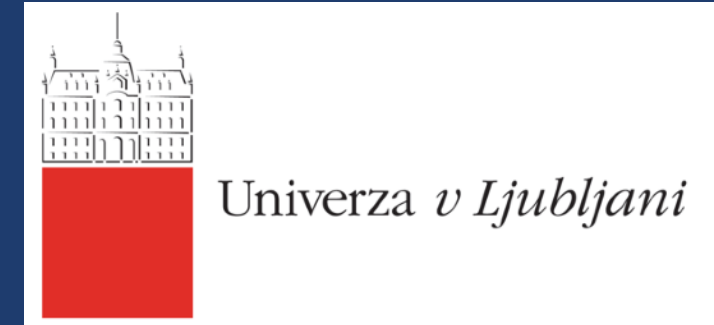


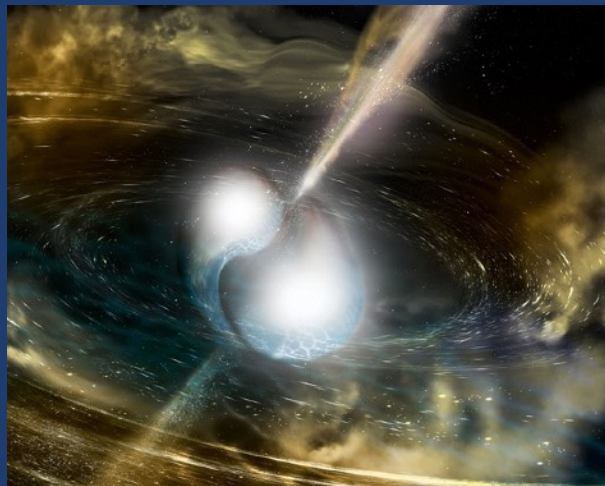
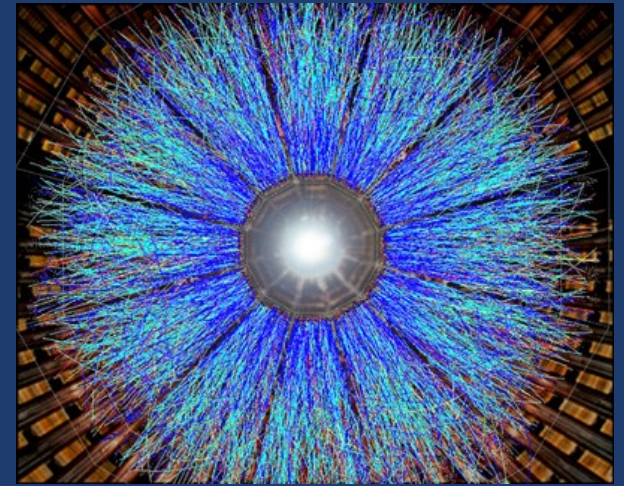
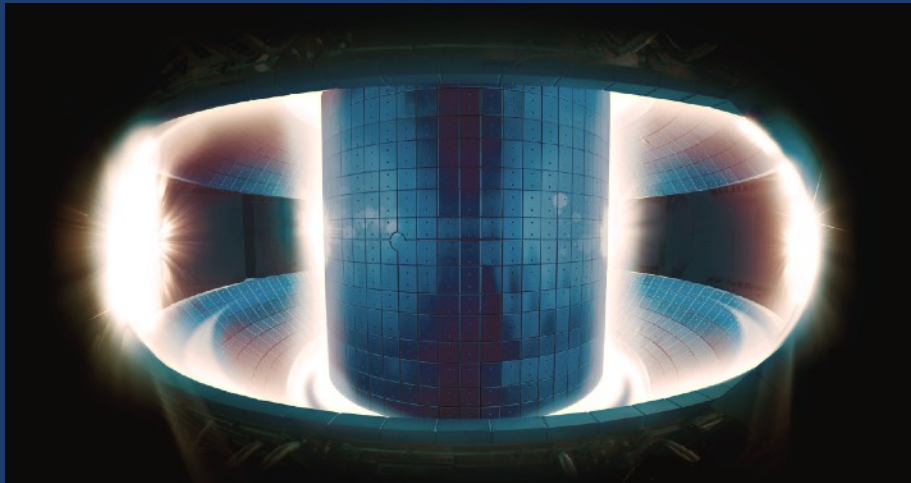
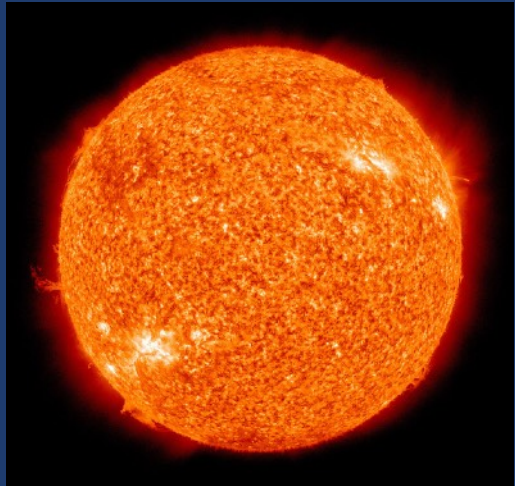


SAŠO GROZDANOV



STRONG-FIELD MAGNETOHYDRODYNAMICS

ASU THEORETICAL PHYSICS
COLLOQUIUM, 26.4.2023



microscopic UV physics
(QFT, EFT, holography)

