

GAUSS CORNER

[1] Some Tips for Gauss

(1) Procedure (Defining functions)

[Basic Structure]

```
proc f(a,b,c) ; @a,b,c (input; scalar, vector or matrix)@  
  local v,u,x ; @declare local variables @  
  :  
  retp(v+u+x) ; @output @  
endp ;
```

- All of the variables defined in proc are local.
- Global variables can be used.

[Example 1]

```
proc f(b) ;  
  retp(1+b+b^2) ;  
endp ;
```

```
c = f(1); @ c = 3 @  
d = f(2); @ d = 7 @
```

[Example 2] Multiple Output

```
proc(2) = f(b) ;  
  retp(1+b,1+2*b^2) ;  
endp ;
```

```
{a,c} = f(1); @a = 2, c = 3.@
```

(2) Minimization

[Basic Structure]

```
library optmum;
#include optmum.ext;
optset;

proc f(b) ; @b = parameter vector @
    :    @ f(b) = function to be minimized @
    retp(...);
endp    ;

b0 = {1,2,...,0}; @ initial value of b @

__title = AGMM@ ; @ Writing title for output @
__opttol = 0.00001 ; @Controlling tolerance rate @
__opstmth = Abfgs,half@; @algorithm @
__output = 0; @ Control output files @

{b, func, grad, retcode} = optprt(optmum(&f,b0)) ;

@ b = the value of b minimizing f(b)@
@ retcode = 0 (normal convergence) @
@ retcode ≠ 0 (bad news)      @
```

(3) Gosub

```
      :  
Gosub weight ;  
      :  
      :  
end;  
weight:  
      :  
return ;
```

- weight: a label for a subroutine.

(4) Computing gradient:

```
proc young(b) ; @ b must be a vector @  
local minsu, chulsoo ... ;  
      :  
retp(...) ;  
endp ;  
  
grad = gradp(&young,b) ;
```

- For example, $\text{young}(b) = g_T(\theta)$ in GMM and $\text{grad} = G_T(\theta)$.

(5) Matrix Operations:

- $\text{rndns}(k,t,dd)$: k = rows; t = cols; dd = seed number
 - outcome: $k \times t$ matrix of iid $N(0,1)$ random numbers.
 - For uniform, use rndus .

- Let A and B be conformable matrices.
 - $A*B$ = product of A and B.
 - A' = transpose of A
 - $A*B'$ = product of A' and B.
 - $A[:,1]$ = the first column of A.
 - $A[1,:]$ = the first row of A.
 - $A[1,2]$ = the (1,2)th element of A.
 - $A[1:5,:]$ = matrix of the 1st, 2nd, 3rd, 4th and 5th rows of A.
 - $\text{invpd}(A)$ = inverse of a positive definite matrix A.
 - $\text{diag}(A)$ = $n \times 1$ vector of diagonal elements of a $n \times n$ matrix A.
 - If $A = [a_{ij}]$, $\text{sqrt}(A) = [\sqrt{a_{ij}}]$; $A^2 = [a_{ij}^2]$.
 - $A|B$ = merging A and B vertically; $A \sim B$ = merging A and B horizontally.
 - $\text{sumc}(A)$ = $n \times 1$ vector of sums of individual columns for a $m \times n$ matrix A.

$$\text{Example: } A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}; \text{sumc}(A) = \begin{pmatrix} 9 \\ 12 \end{pmatrix}.$$

- $\text{meanc}(A)$ = $n \times 1$ vector of means of individual columns for a $m \times n$ matrix A.

$$\text{Example: } A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}; \text{meanc}(A) = \begin{pmatrix} 3 \\ 4 \end{pmatrix}.$$

- $\text{stdc}(A)$ = $n \times 1$ vector of standard errors of individual columns for a $m \times n$ matrix A.
- $A = m \times n$, $B = m \times n$, $C = m \times 1$, $d = \text{scalar}$
 - $A./B = [a_{ij}/b_{ij}]$ (element by element operation)
 - $A./C = [a_{ij}/c_i]$ (element by element operation)
 - $d - A = [d - a_{ij}]$; $d*A = [da_{ij}]$; $A/d = [a_{ij}/d]$.

