha_i + \epsilon_{it}, \alpha_i + \epsilon_{is}) = \sigma^2 / (\sigma^2 + \sigma^2)$ .

Second, LIMDEP will report Breusch and Pagan's LM statistic for testing random-effects model against Model 3) above. Large value of the LM statistic argues in favor of random-effects model.

Third, LIMDEP will give you GLS estimates of coefficients of regressors.

### Information on PANEL.DB

You can read the data set by the following command: (PAN\_READ.LIM)

```
? THIS PROGRAM IS FOR READING PANEL.DB

READ ; NOBS= 2500 ; NVAR=33
      ; FILE=PANEL.DB
      ; FORMAT=(6G13.6)
      ; NAMES=  Y,X1,X2,X3,X4,Z2,Z3,Z4,
                YB,X1B,X2B,X3B,X4B,
                X11AM,X12AM,X13AM,X14AM,X15AM,
                X21AM,X22AM,X23AM,X24AM,X25AM,
                X31AM,X32AM,X33AM,X34AM,X35AM,
                X41AM,X42AM,X43AM,X44AM,X45AM  $
```

Y is the dependent variable; X1,X2,X3, X4 are time-varying regressors; Z2, Z3 and Z4 are time-invariant regressors; X1B, X2B, X3B, X4B and YB are repeated means of corresponding variables (they correspond to 1, 2, 3, 4 and in the class); and X11AM is a vector repeated observations of X1 for t =1 (others are similarly defined). There are 500 cross-sectional units with 5 periods. Therefore, there are in total 2500 observations. Before you start estimation, you have to create stratification variables as I explained above.

The following is my program for within, GLS, Hausman test, ALT1, ALT2 and ALT3 (PAN\_GLS.LIM):

```
CREATE; IND = TRN(5,0) ; PER = TRN(-5,0) $

? SPECIFY # OF OBS.
CALC ; NN = 500 ; TT = 5  $

? SPECIFY # OF TIME-VARYING VARIABLES (KK)
? SPECIFYING # OF TIME-INVARIANT VARIABLES

CALC ; KK = 4 ; GG = 4 $

? PROGRAMS FOR WITHIN ESTIMATION

CREATE ; WX1 = X1 - X1B
      ; WX2 = X2 - X2B
      ; WX3 = X3 - X3B
      ; WX4 = X4 - X4B
      ; WY = Y - YB  $

NAMELIST ; WX = WX1,WX2,WX3,WX4  $
```

```

TYPE      ; WITHIN ESTIMATION RESULTS      $
REGRESS   ; LHS = WY ; RHS = WX           $
CALC      ; LIST ; SIGMAE2 = SUMSQDEV/(NN*(TT-1)-KK)  $

MATRIX    ; WB = B
           ; WCOV = SIGMAE2*XPXI(WX)
           ; STAT(WB,WCOV)                 $

```

? PROGRAM FOR GLS MODEL

```

TYPE      ; BETWEEN ESTIMATION RESULTS $
REGRESS; LHS = YB ; RHS = X1B,X2B,X3B,X4B,ONE,Z2,Z3,Z4 $
CALC     ; LIST
           ; SIGMAA2 = SUMSQDEV/(NN-KK-GG)
           ; THET = SQR(SIGMAE2/SIGMAA2)
           ; THE = 1-THET $
SAMPLE   ; ALL $
CREATE   ; THEY = Y - THE*YB
           ; THEONE = THET
           ; THEX1 = X1 - THE*X1B
           ; THEX2 = X2 - THE*X2B
           ; THEX3 = X3 - THE*X3B
           ; THEX4 = X4 - THE*X4B
           ; THEZ2 = THET*Z2
           ; THEZ3 = THET*Z3
           ; THEZ4 = THET*Z4 $

```

```

NAMELIST; THEX=THEX1,THEX2,THEX3,THEX4,THEONE,THEZ2,THEZ3,THEZ4
$

```

```

REGRESS; LHS = THEY
           ; RHS = THEX
           ; RES = RESY $
TYPE    ; GLS RESULTS $
MATRIX  ; REB = B
           ; RECOV = SIGMAE2*XPXI(THEX)
           ; STAT(REB,RECOV) $

```

? HAUSMAN TEST RESULTS

```

TYPE      ; HAUSMAN TEST RESULTS $

MATRIX    ; REB13 = PART(REB,1,4) ; RECOV13 = PART(RECOV,1,4,1,4) $
MATRIX    ; DIFB = WB~REB13 $
MATRIX    ; INVCOV = WCOV~RECOV13 $
MATRIX    ; DIFV = SINVC(INVCOV)
           ; HTEST = DIFB'|DIFV|DIFB $
CALC     ; LIST

```

```

; HT = HTEST
; P_VAL = 1 - CHI(HT, KK) $

```

? ALTERNATIVES OF HAUSMAN TEST

```

NAMELIST ; TESTX1=WX1, WX2, WX3, WX4, ONE, Z2, Z3, Z4, X1B, X2B, X3B, X4B $
REGRESS ; LHS = RESY ; RHS = TESTX1
; KEEP = FRESY $