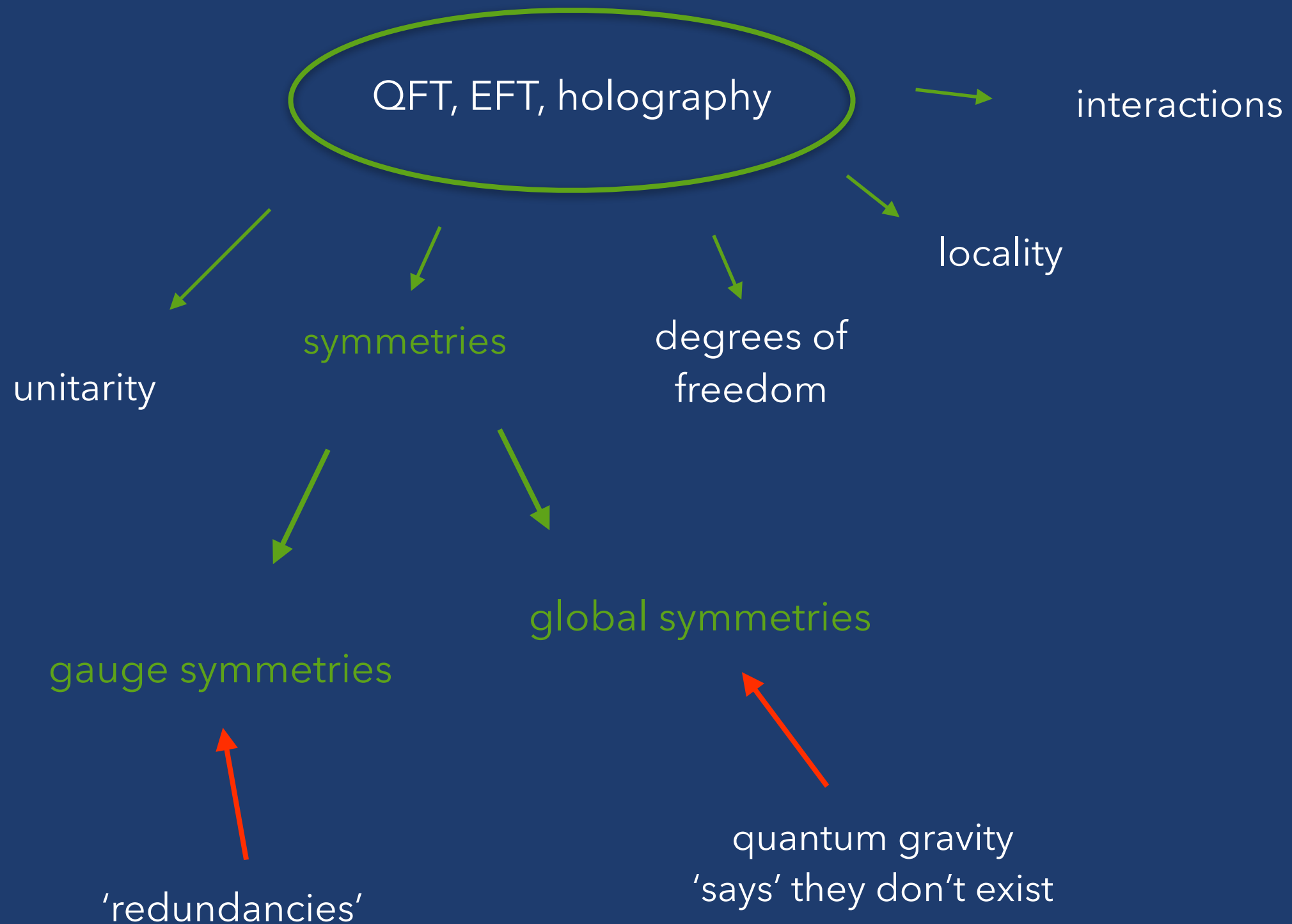


strongly magnetised fluid: **PLASMA**
magnetohydrodynamics

OUTLINE

- higher-form symmetries
- magnetohydrodynamics
- holographic magnetohydrodynamics
- new application: magnetic diffusion in neutron stars
- summary and future directions

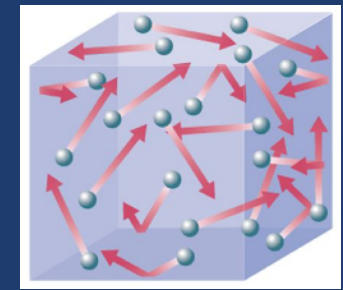
SYMMETRIES IN QFT AND EFT



GLOBAL HIGHER-FORM SYMMETRIES

- zero-form symmetry (one-form conserved current)

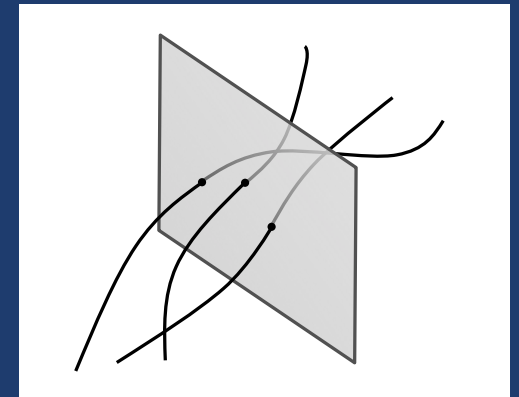
$$\mathcal{O}(x) \rightarrow e^{iq\Lambda} \mathcal{O}(x) \quad \partial_\mu J^\mu = 0$$



- one-form symmetry (two-form conserved current)

[Gaiotto, Kapustin, Seiberg, Willet (2014)]

$$W(C) \rightarrow \exp\left(iq \int_C \Lambda\right) W(C) \quad \partial_\mu J^{\mu\nu} = 0$$



- p -form symmetries count higher-dimensional objects

- EM without matter

$$J^{\mu\nu} = \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} F_{\rho\sigma}$$

$$\tilde{J}^{\mu\nu} = F^{\mu\nu}$$

$$Q = \int_{S_{d-p}} \star J_{p+1}$$

- EM coupled to matter (e.g., QED)

$$J^{\mu\nu} = \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} F_{\rho\sigma}$$

- symmetry is tautological in vacuum

$$\partial_\mu J^{\mu\nu} = \epsilon^{\mu\nu\rho\sigma} \partial_\mu \partial_\rho A_\sigma = 0$$

HIGHER-FORM SYMMETRIES

- continuous symmetries are Abelian, discrete symmetries can be non-Abelian
- SSB and Goldstone bosons [see Hofman, Iqbal (2018); Lake (2018)]

$$\text{zero-form symmetry : } \theta \rightarrow \theta + c, \quad S_{IR} \sim \int d\theta \wedge \star d\theta = \int d^4x \partial_\mu \theta \partial^\mu \theta$$

$$\text{one-form symmetry : } A \rightarrow A + d\alpha, \quad S_{IR} \sim \int dA \wedge \star dA = \int d^4x F_{\mu\nu} F^{\mu\nu}$$

- Goldstone boson of a broken symmetry is the **photon**
- the phase we are most familiar with is the broken phase
- order parameters of SSB

$$\text{zero-form symmetry : } \quad \text{unbroken: } \langle \mathcal{O}^\dagger(x) \mathcal{O}(y) \rangle \sim \exp \{-m|x - y|\}$$

$$\quad \text{broken : } \langle \mathcal{O}^\dagger(x) \mathcal{O}(y) \rangle \sim \langle \mathcal{O}^\dagger(x) \rangle \langle \mathcal{O}(y) \rangle$$

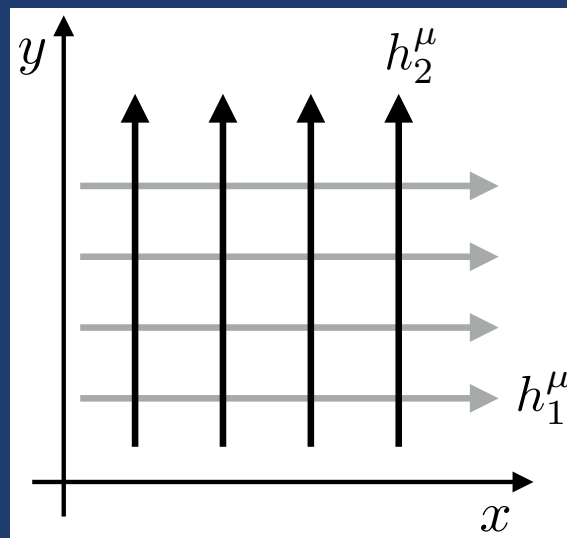
$$\text{one-form symmetry : } \quad \text{unbroken: } \langle W_C \rangle \sim \exp \{-T \text{Area}[C]\}$$

$$\quad \text{broken : } \langle W_C \rangle \sim \exp \{-T \text{Perimeter}[C]\}$$

- analogy with confinement

HIGHER-FORM SYMMETRIES

- many theories have higher-form symmetries:
abelian Higgs model, centre symmetries, various condensed matter systems
- another example: (visco)-elasticity
[Grozdanov, Poovuttikul, PRD (2018); Armas, Jain, JHEP (2019)]



- the language and formalism underpinning these symmetries has been quite thoroughly developed
- new concepts associated with this endeavour:
2-group, non-invertible symmetries that incorporate anomalies, etc.

MAGNETOHYDRODYNAMICS

MHD = Navier-Stokes + Maxwell (EM)

generalise



$$\frac{\partial \epsilon}{\partial t} + \nabla \cdot (\epsilon \vec{v}) = 0$$

$$\epsilon \left(\frac{\partial}{\partial t} + \vec{v} \cdot \nabla \right) \vec{v} = -\nabla p + \vec{J} \times \vec{B}$$

continuity

Euler (or Navier-Stokes)

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\nabla \times \vec{B} = \mu_0 \vec{J}$$

$$\nabla \cdot \vec{B} = 0$$

~~$$\nabla \cdot \vec{E} = 0$$~~

Maxwell

$$\vec{E} + \vec{v} \times \vec{B} = 0, \quad (\sigma \rightarrow \infty)$$

Ohm's law (ideal)

$$\left(\frac{\partial}{\partial t} + \vec{v} \cdot \nabla \right) \left(\frac{p}{\epsilon \gamma} \right) = 0$$

equation of state

- avoid mixing macroscopic and microscopic concepts

- what are the symmetries?

