

# **LINEAR AND ANGULAR KINEMATICS**

*Readings: McGinnis Chapters 2 and 6*

## **DISTANCE, DISPLACEMENT, SPEED, VELOCITY, AND ACCELERATION:**

### **How far?**

Describing change in linear or angular position

Distance (Scalar quantity)—Length of path traveled with no concern for direction (magnitude only)

Displacement (Vector quantity)—Difference between starting and finishing positions; independent of path followed (magnitude and direction)

Symbols: linear -  $\ell$ ,  $d$       angular -  $\phi$ ,  $\theta$

Examples - Linear distance and displacement

Describing race distances:

100 m Sprint       $\ell = 100 \text{ m}$

Indy 500 (auto race)       $\ell = 500 \text{ mi}$

4000 km Tour de France (bike race)

$$\ell = 4000 \text{ km}$$

Characterizing performance:

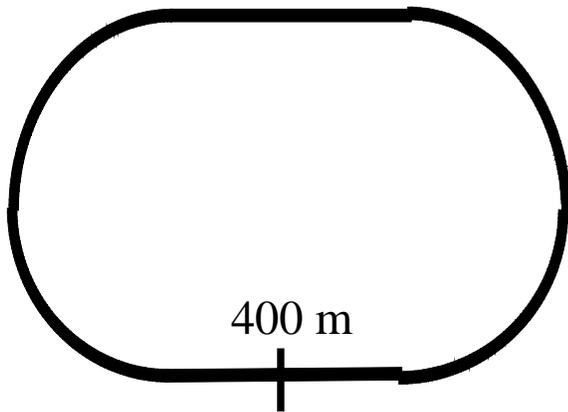
Shot put, Long jump, High jump

long jump of 8.89 m       $\ell = 8.89 \text{ m}$

Typical units of measurement: m, km, ft, mile

Distinguishing distance and displacement

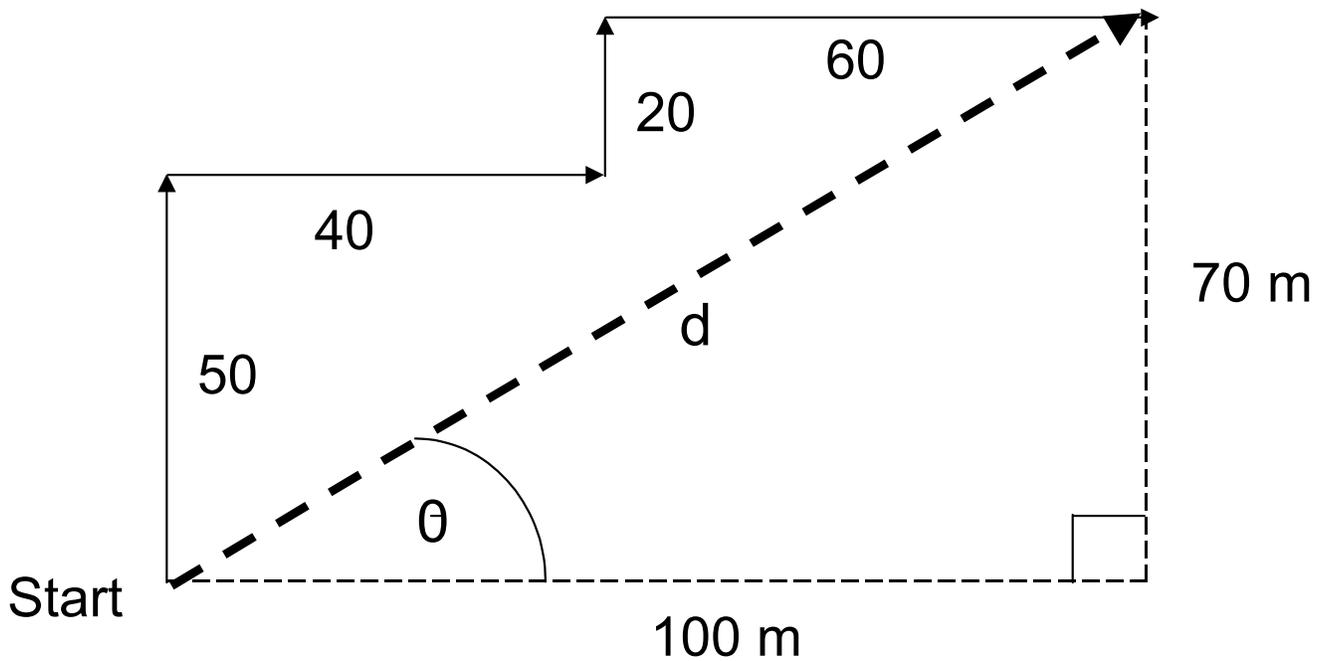
Example: 400 m run (one lap around track)



Distance?

