

1. The size of the gravitational force between any two spherically-symmetric masses in the Universe is given by $F_G = G \frac{m_A m_B}{r^2}$; r is the separation distance between the masses.
 - a. Star A is twice as massive as star B ; no other masses are nearby. No information about their motions is given. Make a FBD on each star, drawing the force arrows to scale.
 - b. Draw a labeled acceleration arrow below each star, once again to scale. Explain the selected length of your acceleration arrows.



2. The gravitational PE stored in a system of two spherically-symmetric masses, M and m , separated by a distance r , is most conveniently written as $U_G(r) = -G \frac{Mm}{r}$.
 - a. Find the expression that results from taking $-\frac{d}{dr}U_G(r)$. For M at the origin (a reasonable choice if we let $M \gg m$), what is the physical significance of your result?
 - b. Show that, given this choice of $U_G(r)$, if a projectile was fired from the surface of a planet of mass M and radius R with a launch speed of $\sqrt{2GM/R}$, then the planet-projectile system would have a total mechanical energy of zero! What would happen to such a projectile launched vertically from the surface of an airless world?
 - c. Consider a 100-kg projectile to be launched from the surface of an airless world having $M = 6.0 \times 10^{24}$ kg and $R = 6500$ km. Find the launch speed needed to create $K+U = 0$ (as in (b)), and calculate each of K and U at the instant of launch.
 - d. For the launch of part (c), what would be the system KE when the projectile has achieved an altitude equal to twice the radius of the planet (*i.e.* $r = 3R$)?