- general equation of state

$$B/T^2 \ll 1, \quad g \ll 1$$

- correct number of transport coefficients?

- quantum effects:
pair-creation, Landau levels?

HYDRODYNAMICS

- low-energy limit of QFTs – a Schwinger-Keldysh effective field theory
[SG, Polonyi (2013); Crossley, Glorioso, Liu (2015); Haehl, Loganayagam, Rangamani (2015); ...]
- conservation laws (equations of motion) of **globally conserved operators**

$$\nabla_{\mu} T^{\mu\nu} = 0 \quad \nabla_{\mu} J^{\mu} = 0$$

- **tensor structures** (symmetries, gradient expansions) and **transport coefficients** (QFT)

$$T^{\mu\nu} = \sum_{n=0}^{\infty} \left[\sum_i^N \lambda_i^{(n)} \mathcal{T}_{(n)}^{\mu\nu} \right]$$

$$\xrightarrow[\substack{u^{\mu} \sim T \sim e^{-i\omega t + iqz}}]{\nabla_{\mu} T^{\mu\nu} = 0}$$

$$\omega(q) = \sum_{n=1}^{\infty} \alpha_n q^n$$

$$\partial u^{\mu} \sim \partial T \ll 1$$

$$\longrightarrow$$

$$\omega/T \sim q/T \ll 1$$

- first-order truncation = Navier-Stokes equations
- dispersion relations:

shear diffusion

$$\omega = -iDq^2$$

sound

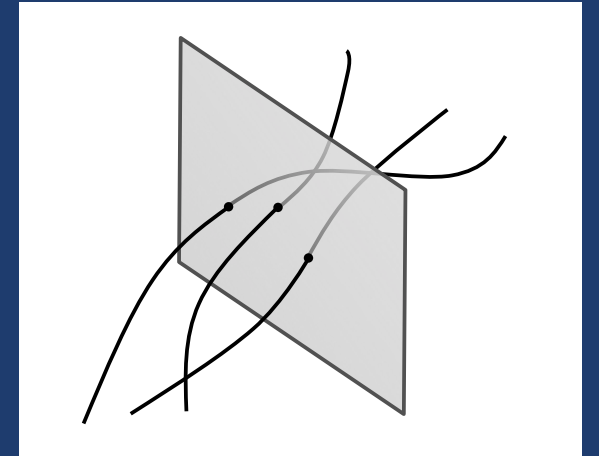
$$\omega = \pm v_s q - i\Gamma q^2$$

equilibrium
temperature

$$q = \sqrt{\mathbf{q}^2}$$

HIGHER-FORM SYMMETRIES AND MHD

- plasma is a phase with an unbroken one-form symmetry and no IR massless photons (Debye screening)
- $\partial_\mu J^{\mu\nu} = 0$ – Ward identity becomes powerful
- magnetohydrodynamics (MHD) is the IR EFT
- IR dynamics encoded in conservation laws



counting # of magnetic flux lines crossing a 2d surface

$$\begin{aligned}\partial_\mu T^{\mu\nu} &= 0 \\ \partial_\mu J^{\mu\nu} &= 0\end{aligned}$$

$$J^{\mu\nu} = \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} F_{\rho\sigma}$$

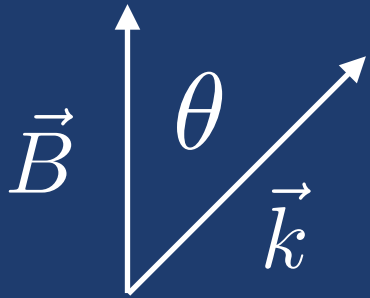
- general formulation for any plasma (EoM level) [Grozdanov, Hofman, Iqbal, PRD (2017)]
- any equation of state $P(B, T)$
- transport coefficients (2+3 viscosities and 2 resistivities) \longrightarrow
- electric field \mathbf{E} is induced at derivative level

functions of B and T

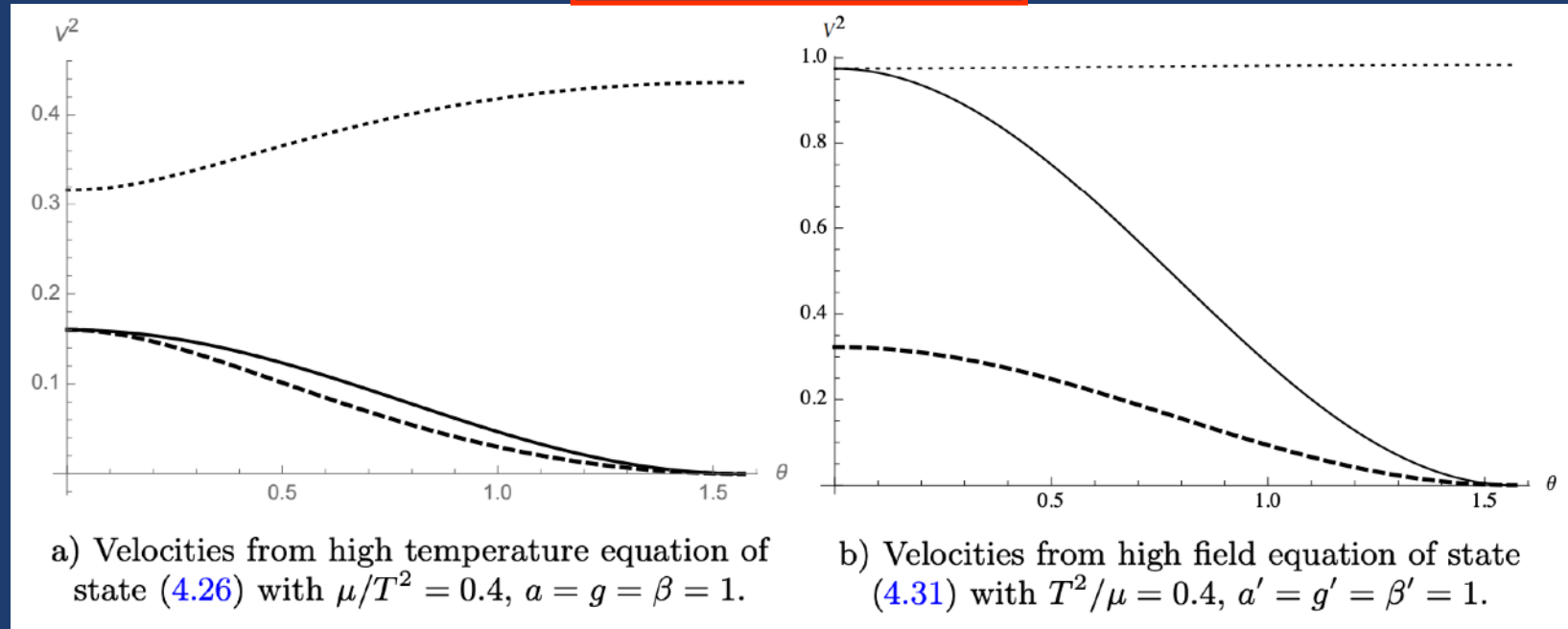
$$\begin{aligned}\eta_\perp &\geq 0 & \eta_\parallel &\geq 0 \\ r_\perp &\geq 0 & r_\parallel &\geq 0 \\ \zeta_\perp &\geq 0 & \zeta_\perp \zeta_\parallel &\geq \zeta_\times^2\end{aligned}$$