[2] Program for OLS

Program: ols.prg (Can download from the website for ECN 525)

```
/*
** OLS Program
*/

@ Data loading @

load data[100,5] = exer.txt;

@ Define # of observations, # of regressors, X and Y @

tt = rows(data); @ # of observations @
kk = 5; @ # of regressors @
y = data[:,1];
x2 = data[:,2];
x3 = data[:,3];
x4 = data[:,4];
x5 = data[:,5];
vny = {"y"}; @ name of the dependent variable @

@ Dependent variable @

yy = y ;
vny = {"y"};

@ Regressors @

xx = ones(tt,1)~x2~x3~x4~x5;
vnx = {"cons", "x2", "x3", "x4", "x5" } ;

@ Do not change below @
@ OLS using yy and xx @

b = invpd(xx'xx)*(xx'yy);
e = yy - xx*b ;

s2 = (e'e)/(tt-kk);
v = s2*invpd(xx'xx);

econ = b~sqrt(diag(v))~(b./sqrt(diag(v)));
econ = vnx~econ;

se = sqrt(diag(v));
```

```

sst = yy'yy - tt*meanc(yy)^2;
sse = e'e;

r2 = 1 - sse/sst;

@ Printing out OLS results @

output file = ols.out reset;

let mask[1,4] = 0 1 1 1;
let fmt[4,3] =
    "_.*s" 8 8
    ".*lf" 10 4
    ".*lf" 10 4
    ".*lf" 10 4;

format /rd 10,4 ;
"" ;
"OLS Regression Result" ;
"-----" ;
" dependent variable: " $vny ;
"" ;
" R-Squares          " r2 ;
"" ;
"variable   coeff.  std. err.  t-st " ;
yyprin = printfm(econ,mask,fmt);
"" ;

output off ;

```

Outcome in old.out

OLS Regression Result

```

-----
dependent variable:      y

R-Squares                0.8960

variable   coeff.   std. err.   t-st
cons      -0.0009   0.2225     -0.0042
x2         0.9617   0.2040      4.7145
x3         1.7759   0.2659      6.6790
x4         3.0003   0.1903     15.7669
x5         3.8823   0.2035     19.0790

```

[3] Program for Monte Carlo Experiments

Program: olsmonte.prg (Can download from the ECN 525 website)

```
/*
** Monte Carlo Program
*/

@ Load Data @

load data[100,5] = exer.txt ;

@ Data generation under Strong Ideal Conditions @

/*
** The regressors are common to individual data sets.
** The errors are different across different data sets
** That is, regressors are nonstochastic but the errors are
*/

seed = 1;
tt = 100; @ # of observations @
kk = 5; @ # of betas @
iter = 5000; @ # of sets of different data @
xx = ones(tt,1)~data[.,2:5]; @ Regressors are fixed @
tb = {0,1,2,3,4} ; @  $y = x(2)*1 + x(3)*2 + x(4)*3 + x(5)*4 + e$  @

storb = zeros(iter,1);
storse = zeros(iter,1);

i = 1; do while i <= iter;

@ Generating y @
yy = xx*tb + 2*rndns(tt,1,seed);

@ OLS using yy and xx @

b = invpd(xx'xx)*(xx'yy);
e = yy - xx*b ;

s2 = (e'e)/(tt-kk);
v = s2*invpd(xx'xx);

se = sqrt(diag(v));

storb[i,1] = b[2,1];
```

```

storse[i,1] = se[2,1];

i = i + 1; endo;

@ Reporting Monte Carlo results @

output file = olsmonte.out reset;

format /rd 12,3;

"Monte Carlo results";
"-----";
"Mean of OLS b(2)           =" meanc(storb);
"s.e. of OLS b(2)          =" stdc(storb);
"mean of estimated s.e. of OLS b(2) =" meanc(storse) ;

library pgraph;
graphset;
{a1,a2,a3}=hist(storb,50);
output off ;

```

Outcome in olsmonte.out

```

Monte Carlo results
-----
Mean of OLS b(2)           =    0.998
s.e. of OLS b(2)          =    0.184
mean of estimated s.e. of OLS b(2) = 0.185