Displacement?

Example: Walking north and east, then north and east again:



Overall distance traveled?  $\ell$

Displacement ("as the crow flies")?

Magnitude  $d$

Direction  $\theta$

## Examples - Angular distance and displacement.

Diving, gymnastics:

“triple somersault with a full twist”

3.0 revolutions about a transverse axis  
(somersaulting axis) combined with 1 rev  
about a longitudinal axis (twisting axis)

transverse axis  $\phi = \underline{\hspace{2cm}}$   $\theta = \underline{\hspace{2cm}}$

long. axis  $\phi = \underline{\hspace{2cm}}$   $\theta = \underline{\hspace{2cm}}$

Discus throw:

Body rotates through  $\underline{\hspace{2cm}}$  rotations prior to  
discus release.

$\phi = \underline{\hspace{2cm}}$  rev  $\theta = \underline{\hspace{2cm}}$  rev

Joint range of motion:

The elbow and knee have ROM's of  
approximately 150 degrees.

$\phi = \underline{\hspace{2cm}}$   $\theta = \underline{\hspace{2cm}}$

Typical units - 3 used commonly:

revolutions, radians, degrees

1 rev =  $2\pi$  rad (i.e., 6.28 rad) = 360 deg

1 rad = 57.3 deg

## How fast?

Describing rate of change of linear or angular position with respect to (wrt) time

Speed or Velocity: Rate at which a body moves from one position to another

Speed (scalar)

Velocity (vector)

Note: *There will be times when it is important to use velocity because of its vector characteristic.*

Linear:

Angular:

$$\bar{v} = \frac{d}{\Delta t}$$

$$\bar{\omega} = \frac{\theta}{\Delta t}$$

Examples of linear speed or velocity:

Tennis: 125 mph (55.9 m/s) serve

$$v = 125 \text{ mph} = 55.9 \text{ m/s}$$

Pitching: 90 mph (40.2 m/s) fastball

$$v = 90 \text{ mph} = 40.2 \text{ m/s}$$

Running:

Marathon (26.2 mi) - 2 hr 10 min  
(2.17 hr)

$$\bar{v} = 12.1 \text{ mph (5.4 m/s; 4:57 per mile)}$$

Sprinting - 100 m in 9.86 s

$$\bar{v} = 10.14 \text{ m/s} = 22.7 \text{ mph}$$

Football – “4.6” speed (40 yd in 4.6 s)

$$\bar{v} = 7.95 \text{ m/s} = 17.8 \text{ mph}$$

Typical units of measurement for  $v$ :

m/s, km/hr (kph), ft/s, mph

Examples of angular speed or velocity:

Auto engine speed - 3000 rpm

$$\omega = 3000 \text{ rpm}$$

CD ROM drive - 400 rpm

$$\omega = 400 \text{ rpm}$$

Cycling cadence - 90 rpm

$$\omega = 90 \text{ rpm}$$

Isokinetic dynamometer (Cybex and others) -

e.g., 60 deg/s

$$\omega = 60 \text{ deg/s}$$

Body segment  $\omega$ 's -

e.g., peak  $\omega$  of soccer player's knee...

2400 deg/s . 6.7 rev/s

Typical units of measurement for  $\omega$ :

