WiP Abstract: Conformance Testing as Falsification for Cyber-Physical Systems

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In a typical Model-Based Design (MBD) process for Cyber-Physical Systems, an initial 'simple' *Model* is successively refined and made more accurate and complex; then it is implemented on a real-time computational platform, and further modified to yield an *Implementation*. The goal is to produce a system that satisfies a formal specification Φ. This successive refinement raises the question of how "close" are the "simple" Model and the "complex" Implementation. Answering this question is important because it is not always possible to verify formally that the Implementation satisfies the specification Φ. Moreover, even if the Implementation satisfies Φ, it will have unspecified behavior which might exhibit bugs. By quantifying the 'closeness' between Model and Implementation, our level of confidence in the Implementation derives from our confidence in the Model, and the fact that the Model satisfies Φ.

Because formal analysis of non-deterministic models is rarely utilized and supported by industry tools, language inclusion can not be used to answer this question. Thus, an appropriate notion of closeness, or *conformance*, between Model and Implementation is required. *Conformance testing* is the process of establishing whether behaviors exhibited by Model and Implementation are conformant. Existing works apply only to certain classes of systems and rely on the full knowledge of the mathematical representations of Model and Implementation, often not available for industrial CPS.

In this work, we give a rigorous mathematical definition of conformance between two output trajectories $\mathbf{y}_M$ and $\mathbf{y}_I$ of the Model and Implementation, resp., when driven from the same initial conditions, with the same control input. We term this conformance notion $(T, J, (\tau, \varepsilon))$-closeness. Its distinctive feature is that it measures the difference between $\mathbf{y}_M$ and $\mathbf{y}_I$ in both space and time. Coarsely, two output trajectories are conformant with degree $(\tau, \varepsilon) \in \mathbb{R}^2_+$, over a hybrid time-horizon $(T, J) \in \mathbb{R}_+ \times \mathbb{N}$, if every $\mathbf{y}_M$-point has a $\mathbf{y}_I$-point ε-close to it within a window of width 2τ, and vice-versa. Several application-dependent notions of system similarity can be shown to be implied by $(T, J, (\tau, \varepsilon))$-closeness.

Using $(T, J, (\tau, \varepsilon))$-closeness, it is possible to perform the following MBD tasks in a rigorous manner:

◦ Define conformance between a Model and Implementation, which are said to be conformant with degree $(T, J, (\tau, \varepsilon))$ iff given the same initial conditions, and the same input signal, they produce trajectories that are $(T, J, (\tau, \varepsilon))$-close.

◦ Given a tuple (τ, ε), determine whether the Model and Implementation are conformant by performing a search over the initial conditions and input signal space for two trajectories that are not $(T, J, (\tau, \varepsilon))$-close. If such a pair is found, then the Implementation needs to be revised to conform the Model.

◦ Given T and J, determine a smallest pair (τ, ε) such that the two systems are $(T, J, (\tau, \varepsilon))$-close. Such a smallest value is termed the *degree of conformance* between the two systems.

We demonstrate the above tasks on an industrial automatic transmission, where the Model is in Simulink, and the Implementation is a high-fidelity engine model from Simuquest with a large number of black box components. Using our methods, we can reliably approximate the degree of conformance between the two systems.

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