HIGHER-FORM SYMMETRIES AND MHD

- strong- \mathbf{B} dispersion relations



speeds of waves



- Kubo formulae for resistivities (also *wip* with Frangi)

$$r = 1/\sigma (?)$$

$$r_{\parallel} = \lim_{\omega \rightarrow 0} \lim_{k^z \rightarrow 0} \frac{\langle J^{xy}(-\omega, -k^z) J^{xy}(\omega, k^z) \rangle_R}{-i\omega}$$

$$r_{\perp} = \lim_{\omega \rightarrow 0} \lim_{k^z \rightarrow 0} \frac{\langle J^{xz}(-\omega, -k^z) J^{xz}(\omega, k^z) \rangle_R}{-i\omega}$$

- symmetry-enhanced (non-dissipative) $T = 0$ limit due to $SO(1,1)$ boost symmetry along the strings (flux lines)
- example: Alfvén waves

$$\omega = \pm k \cos \theta$$

HIGHER-FORM SYMMETRIES AND MHD

- old theories are special limits of new generalised MHD
- can be easily systematically extended using our formalism

first-order expansion in $B/T^2 \ll 1$

zero-temperature limit: $T = 0$

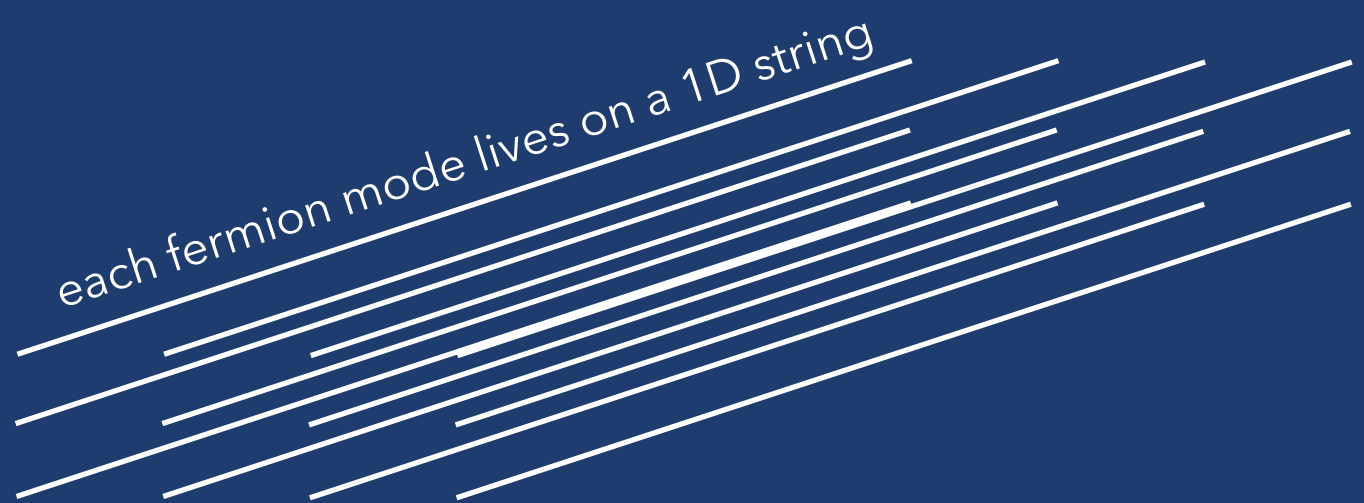
- massless lowest Landau level fermion in a strong, dynamical magnetic field
+ $2d$ bosonisation
- force-free electrodynamics
and corrections [Glorioso, Son (2018)]
Maxwell's equations
+ constraint

$$\mathbf{E} \cdot \mathbf{B} = 0$$

standard, textbook ideal MHD
with new dissipative terms

$$P(B, T) = \frac{a}{4} T^4 + \frac{g^2}{2} B^2 + \frac{\beta}{4} \frac{B^4}{T^4} + \dots$$

each fermion mode lives on a 1D string




EXAMPLE: LEADING-ORDER CORRECTED NON-RELATIVISTIC MHD

$$\partial_i B^i = 0$$

$$\partial_t B^i = -\varepsilon^{ijk} \partial_j E_k, \quad E^i = -(\vec{v} \times \vec{B})^i + j_{diss}^i$$

$$\partial_t \varepsilon + \partial_i (\varepsilon v^i) = 0$$

$$\varepsilon (\partial_t + \vec{v} \cdot \nabla) v^i = -\partial^i p + (\vec{B} \cdot \nabla) B^i + \partial_i \Pi_{visc}^{ij}$$

$$p(T, B) = \text{the equation of state}$$

extremely complicated equations
are systematically generated from
the simpler higher-form language

$$j_{diss}^i = r_{\perp} \frac{T}{B^2} \varepsilon^{ijk} \left[B^n \partial_j \left(\frac{\mu_B B_n}{T} \right) - \vec{B} \cdot \nabla \left(\frac{\mu_B B_j}{T} \right) \right] B_k + r_{\parallel} \left(\frac{\mu_B B^i}{B} \right) B_p \varepsilon^{pmn} \partial_m \left(\frac{B_n}{B} \right)$$

$$\begin{aligned} \Pi_{diss}^{ij} = & \eta_{\perp} \left[(\mathcal{S}^{ij} - \delta^{ij} (\nabla \cdot \vec{v})) + \frac{B^i B^j}{B^2} (\nabla \cdot \vec{v}) + \delta^{ij} \frac{\vec{B} \cdot (\vec{B} \cdot \nabla) v}{B^2} - \frac{1}{B^2} (B^i (\vec{B} \cdot \nabla) v^j + B^j (\vec{B} \cdot \nabla) v^i) \right] \\ & + \eta_{\parallel} \left[\frac{1}{B^2} \left(B^i \mathcal{S}^{jk} B_k + B^j \mathcal{S}^{jk} B_k - \frac{2B^i B^j}{B^4} B^k B^l \mathcal{S}_{kl} \right) \right] + \left[\delta^{ij} - \frac{B^i B^j}{B^2} \right] \delta f + \frac{B^i B^j}{B^2} \delta \tau \end{aligned}$$

$$\mathcal{S}^{ij} = \partial^i v^j + \partial^j v^i$$

$$\delta f = -\zeta_{\perp} \left((\nabla \cdot \vec{v}) - \frac{\vec{B} \cdot (\vec{B} \cdot \nabla) \vec{v}}{B^2} \right) - \zeta_{\times} \left(\frac{\vec{B} \cdot (\vec{B} \cdot \nabla) \vec{v}}{B^2} \right)$$

$$\delta \tau = -\zeta_{\times} \left((\nabla \cdot \vec{v}) - \frac{\vec{B} \cdot (\vec{B} \cdot \nabla) \vec{v}}{B^2} \right) - \zeta_{\parallel} \left(\frac{\vec{B} \cdot (\vec{B} \cdot \nabla) \vec{v}}{B^2} \right)$$

HOLOGRAPHIC MHD

- holographic duality:

some QFTs in 4d = gravity (string theory) in 5d

- holographic dual of a magnetised plasma
[Grozdanov, Poovuttikul, JHEP (2017); Hofman, Iqbal, SciPost (2017)]