rpm, deg/s, rad/s

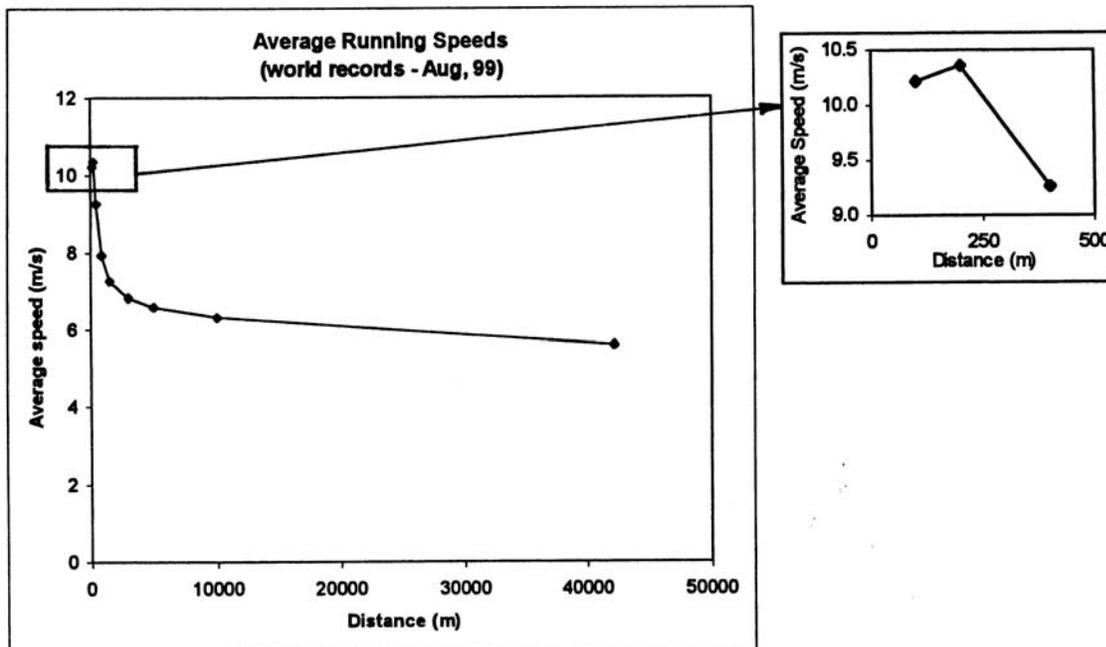
## Average vs. Instantaneous Velocities



Average speed per race distance:

100 m...marathon

Race that produces highest average speed?



Sometimes  $\bar{v}$  over relatively long  $t$  is not very informative - reflects need for a “kinematic profile” for more detailed information about performance

e.g., distance running - split times

e.g., sprinting - 1987 T&F World Champ.

Johnson vs. Lewis

9.83 s

9.93 s

$\Delta = 0.100$  s

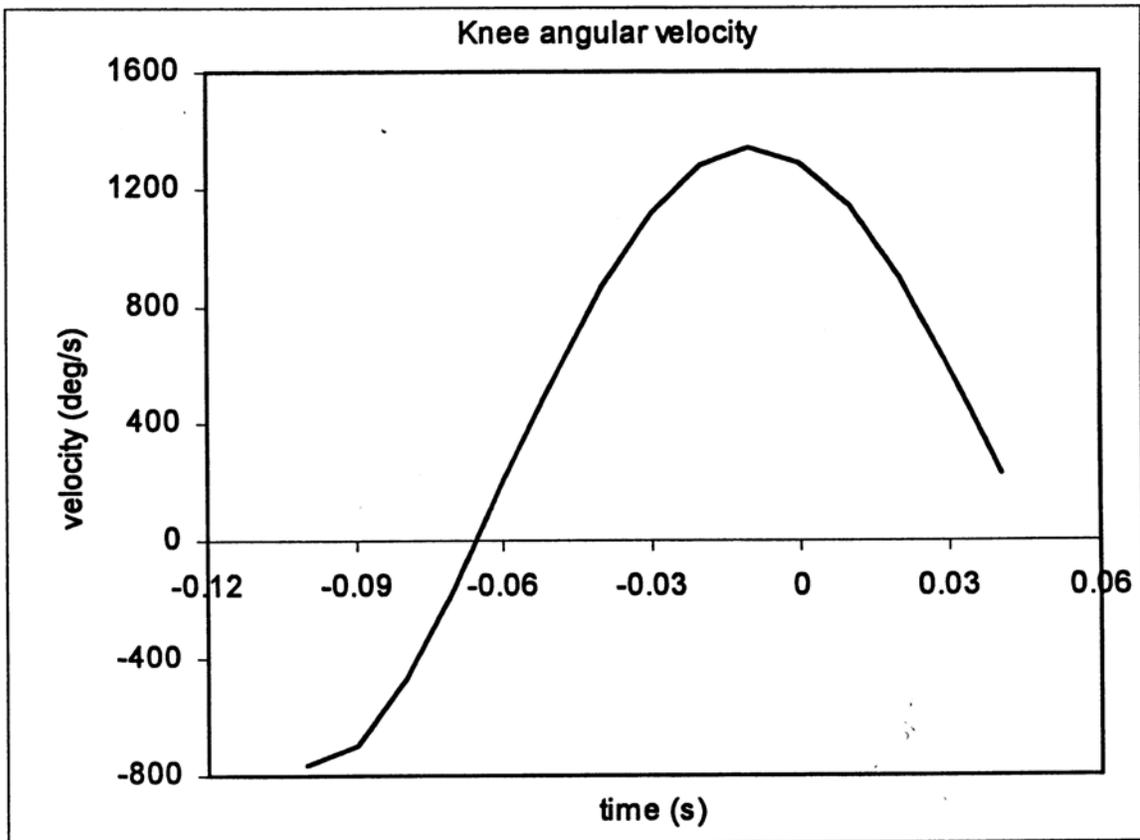
Where was race won or lost?