```

[4] Programs for Basic Panel Data Models

Program name: pan_gls.prg

```
new ;

@ You must locate MGIV.COL in the directory you execute this program @

    #include mgiv.col ;

@ Open an output file @

    output file = pan_gls.out reset ;

@ Formatting output file @

    format /rd 12,4 ;

@ Provide # of observations and # of variables @

    nobs = 336 ;
    nvar = 13 ;

@ Read Data @

    load dat[nobs,nvar] = auto_1.txt ;
    @ 48 states (N = 48), 1982 - 1988 (T = 7)@

@ Define Variables @

    id    = dat[.,1] ; @ ID for States @
    year  = dat[.,2] ; @ year @
    spircons = dat[.,3] ; @ Spirits consumption @
    unrate = dat[.,4] ; @ Unemployment rate @
    perinc = dat[.,5] ; @ Personal Income @
    emppop = dat[.,6] ; @ Employment/Population Ration @
    beertax = dat[.,7] ; @ Tax on Case of Beer @
    mllda  = dat[.,8] ; @ Minimum Legal Drinking Age @
    vmiles = dat[.,9] ; @ Ave. mile per driver @
    jaild  = dat[.,10] ; @ Mandatory Jail Sentence = 1 @
    comserd = dat[.,11] ; @ Mandotory Jail Sentence @
    allmort = dat[.,12] ; @ # of Vehicle Fatalities @
    mrall  = dat[.,13] ; @ Vehicle Fatality Rate (VFR) @

@ Creating Time dummy variables @

    v = {1982.5, 1983.5, 1984.5, 1985.5, 1986.5, 1987.5 } ;
    dyr = dummy(year,v);

@ Define N and T @

    t = 7 ;
    n = rows(dat)/t ;

@ Define Dep. Var., Time-varying Reg. and Time-invariant Reg. @
```

```

yy = mrrall*10000 ; @ dependent var. @
xx = beertax~mlda~jailed~comserd~ln(perinc)~dyr[.,2:7]; @ time-varying indep. @
zz = ones(rows(yy),1); @ time-invariant indep. @

vny = {"VFR"};
vnx = {"beertax","mlda","jailed","comserd","unrate","lpinc",
      "yr83", "yr84", "yr85", "yr86", "yr87", "yr88"};
vnz = {"cons"};

@ Exclude year dummy vars. from xx to make pvxx full column @
@ Use xxt for ALT1 test @

xxt = beertax~mlda~jailed~comserd~unrate~ln(perinc) ;

/*
** From Here, Do Not Change
*/

clear dat ;

let mask[1,4] = 0 1 1 1 ;
let fmt[4,3] =
"-* *s" 8 8
"* *lf" 10 4
"* *lf" 10 4
"* *lf" 10 4;

@ Define k and g @

k = cols(xx) ;
kt = cols(xxt) ;
g = cols(zz) ;

@ Creating AM and Mean Variables @

pvxxt = pvmat1(xxt,n,t) ;
pvxx = pvmat1(xx,n,t) ;
pvyy = pvmat1(yy,n,t) ;

@ creating Deviation-From-Mean Variables @

qvxx = qvmat(xx,n,t) ;
qvyy = qvmat(yy,n,t) ;

@ OLS estimation @

ow = xx~zz;
od = invpd(ow'ow)*(ow'yy);
oe = yy - ow*od;
os2 = (oe'oe)/(rows(ow)-cols(ow));
ov = os2*invpd(ow'ow);
ose = sqrt(diag(ov));
orsq = 1-(oe'oe)/(yy'yy-rows(yy)*meanc(yy)^2);

"OLS Estimation Result" ;
"-----" ;