- generating functional

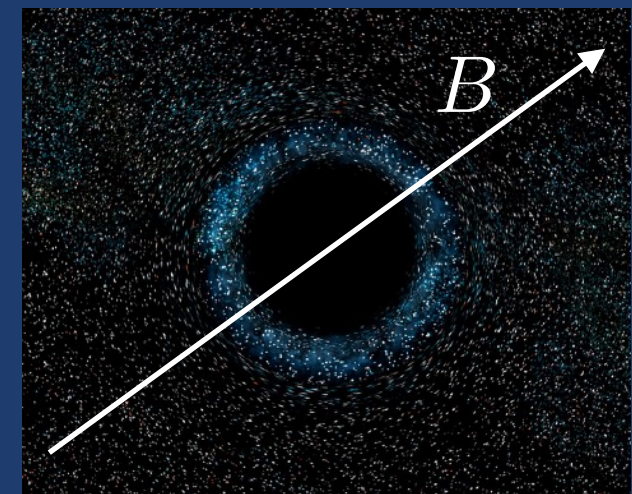
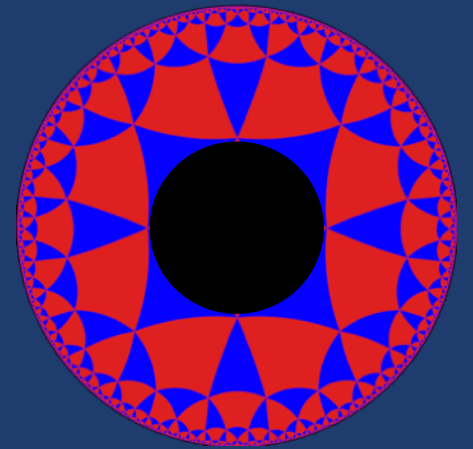
$$W [g_{\mu\nu}, b_{\mu\nu}] = \left\langle \exp \left[i \int d^4x \sqrt{-g} \left(\frac{1}{2} T^{\mu\nu} g_{\mu\nu} + J^{\mu\nu} b_{\mu\nu} \right) \right] \right\rangle$$

- theory of gravity and **two-form gauge field** ($H = db$) in 5d

$$S = \frac{N_c^2}{8\pi^2} \left[\int d^5x \sqrt{-g} \left(R + 12 - \frac{1}{3e^2} H_{\mu\nu\rho} H^{\mu\nu\rho} \right) + \int_{\partial M} d^4x \sqrt{-\gamma} \left(2 \text{tr} K - 6 + \frac{1}{e^2} \mathcal{H}_{ab} \mathcal{H}^{ab} \ln \mathcal{C} \right) \right]$$

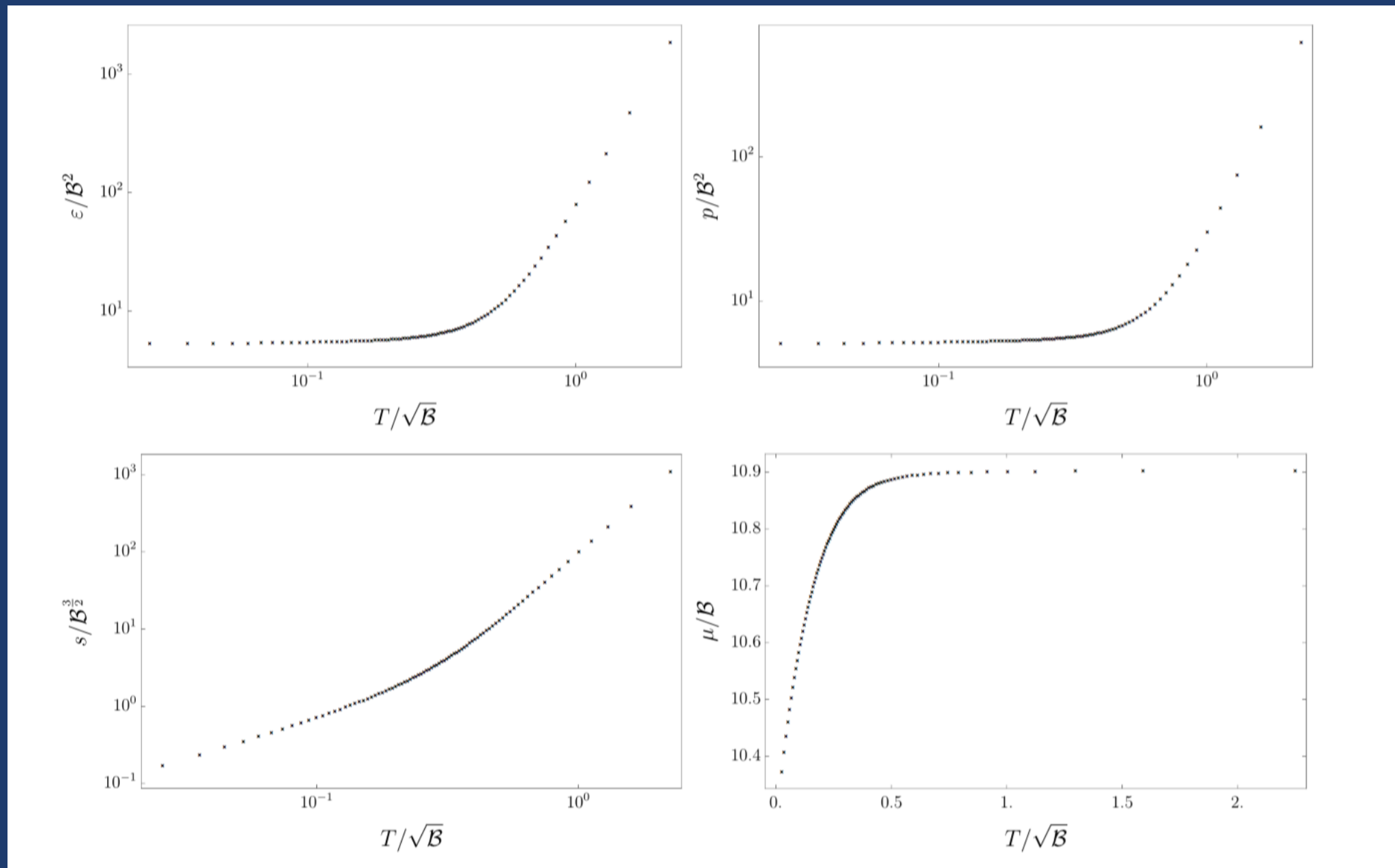
+ mixed boundary conditions

- holographic model with **dynamical electromagnetism** (gauged U(1) R-symmetry)