Reaction time:  $\Delta = 0.067$  s

After 10 m:  $\Delta = 0.100$  s

By decreasing  $t$  over which we examine velocity and other kinematic information, we approach *instantaneous* estimates of performance - gives more detail about performance.

e.g., during a soccer kick (next page):



## Acceleration

Describing the rate of change of linear or angular velocity wrt time

Vector only - no scalar equivalent

Linear:

Angular:

Typical units of measurement for acceleration:

Linear -  $\text{m/s}^2$ ,  $\text{ft/s}^2$

Angular -  $\text{deg/s}^2$ ,  $\text{rad/s}^2$

### Example - linear

An athlete described as being “quick” or having “good acceleration” - same as being fast?

No, acceleration describes a person’s ability to change speed or direction; doesn’t describe top speed.

### Example - angular

Throwing a baseball

Angular speed of shoulder internal rotation increases from zero to 1800  $\text{deg/s}$  in 26 ms just prior to release...

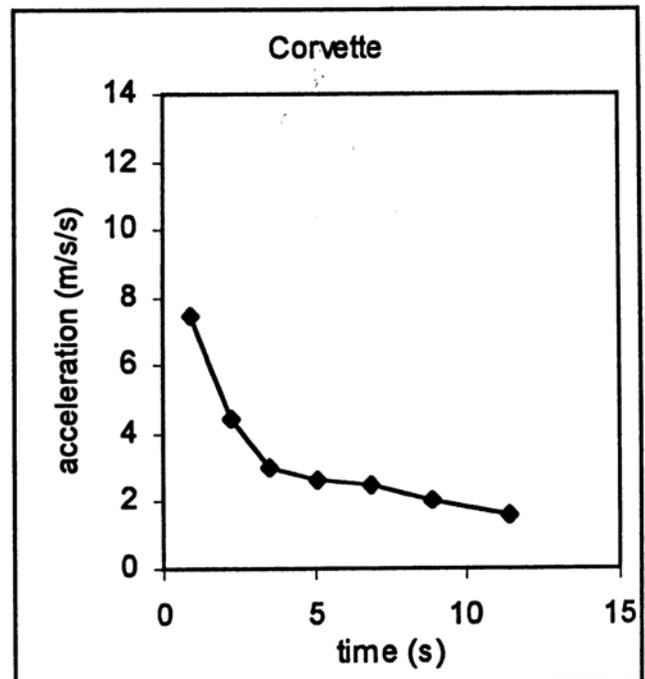
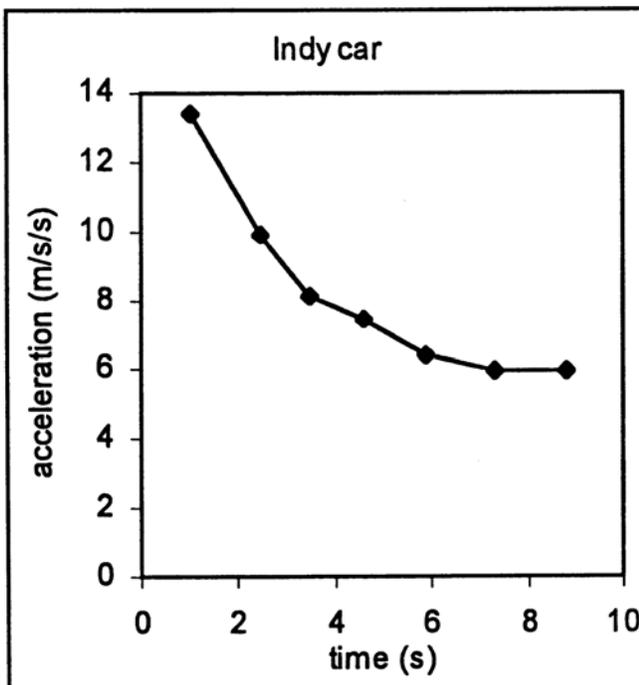