```

```

" dependent variable: " $vny ;
"";
"variable  coeff. std. err. t-st ";
yyprin = printfm((vnx|vnz)~od~ose~(od./ose),mask,fmt);
"";
"R-Square =" orsq;
"";

@  Within Estimation  @

wb = invpd(qvxx'qvxx)*(qvxx'qvyy) ;

we = qvyy - qvxx*wb ;
ssq = (we'we)/(n*t-n-k) ;
wc = ssq*inv(qvxx'qvxx) ;
ws = sqrt(diag(wc)) ;
wrsq = 1 - (we'we)/(yy'yy-rows(yy)*meanc(yy)^2);

"Within Estimation Result" ;
"-----" ;
" dependent variable: " $vny ;
"";
"variable  coeff. std. err. t-st ";
yyprin = printfm(vnx~wb~ws~(wb./ws),mask,fmt);
"";
"R-Square =" wrsq;
"";

@  GLS estimation  @

bx = xx~zz ;
bd = invpd(bx'bx)*(bx'yy) ;
bee = pvyy - pvmat1(bx,n,t)*bd ;
ssqbb = (bee'bee)/(n-k-g) ;
theta = sqrt(ssq/ssqbb) ;
ssqaa = (ssqbb-ssq)/t ;

yystar = yy - (1-theta)*pvyy ;
xxstar = xx - (1-theta)*pvxx ;
zzstar = theta*zz ;

regstar = xxstar~zzstar ;

gd = invpd(regstar'regstar)*(regstar'yystar) ;
gc = ssq*invpd(regstar'regstar) ;
gs = sqrt(diag(gc)) ;
gee = qvyy - qvxx*gd[1:cols(xx)] ;
grsq = 1 - gee'gee/(yy'yy-rows(yy)*meanc(yy)^2);

"GLS Estimation Result" ;
"-----" ;
" dependent variable: " $vny ;
"";
"variable  coeff. std. err. t-st ";
yyprin = printfm((vnx|vnz)~gd~gs~(gd./gs),mask,fmt);
"";
"R-Square =" grsq;

```

```

"";

" THETA = " theta ;
" SIGE2 = " ssq ;
" SIGA2 = " ssqaa ;
" S.E.R.= " sqrt(ssq);
"";

@ CREATING GLS RESIDUALS @

gee = yystar - regstar*gd ;

@ H TEST FOR W VS. GLS @

gb = gd[1:k] ;
gbc = gc[1:k,1:k] ;
ht = (wb-gb)'pinv(wc-gbc)*(wb-gb) ;
df = rank(wc-gbc) ;

"Hausman Test, p-val, df =" ht cdfchic(ht,df) df ;

@ J TEST FOR W VS. GLS USING PX ONLY @

axx = qvxx~pvxxt~zz ;
abb = invpd(axx'axx)*(axx'gee) ;
ru2 = (axx*abb)'(axx*abb)/(gee'gee) ;
alt1 = t*n*ru2 ;
df = cols(pvxxt) ;

"ALT1 Test, p-val, df =" alt1 cdfchic(alt1,df) df ;

```

OUTPUT OFF

Output: pan_gls.out

OLS Estimation Result

```

-----
dependent variable:          VFR

variable      coeff.   std. err.   t-st
beertax       0.1112   0.0624     1.7832
mlda          -0.0297  0.0317    -0.9367
jailed        0.1959   0.0723     2.7085
comserd       0.1460   0.0813     1.7951
unrate       -0.0227  0.0143    -1.5852
lpinc        -1.9018  0.2265    -8.3957
yr83         -0.0900  0.0959    -0.9389
yr84         -0.0648  0.0996    -0.6504
yr85         -0.0783  0.1006    -0.7782
yr86          0.0632  0.1022     0.6185
yr87          0.1032  0.1067     0.9671
yr88          0.1404  0.1107     1.2679
cons         20.7805  2.3157     8.9738

```

R-Square = 0.3482

Within Estimation Result

```

-----
dependent variable:          VFR

variable    coeff.  std. err.  t-st
beertax    -0.4768   0.1657   -2.8773
mlda       -0.0019   0.0178   -0.1053
jailed      0.0147   0.1201    0.1222
comserd     0.0345   0.1377    0.2503
unrate     -0.0629   0.0111   -5.6629
lpinc       1.7964   0.3625    4.9560
yr83       -0.0972   0.0322   -3.0232
yr84       -0.2812   0.0371   -7.5740
yr85       -0.3745   0.0389   -9.6220
yr86       -0.3376   0.0422   -8.0090
yr87       -0.4347   0.0481   -9.0369
yr88       -0.5213   0.0537   -9.7103