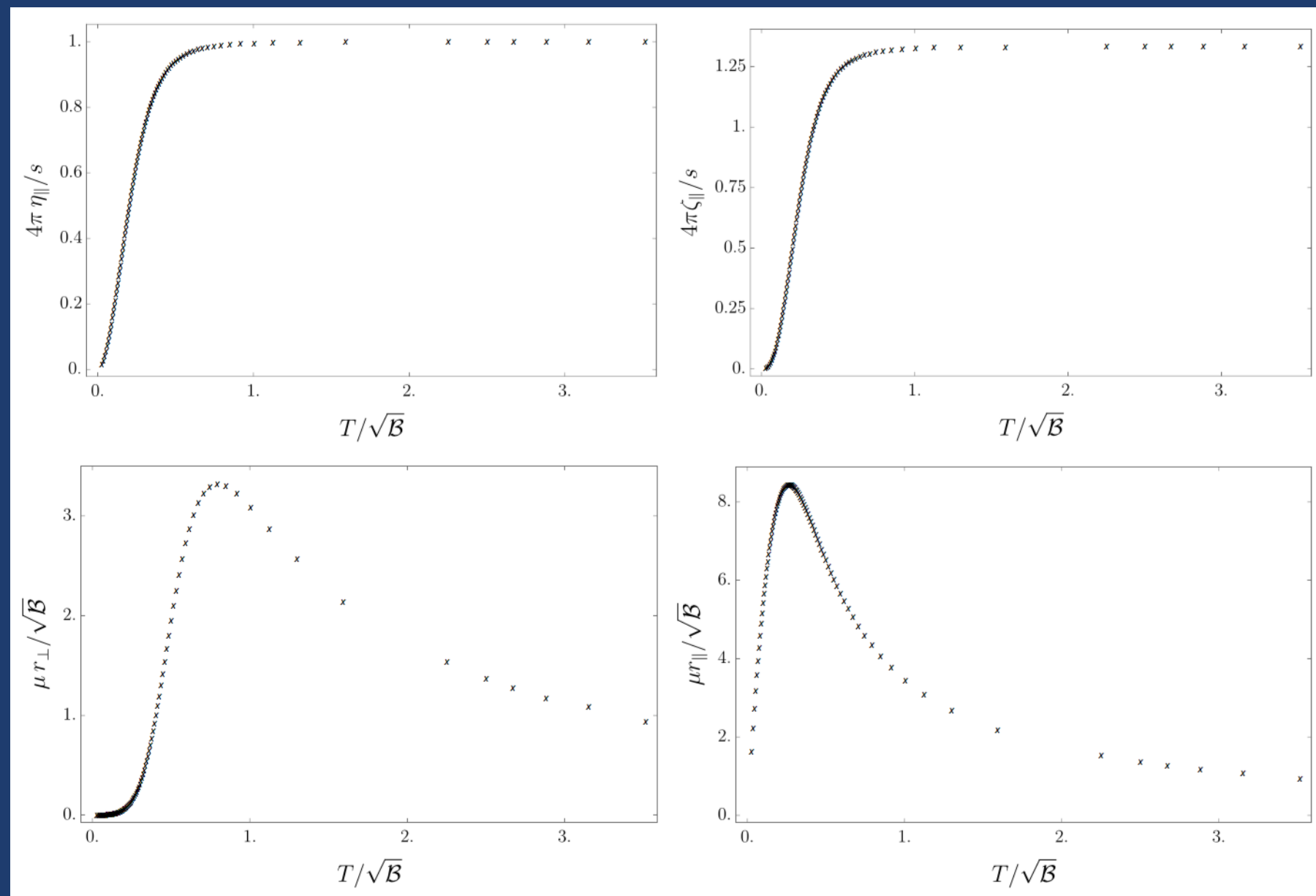


HOLOGRAPHIC MHD EQUATION OF STATE

	weak field ($T/\sqrt{\mathcal{B}} \gg 1$)	strong field ($T/\sqrt{\mathcal{B}} \ll 1$)
ε	$\frac{N_c^2}{2\pi^2} (74.1 \times T^4)$	$\frac{N_c^2}{2\pi^2} (5.62 \times \mathcal{B}^2)$
p	$\frac{N_c^2}{2\pi^2} (25.3 \times T^4)$	$\frac{N_c^2}{2\pi^2} (5.32 \times \mathcal{B}^2)$
s	$\frac{N_c^2}{2\pi^2} (99.4 \times T^3)$	$\frac{N_c^2}{2\pi^2} (7.41 \times \mathcal{B} T)$
μ	$\frac{N_c^2}{2\pi^2} (10.9 \times \mathcal{B})$	$\frac{N_c^2}{2\pi^2} (2.88 \times \mathcal{B})$



HOLOGRAPHIC MHD TRANSPORT COEFFICIENTS



	weak field ($T/\sqrt{B} \gg 1$)	strong field ($T/\sqrt{B} \ll 1$)
η_{\perp}	$\frac{s}{4\pi}$	$\frac{s}{4\pi}$
η_{\parallel}	$1.00 \times \frac{s}{4\pi}$	$\frac{s}{4\pi} \left(21.32 \times \frac{T^2}{B} \right)$
ζ_{\perp}	$0.33 \times \frac{s}{4\pi}$	$\frac{s}{4\pi} \left(16.34 \times \frac{T^3}{B^{3/2}} \right)$
ζ_{\parallel}	$1.33 \times \frac{s}{4\pi}$	$\frac{s}{4\pi} \left(65.37 \times \frac{T^3}{B^{3/2}} \right)$
ζ_{\times}	$-0.66 \times \frac{s}{4\pi}$	$-\frac{s}{4\pi} \left(32.69 \times \frac{T^3}{B^{3/2}} \right)$
r_{\perp}	$\frac{B}{\mu} \left(3.37 \times \frac{1}{T} \right)$	$\frac{\sqrt{B}}{\mu} \left(4.7 \times \frac{T^3}{B^{3/2}} \right)$
r_{\parallel}	$\frac{B}{\mu} \left(3.37 \times \frac{1}{T} \right)$	$\frac{\sqrt{B}}{\mu} \left(62.3 \times \frac{T}{\sqrt{B}} \right)$

- maximal resistivity
- bulk viscosities

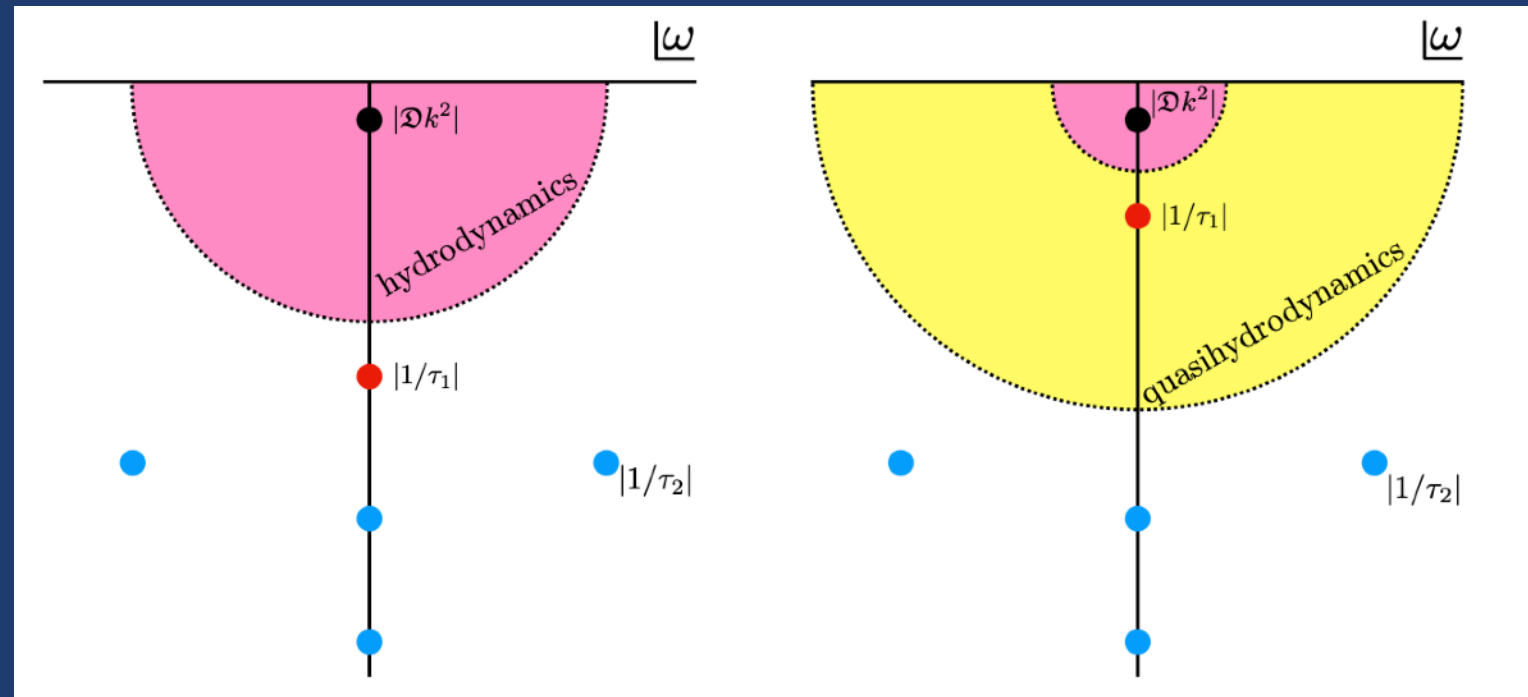
$$\zeta_{\perp} \zeta_{\parallel} = \zeta_{\times}^2$$