Ball velocity at release correlates strongly ( $r=.75$ ) with shoulder internal rotation speed at release (Sherwood, 1995).

## Example – linear:

### Auto accelerations - Indy car vs. Corvette

Indy car				Corvette			
$\Delta\text{mph}$	$\Delta\text{m/s}$	$\Delta t$ (s)	$\bar{a}$ ( $\text{m/s}^2$ )	$\Delta\text{mph}$	$\Delta\text{m/s}$	$\Delta t$ (s)	$\bar{a}$ ( $\text{m/s}^2$ )
0-60	0-26.8	2.0	13.42	0-30	0-13.4	1.8	7.45
60-80	26.8-35.8	0.9	9.94	30-40	13.4-17.9	1.0	4.47
80-100	35.8-44.7	1.1	8.13	40-50	17.9-22.4	1.5	2.98
100-120	44.7-53.7	1.2	7.45	50-60	22.4-26.8	1.7	2.63
120-140	53.7-62.6	1.4	6.39	60-70	26.8-31.3	1.8	2.48
140-160	62.6-71.6	1.5	5.96	70-80	31.3-35.8	2.2	2.03
160-180	71.6-80.5	1.5	5.96	80-90	35.8-40.3	2.8	1.60



\_\_\_\_\_ When is speed or velocity highest for Indy car?

\_\_\_\_\_ When is acceleration highest for Indy car?

\_\_\_\_\_ Is the speed or velocity of the Indy car changing approximately 6-8 seconds after the start?