```

```

TYPE ; ALT1 TEST $
CALC ; LIST
; ALT1 = TT*NN*RSQRD
; P_VAL = 1 - CHI(ALT1, KK) $

```

```

TYPE ; ALT2 TEST $
CALC ; LIST
; ALT2 = DOT(FRESY, FRESY) / SIGMAE2
; HT = HT
; P_VAL = 1 - CHI(ALT2, KK) $

```

```

NAMELIST ; TESTX2 = WX, ONE, Z2, Z3, Z4,
; X11AM, X12AM, X13AM, X14AM, X15AM,
; X21AM, X22AM, X23AM, X24AM, X25AM,
; X31AM, X32AM, X33AM, X34AM, X35AM,
; X41AM, X42AM, X43AM, X44AM, X45AM $

```

```

TYPE ; ALT3 TEST $
CALC ; DD = TT*KK ;
REGRESS ; LHS = RESY ; RHS = TESTX2 $
CALC ; LIST
; ALT3 = TT*NN*RSQRD
; P_VAL = 1 - CHI(ALT3, DD) $

```

[EXERCISE] Use PANEL.DB.

- 1) Run the above program and report the estimation results.
- 2) Compare the estimation results from 1) and estimation results you can directly obtain using LIMDEP's panel data commands.
- 3) Assume that Z2, Z3 and Z4 are correlated with the individual effects while other regressors (including ONE) are not. Make a program for Hausman-Taylor estimation method, and report your results.
- 4) Test the Hausman-Taylor specification using Hausman test method. (Hint: Your result must be favorable for H-T specification.) Use GINV.
- 5) Assume the same things as 3). Make a program for AM estimation method, and report your results.
- 6) Test AM specification using Hausman test method.

## Probit for Panel Data

The basic command is:

```
PROBIT ; LHS = ... ; RHS = ... ; PDS = T $
```

For probit, the data must be balanced; T, the number of periods must be the same for each i. Data arrangement is identical to the regression model, with multiple records per i. But, here, data must be arranged in N contiguous blocks of exactly T observations.

## SOME USEFUL LIMDEP COMMANDS

### MATRIX OPERATION

#### Data Area

LIMDEP store your data in a form similar to Lotus worksheet file. You can read up to 200 variables, and the observations depending on the ram size of your computer.

#### Namelist

It is used to define data matrices. In a sense, it is akin to creating usual matrices.

```
NAMELIST ; X = ONE,ED,URB,MINOR $  
PROBIT ; LHS = EMP ; RHS = X $
```

#### Sample Selection

When you use subsamples,

```
SAMPLE ; 1-100, 201-300 $  
PROBIT ; LHS = EMP ; RHS = X $
```

If you want to restore all observations,

```
SAMPLE ; ALL $
```

## Reject

You use this command if you want to eliminate some observations.

```
REJECT ; LF # 1 $ or REJECT ; LF = 0 $
```

Then, you can eliminate observations for housewives. If you want to restore all the observations,

```
SAMPLE ; ALL $
```

## Placing matrix results in scalar

1) A IS 1 x 1 MATRIX.

```
CALC ; AA = A $
```

Then, A is stored as a scalar in the name of A.

2) A is 4 x 4, and wish to use the (2,1) entry as a scalar

```
MATRIX ; AA = A(2,1) $  
CALC ; AAA = AA $
```

IMPORTANT: Do not use the same name in both CALC and MATRIX.

## Matrix Algebra

A. Matrix Algebra

- 1)  $A|B = AB$
- 2)  $A \sim B = A - B$
- 3)  $A \& B = A + B$
- 4)  $A' = \text{TRANSPOSE OF } A$
- 5)  $\text{SINV}(A) = \text{INVERSE OF } A$ , WHERE A IS SYMMETRIC PD.
- 6)  $\text{GINV}(A) = \text{INVERSE OF } A$ , WHERE A IS ANY SQUARE MATRIX.

IMPORTANT: I strongly recommend you to use SINV for symmetric and pd matrices. During an estimation procedure, you often create symmetric pd matrices, or your matrix outcomes are usually symmetric pd. If SINV does not work, it implies that you made some mistakes in the program. So, you can indirectly check your program using SINV.

- 7)  $\text{NVSM}(A,B) = \text{INVERSE OF } (A + B)$   
 $\text{NVSM}(A,-B) = \text{INVERSE OF } (A - B)$

- 8) INIT(p,q,r) = p x q MATRIX WHOSE ENTRIES ARE ALL r.
- 9) STAT(B,VARB) = TABLE SHOWING STATISTICAL RESULTS.