- all transport coefficients must vanish at $T = 0$
[Grozdanov, Hofman, Iqbal, PRD (2017)]
- holography agrees
[Grozdanov, Poovuttikul, JHEP (2017)]

reminiscent of Kovtun-Son-Starinets and Haack-Yarom – minimisation of entropy
[see Grozdanov, Starinets, JHEP (2014)]

BEYOND MHD

- *quasihydrodynamics*
[Grozdanov, Lucas, Poovuttikul, PRD (2018)]
- screened photons
- dynamical electric fields
- Ampere's law
- Müller-Israel-Stewart theory structure
- systematic construction of EFTs beyond the MHD limit
- study of plasma instabilities



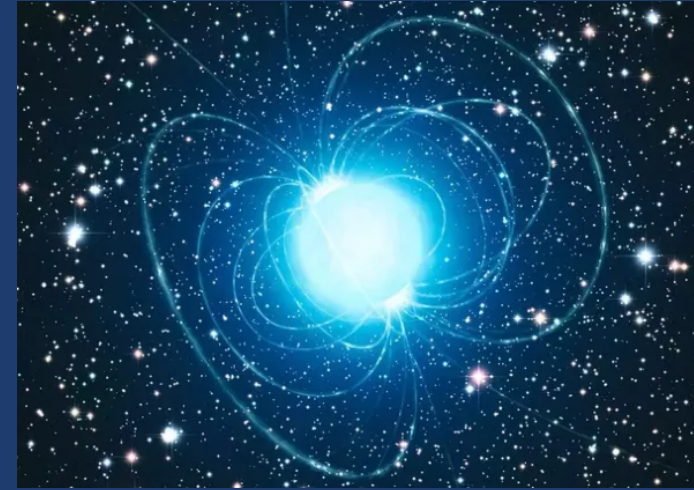
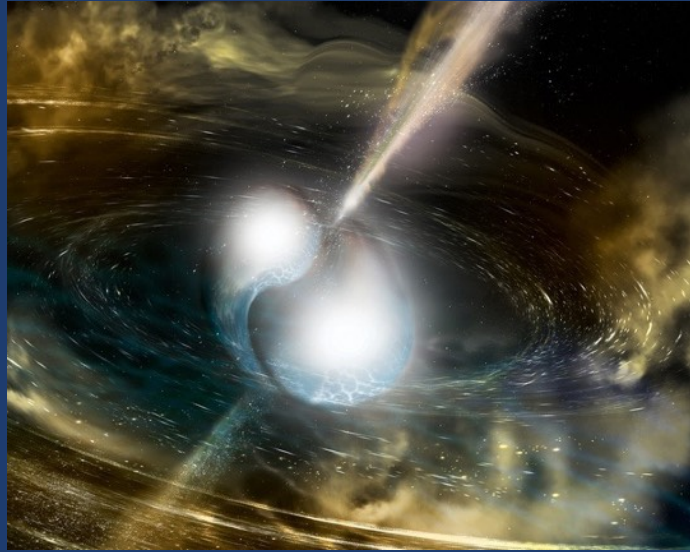
$$\partial_t \mathbf{E} - \nabla \times \mathbf{B} = -\frac{1}{\tau} (\mathbf{E} + \mathbf{v} \times \mathbf{B}) + O(\partial^2)$$

$$J^{\mu\nu} = 2\rho u^{[\mu} h^{\nu]} + \mathcal{J}^{\mu\nu}, \quad u^\lambda \nabla_\lambda \mathcal{J}^{\mu\nu} + \dots = -\frac{1}{\tau} \mathcal{J}^{\mu\nu}$$



NEW APPLICATION: MAGNETIC DIFFUSION IN NEUTRON STARS

[GROZDANOV, LEUTHEUSSER, LIU, VARDHAN, 2022 AND 2023]



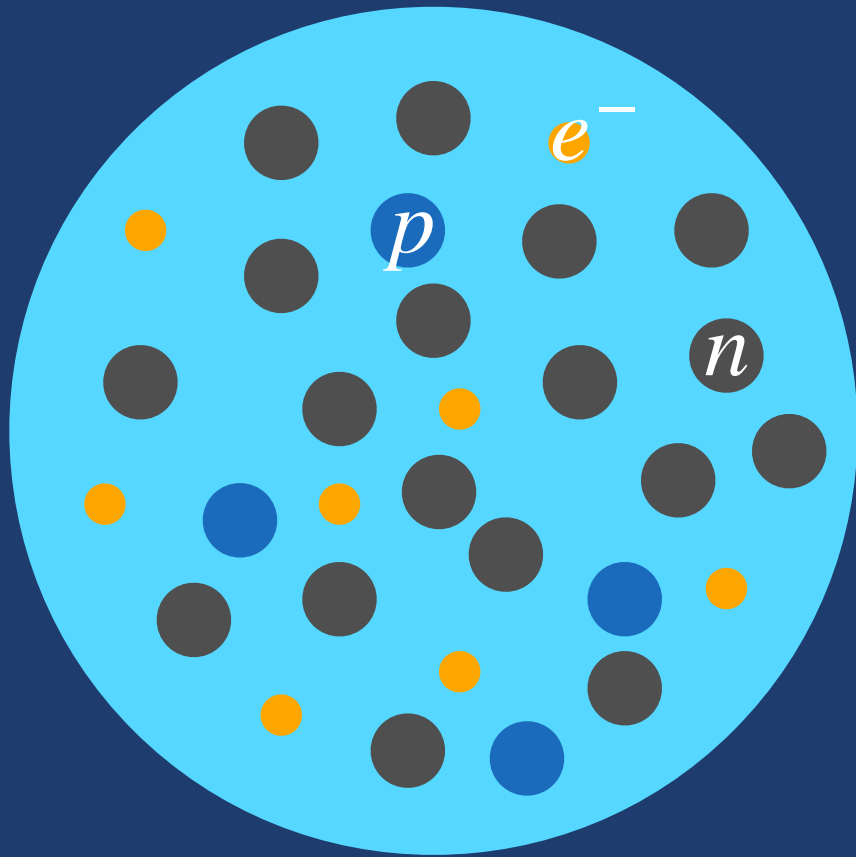
dynamics of strong magnetic fields in
neutron stars

old: microscopic model of
Goldreich and Reisenegger (1992)

new approach: higher-form
symmetries and EFT

MAGNETIC DIFFUSION IN NEUTRON STARS

- theory of magnetic field evolution [Goldreich and Reisenegger (1992)]
- neutron star is a fluid made of neutrons, electrons and protons



$$\mu_n + m_n \psi = \text{constant}$$

$$m_p \frac{\partial v_p}{\partial t} + m_p (v_p \cdot \nabla) v_p = -\nabla \mu_p - m_p \nabla \psi + e \left(\mathbf{E} + \frac{v_p}{c} \times \mathbf{B} \right) - \frac{m_p v_p}{\tau_{pn}} - \frac{m_p (v_p - v_e)}{\tau_{pe}},$$