### **Link between position, velocity, and acceleration:**

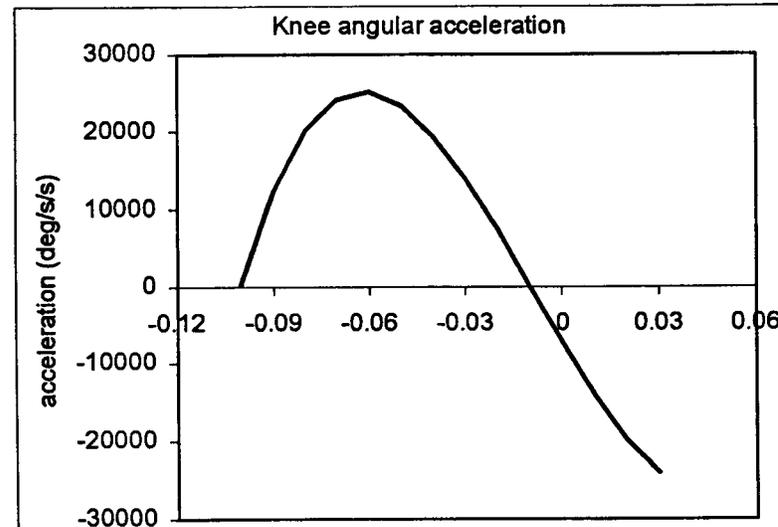
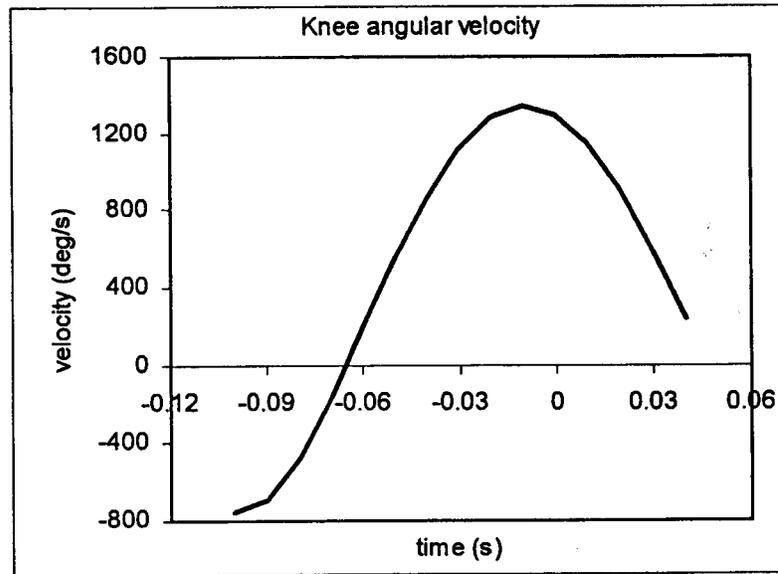
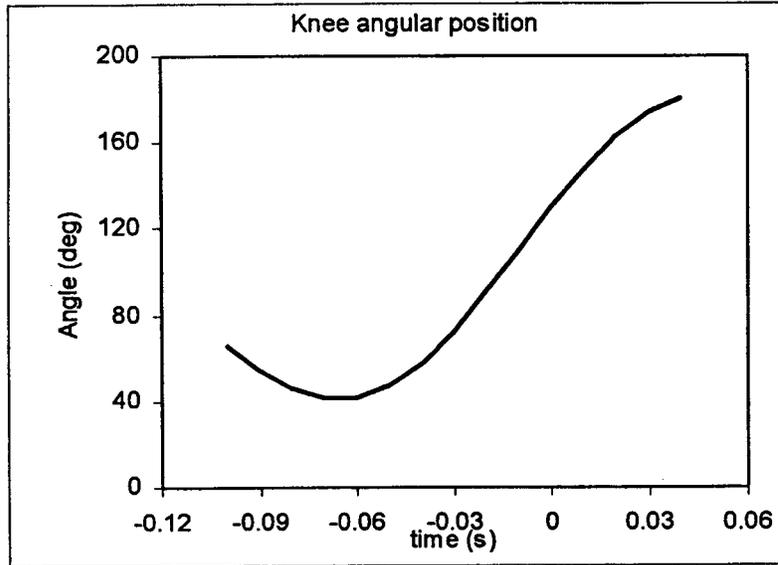
Velocity - rate of change of position wrt time

Acceleration - rate of change of velocity wrt time

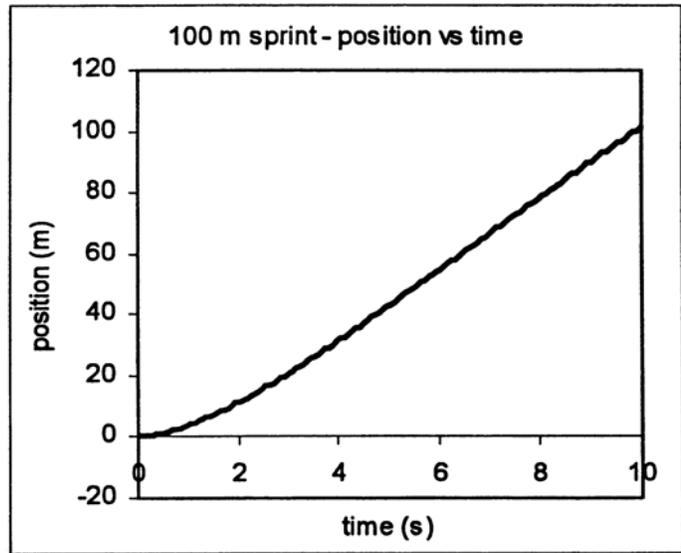
- Instantaneous velocity is reflected by the *slope* of the position curve at some instant in time.
- Instantaneous acceleration is reflected by the *slope* of the velocity curve at some instant in time.