```

R-Square = 0.9390

GLS Estimation Result

```

-----
dependent variable:          VFR

variable    coeff.  std. err.  t-st
beertax     0.0052   0.1140    0.0454
mlda         0.0005   0.0175    0.0307
jailed       0.1429   0.0992    1.4404
comserd     -0.0704   0.1145   -0.6149
unrate      -0.0780   0.0105   -7.4267
lpinc        0.4189   0.3071    1.3641
yr83        -0.0918   0.0321   -2.8580
yr84        -0.2577   0.0368   -6.9957
yr85        -0.3237   0.0383   -8.4470
yr86        -0.2533   0.0409   -6.1996
yr87        -0.3193   0.0460   -6.9357
yr88        -0.3794   0.0510   -7.4451
cons        -1.1846   2.9655   -0.3995

```

R-Square = 0.9328

```

THETA = 0.1213
SIGE2 = 0.0241
SIGA2 = 0.2304
S.E.R.= 0.1551

```

```

Hausman Test, p-val, df = 76.4475 0.0000 6.0000
ALT1 Test, p-val, df = 66.3981 0.0000 6.0000

```

Program name: pan_gls2.prg

```
new ;

@ Locate MGIV.COL in the directory you execute this program @

#include mgiv.col ;

@ Open output file @

output file = pan_gls2.out reset ;

@ Format output file @

format /rd 12,4 ;

@ Provide # of observations and # of variables @

nobs = 336 ;
nvar = 13 ;

@ Read Data @

load dat[nobs,nvar] = auto_1.txt ;
@ 48 states (N = 48), 1982 - 1988 (T = 7)@

@ Define Variables @

id = dat[.,1] ; @ ID for States @
year = dat[.,2] ; @ year @
spircons = dat[.,3] ; @ Spirits consumption @
unrate = dat[.,4] ; @ Unemployment rate @
perinc = dat[.,5] ; @ Personal Income @
emppop = dat[.,6] ; @ Employment/Population Ratio @
beertax = dat[.,7] ; @ Tax on Case of Beer @
mlda = dat[.,8] ; @ Minimum Legal Drinking Age @
vmiles = dat[.,9] ; @ Ave. mile per driver @
jaild = dat[.,10] ; @ Mandatory Jail Sentence = 1 @
comserd = dat[.,11] ; @ Mandatory Jail Sentence @
allmort = dat[.,12] ; @ # of Vehicle Fatalities @
mrall = dat[.,13] ; @ Vehicle Fatality Rate (VFR) @

@ Creating Time dummy variables @

v = {1982.5, 1983.5, 1984.5, 1985.5, 1986.5, 1987.5} ;
dyr = dummy(year,v);

@ Define N and T @

t = 7 ;
n = rows(dat)/t ;

@ Define Dep. Var., Time-varying Reg. and Time-invariant Reg. @

yy = mrall*10000 ; @ dependent var. @
xx = beertax~mlda~jaild~comserd~unrate~ln(perinc)~dyr[.,2:7]; @ time-varying indep. @
```

```

zz = ones(rows(yy),1); @ time-invariant indep. @

vny = {"VFR"};
vnx = {"beertax","mlda","jailed","comserd","unrate","lpinc",
      "yr83", "yr84", "yr85", "yr86", "yr87", "yr88"};
vnz = {"cons"};

/*
** From Here, Do Not Change
*/

clear dat ;

@ Define k and g @

k = cols(xx) ;
g = cols(zz) ;

let mask[1,4] = 0 1 1 1 ;
let fmt[4,3] =
"-. *s" 8 8
"*. *|f" 10 4
"*. *|f" 10 4
"*. *|f" 10 4;

@ Within with HET-AUTO adjustment @

{wb,wcovh} = w_ha(xx,yy,n,t) ;
wsh = sqrt(diag(wcovh)) ;

"Within Estimation Results (HETERO/AUTO ADJUSTED)" ;
"-----" ;
" dependent variable: " $vny ;
"" ;
"variable   coeff. std. err. t-st " ;
yyprin = printfm(vnx~wb~wsh~(wb./wsh),mask,fmt);
"" ;

@ Kiefer's Estimation @

{kb,kcov,kcovh} = kiefer(xx,yy,n,t) ;
ks = sqrt(diag(kcov)) ;
ksh = sqrt(diag(kcovh)) ;

"Kiefer's Within Estimation Results" ;
"-----" ;
" dependent variable: " $vny ;
"" ;
"variable   coeff. std. err. t-st " ;
yyprin = printfm(vnx~kb~ks~(kb./ks),mask,fmt);
"" ;

"Kiefer's Within Estimation Results (HETERO ADJUSTED)" ;
"-----" ;
" dependent variable: " $vny ;
"" ;
"variable   coeff. std. err. t-st " ;