**B. FOR DATA MATRICES (ASSUME X AND Z ARE DEFINED BY NAMELIST.)**

- 1) XPXI(X) = INVERSE OF X'X = SUM of  $x_i'x_i$ .
- 2) XDOT(X,ONE) = SUM OF  $x_i'$
- 3) XDOT(X,ONE,U) = SUM OF  $u_i x_i'$  WHERE U IS A VARIABLE
- 4) XDOT(X,ONE,Y) = SUM OF  $x_i y_i$  WHERE Y IS A VARIABLE
- 5) XDOT(X) = X'X = sum of  $x_i x_i$
- 6) XDOT(X,U) = SUM OF  $u_i x_i' x_i$ .
- 7) XDOT(X,Z,U) = SUM OF  $u_i x_i' z_i$ .
- 8) ASSUME B IS A VECTOR.  
CREATE; XX = DOT(X,B) \$

This command creates a new variable XX.

**(EXAMPLE)**

```

NAMELIST ; X = ONE, ED, URB, MINOR $
REGRESS ; LHS = LRATE ; RHS = X $
MATRIX ; OLSB = B $
CREATE ; FLRATE = DOT(X,OLSB) $

```

Here, FLRATE is the fitted value of LRATE.

**Scalar Multiplication**

- 1) 2\*IDEN(2) = 2I<sub>2</sub>
- 2) 1/2\*IDEN(2) = I<sub>2</sub>/2

**Using Calculator Commands in Matrix Commands**

```

CALC ; PP = 1-2*PHI(1.96) $
MATRIX ; PP*XDOT(X)

```

**Partitioned Matrices**

1) ~~~~~C~=[C1,~C2]~~~~ ~~~ C~=[C1`,~C2]

2) ~~~~~C~ = ~[C1~/~ C2]~~~~ ~~~ C~==LEFT \[ MATRIX { C1 # C2 } RIGHT \]

3) ~~~~~C~=[C11`,~C12~/~C21`,C22]~~~~ C~==LEFT \[ MATRIX { C11 & C12 # C21 & C22 } RIGHT \]

## Extracting Part of a Matrix

- 1) A is a vector. You want to create a matrix with 2-10 entries of A. Then, `AA = PART(A,2,10)`.
- 2) A is a matrix. You want to create a matrix with 2-5 rows and 3-7 columns of A. Then, `AA = PART(A,2,5,3,7)`.

## Editing a Matrix

A is a matrix. You want to replace the (2,4)th entry by 3. Then,

```
MATRIX ; A(2,4) = 3 $
```

FOR MORE DETAILS, SEE THE HANDOUT

## CREATING VARIABLES

### Creating Dummy Variables

(EXAMPLE 1) Assume X,Y,Z are variables:

```
CREATE ; P = Z > 0 ; ZZ = Z = 1 ; A = X > 0 * PHI(Y) $
```

This command creates 3 dummy variables:

- 1) `P = 1 IF Z > 0, AND 0 IF Z <= 0`
- 2) `ZZ = 1 IF Z = 1, AND 0, OTHERWISE.`
- 3) `A = PHI(Y) IF X > 0, AND 0 IF X <= 0.`

(EXAMPLE 2)

```
CREATE ; IF (AGE >= 56) AGE56 = 1  
; IF ( 46 <= AGE & AGE <= 55) AGE46 = 1  
; IF ( 31 <= AGE & AGE <= 45) AGE31 = 1  
; IF ( 23 <= AGE & AGE <= 30) AGE23 = 1  
; IF ( AGE <= 22 ) AGE19 = 1 $
```

## Creating Variables

(EXAMPLE) Assume C and D are defined as a scalar (by CALC command).

```
CREATE      ; X12 = X1*X2 ; X23 = X2/X3 ; X11 = 1-C*X1
            ; X33 = (C/D)*X1 $
```

## Creating Variable Using a Vector

(EXAMPLE 1) Assume that X is defined by namelist.

```
NAMELIST   ; X = ONE,X1,X2,X3 $
REGRESS    ; LHS = Y ; RHS = X $
MATRIX     ; OLSB = B          $
CREATE     ; YFIT = DOT(X,OLSB) $
```

This program creates  $\hat{y}_i = x_i$ . Don't use CREATE; YFIT = X\*OLSB.

(EXAMPLE 2)

```
NAMELIST; X = ONE,X1,X2,X3 $
PROBIT  ; LHS = Y ; RHS = X $
MATRIX  ; PROBITB = B $
CREATE  ; SELVAR = N01(DOT(X,PROBITB))/PHI(DOT(X,PROBITB)) $
```

This program creates selectivity regressor for the two-stage estimation of Heckman's simple selection model:  $\hat{y}_i = (x_i) / (x_i)$ .

## Functions for CREATE

See Handout of transformation.

### CREATING STANDARD BIVARIATE NORMAL CDF

Suppose you want to create the variable:  $z_i = F(x_{1i}, x_{2i}, \rho)$  where F is cdf for standard bivariate normal. Assume that  $\rho$  is defined by CALC command in the name of RO. (Do not use the name "RHO". This name is reserved for LIMDEP. See the Handout by Dr. Kim, p.1.) Then,

```
NAMELIST; ZZ = X1,X2 $
CREATE  ; Z = BVN(ZZ,RO) $
```

You may replace RO by any number you wish.