*See soccer kick - angular position, velocity, and acceleration graphs next page*

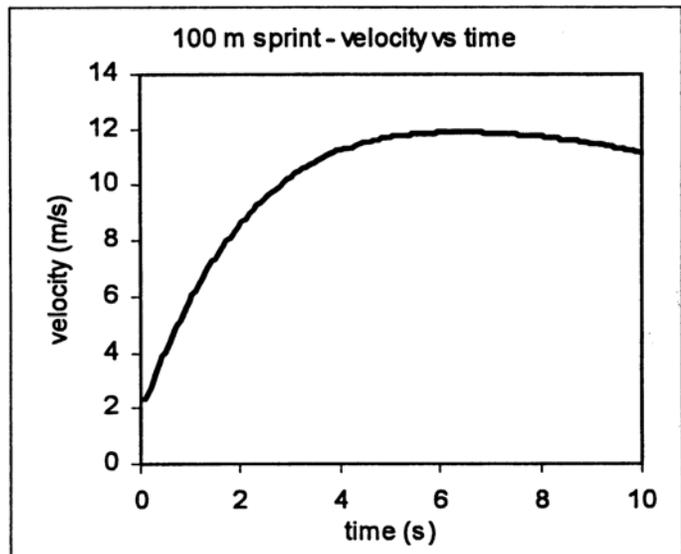
# Knee angular kinematic profile (soccer kick)



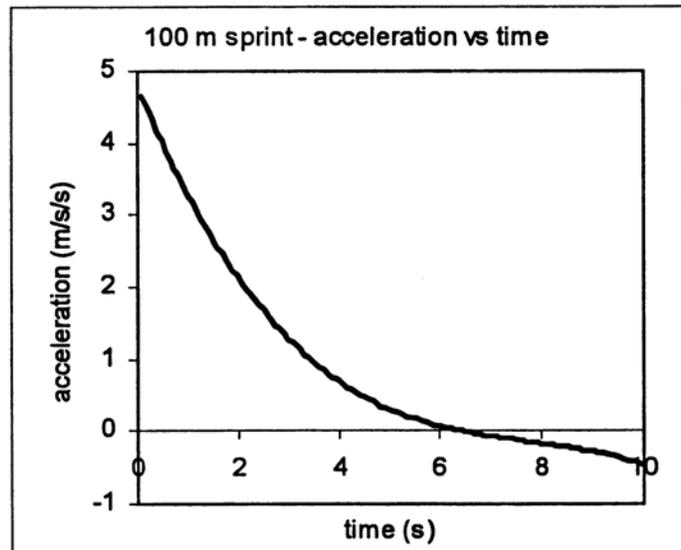
100 m dash linear  
kinematic profile  
(highly skilled  
sprinter)



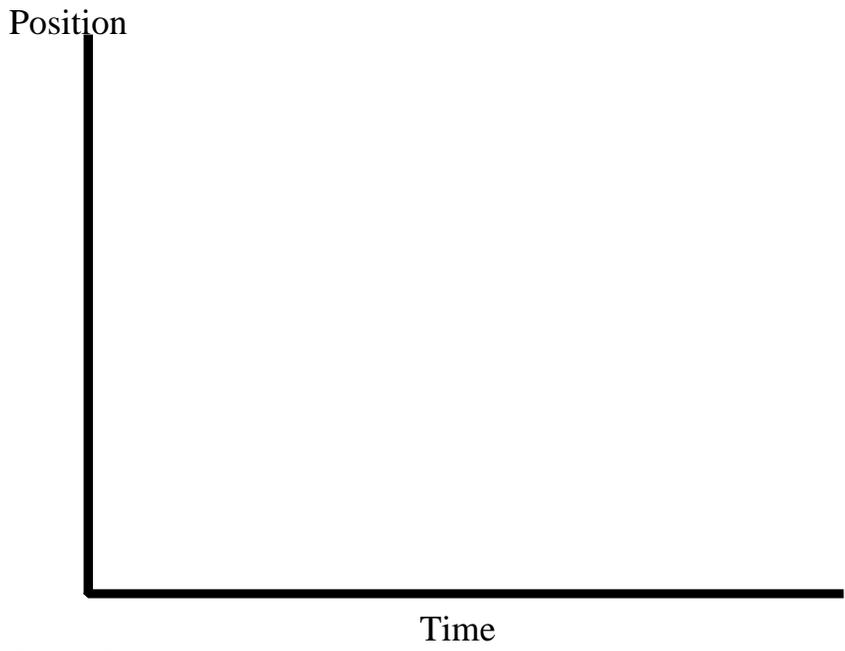
When is maximum  
velocity achieved?