```

```
yyprin = printfm(vnx~kb~ksh~(kb./ksh),mask,fmt);
"";
```

@ RE-GLS Estimation @

```
{rb,rcov,rcovh} = regls(xx,yy,n,t) ;
rs = sqrt(diag(rcov)) ;
rsh = sqrt(diag(rcovh)) ;
```

```
"RE-GLS Estimation Results" ;
"-----" ;
" dependent variable: " $vny ;
"" ;
"variable  coeff. std. err. t-st " ;
yyprin = printfm(vnx~rb~rs~(rb./rs),mask,fmt);
"" ;
```

```
"RE-GLS Estimation Results (CROSS-SECTION HETERO ADJUSTED)" ;
"-----" ;
" dependent variable: " $vny ;
"" ;
"variable  coeff. std. err. t-st " ;
yyprin = printfm(vnx~rb~rsh~(rb./rsh),mask,fmt);
"" ;
```

output off

Output file: pan_gls2.prg

Within Estimation Results (HETERO/AUTO ADJUSTED)

```
-----
dependent variable:          VFR

variable  coeff.  std. err.  t-st
beertax  -0.4768   0.2949   -1.6167
mlda     -0.0019   0.0209   -0.0894
jailed   0.0147   0.0158    0.9292
comserd  0.0345   0.1285    0.2684
unrate   -0.0629   0.0127   -4.9657
lpinc    1.7964   0.6243    2.8775
```

Kiefer's Within Estimation Results

```
-----
dependent variable:          VFR

variable  coeff.  std. err.  t-st
beertax  -0.1833   0.1837   -0.9982
mlda     -0.0058   0.0175   -0.3343
jailed   -0.0026   0.0882   -0.0295
comserd  0.0420   0.1110    0.3784
unrate   -0.0518   0.0112   -4.6255
lpinc    2.0991   0.3932    5.3387
```

Kiefer's Within Estimation Results (HETERO ADJUSTED)

```

-----
dependent variable:          VFR

variable    coeff.  std. err.  t-st
beertax    -0.1833   0.2254   -0.8135
mlda       -0.0058   0.0157   -0.3720
jailed     -0.0026   0.0138   -0.1885
comserd     0.0420   0.0924    0.4545
unrate     -0.0518   0.0107   -4.8367
lpinc      2.0991   0.5934    3.5373

```

RE-GLS Estimation Results

```

-----
dependent variable:          VFR

variable    coeff.  std. err.  t-st
beertax     0.4601   0.1210    3.8032
mlda        -0.0112   0.0233   -0.4819
jailed      0.1532   0.0957    1.5998
comserd     -0.0521   0.1147   -0.4538
unrate      -0.0062   0.0126   -0.4970
lpinc       0.2217   0.0521    4.2559

```

RE-GLS Estimation Results (CROSS-SECTION HETERO ADJUSTED)

```

-----
dependent variable:          VFR

variable    coeff.  std. err.  t-st
beertax     0.4601   0.1028    4.4774
mlda        -0.0112   0.0174   -0.6464
jailed      0.1532   0.1249    1.2261
comserd     -0.0521   0.1346   -0.3868
unrate      -0.0062   0.0123   -0.5084
lpinc       0.2217   0.0430    5.1512

```