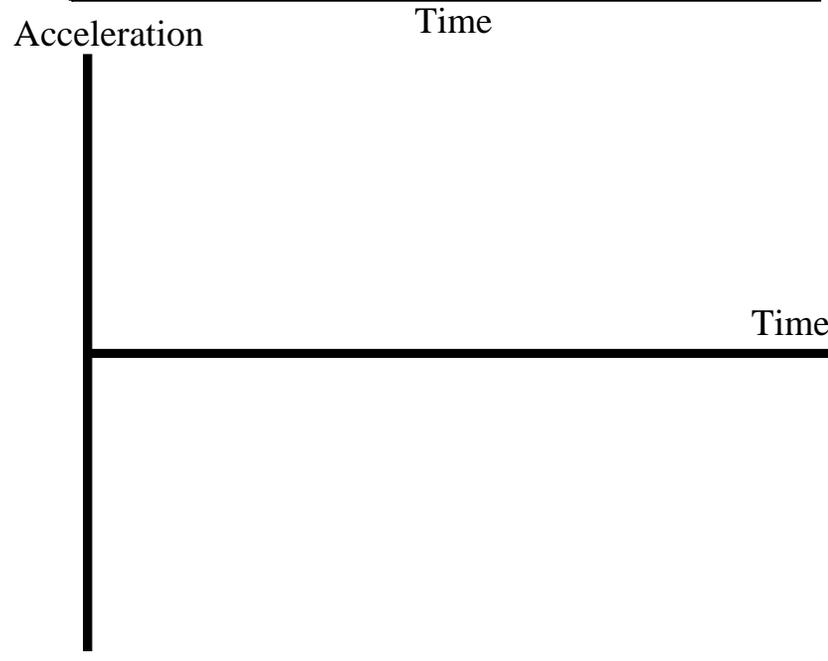
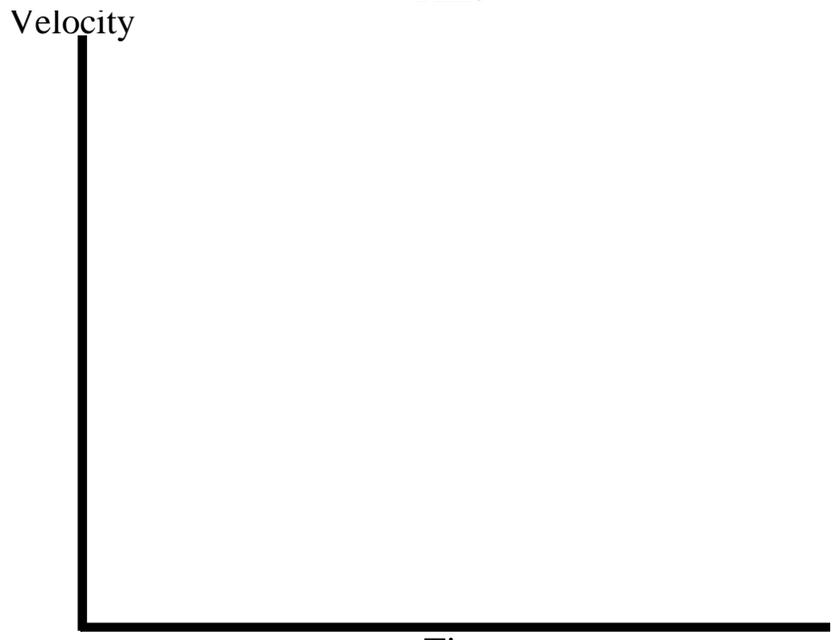
When is  
acceleration  
highest?



What is the  
approximate  
acceleration of  
sprinter 6 seconds  
into the race?



Can you deduce the position vs. time and acceleration vs. time profiles based on the velocity profile of a hand reaching for a glass of water?



<b><i>Six Cases of Acceleration</i></b>					
Case	Change in Speed	Starting Direction	Ending Direction	$\Delta v$	Accel. ( $\Delta v/\Delta t$ )
1	Speeding up				
2	Slowing down				
3	Speeding up				
4	Slowing down				
5	Reversing directions				
6	Reversing directions				

### Notes:

1. Speeding up in the positive direction = \_\_\_\_\_ acceleration
2. Slowing down in the positive direction = \_\_\_\_\_ acceleration
3. Speeding up in the negative direction = \_\_\_\_\_ acceleration
4. Slowing down in the negative direction = \_\_\_\_\_ acceleration
5. *Reversing directions* from positive to negative = \_\_\_\_\_ acceleration
6. *Reversing directions* from negative to positive = \_\_\_\_\_ acceleration.