$$m_e^* \frac{\partial v_e}{\partial t} + m_e^* (v_e \cdot \nabla) v_e = -\nabla \mu_e - e \left(\mathbf{E} + \frac{v_e}{c} \times \mathbf{B} \right) - \frac{m_e^* v_e}{\tau_{en}} - \frac{m_e^* (v_e - v_p)}{\tau_{ep}}.$$

$$\Delta \Gamma \equiv \Gamma(p + e^- \rightarrow n + \nu_e) - \Gamma(n \rightarrow p + e^- + \bar{\nu}_e) = \lambda \Delta \mu$$

weak interactions influence continuity equations

$$\frac{\partial \mathbf{B}}{\partial t} = -c \nabla \times \left(\frac{\mathbf{j}}{\sigma_0} \right) + \nabla \times (\mathbf{v} \times \mathbf{B}) - \left(\frac{m_p/\tau_{pn} - m_e^*/\tau_{en}}{m_p/\tau_{pn} + m_e^*/\tau_{en}} \right) \nabla \times \left(\frac{\mathbf{j} \times \mathbf{B}}{n_c e} \right)$$

$$\sigma_0 = n_c e^2 \left(\frac{1}{\tau_{ep}/m_e^*} + \frac{1}{\tau_{pn}/m_p + \tau_{en}/m_e^*} \right)^{-1} \quad \frac{v_p + v_e}{2} = \mathbf{v} - \left(\frac{m_p/\tau_{pn} - m_e^*/\tau_{en}}{m_p/\tau_{pn} + m_e^*/\tau_{en}} \right) \frac{\mathbf{j}}{2n_c e} \quad \mathbf{j} = \frac{c \nabla \times \mathbf{B}}{4\pi}$$

MAGNETIC DIFFUSION IN NEUTRON STARS

- theory of magnetic field evolution [Goldreich and Reisenegger (1992)]
- neutron star is a fluid made of neutrons, electrons and protons
- phenomenological considerations give MHD evolution equations for magnetic diffusion
- coefficients are determined in terms of microscopic quantities

$$\nabla \cdot \mathbf{B} = 0, \quad \partial_t \mathbf{B} = -\nabla \times \mathbf{E}$$

$$\mathbf{E} = \eta \mathbf{j} + c_a (\mathbf{j} \times \mathbf{B}) \times \mathbf{B} + c_H \mathbf{j} \times \mathbf{B}$$

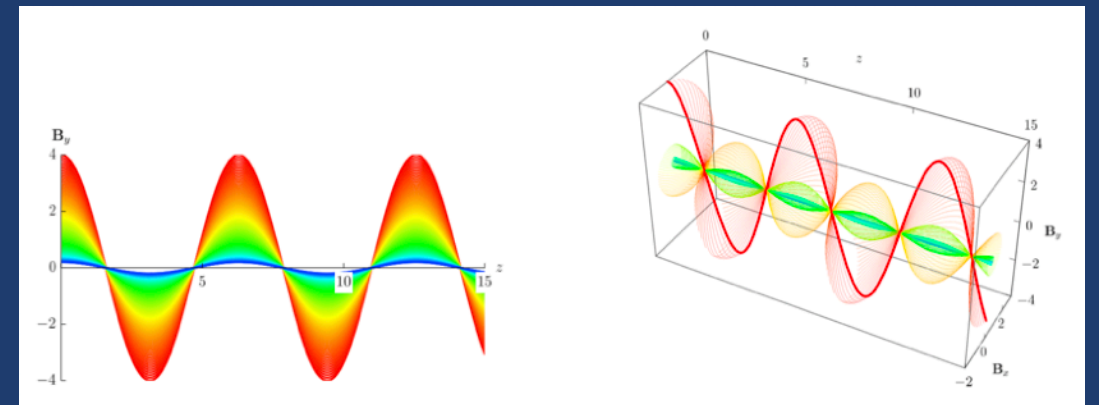
$$\mathbf{j} \equiv \nabla \times \mathbf{B}, \quad \eta, c_a, c_H = \text{const.}$$

Hall drift

standard diffusion

$$\partial_t \mathbf{B} = \eta \nabla^2 \mathbf{B}$$

ambipolar diffusion

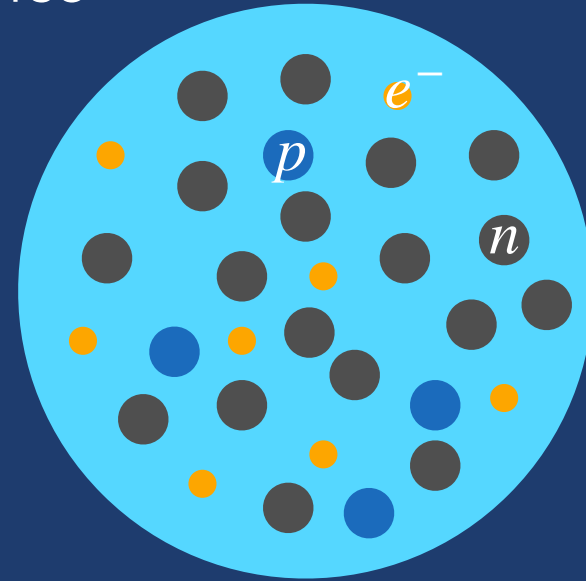


MAGNETIC DIFFUSION IN NEUTRON STARS

- EFT (CTP formalism) for the one-form symmetry with broken C-invariance
[Grozdanov, Leutheusser, Liu, Vardhan, 2207.01636 & to appear]

$$J^{0i} = a G_{0i} - \beta_0 (c \delta_{ij} + \tilde{c} G_{0i} G_{0j}) \partial_0 G_{0j} + h \epsilon_{ijn} G_{0n} \partial_0 G_{0j} + m \delta_{ij} \epsilon_{klm} G_{0m} H_{jkl}$$

$$J^{ij} = -2\beta_0 (d \delta_{ik} \delta_{jl} + \tilde{d} \epsilon_{ijm} \epsilon_{klm} G_{0m} G_{0n}) \partial_0 G_{kl} - m \epsilon_{lij} \partial_l G_{0k}^2 + 2p \delta_{k[i} \epsilon_{j]ln} G_{0n} \partial_0 G_{kl}$$



- new magnetic diffusion equation

$$\nabla \cdot \mathbf{B} = 0, \quad \partial_t \mathbf{B} = -\nabla \times \mathbf{E}$$

$$\mathbf{E} = \eta \mathbf{j} + c_a (\mathbf{j} \times \mathbf{B}) \times \mathbf{B} + c_H \mathbf{j} \times \mathbf{B}$$

$$- c_H (\nabla \ln a(\mathbf{B}^2) \times \mathbf{B}) \times \mathbf{B} - c_\eta \nabla \ln a(\mathbf{B}^2) \times \mathbf{B} + \nabla f$$

$$\eta = c_\eta + c_a \mathbf{B}^2, \quad c_\eta = \frac{2\beta_0 d}{a}, \quad c_a = \frac{4\beta_0 \tilde{d}}{a^3}, \quad c_H = -\frac{p}{a^2}$$

all functions
of \mathbf{B}

- one can compute all correlation functions of \mathbf{B} and \mathbf{E} from auxiliary higher-form variables
– a much more ‘natural’ description

MAGNETIC DIFFUSION IN NEUTRON STARS

- magnetic field dependence of susceptibilities

$$\chi_{\parallel} = a + \tilde{a}B_0^2, \quad \chi_{\perp} = a, \quad \tilde{a} = 2a'(B_0^2)$$

- Kubo formulae:

$$\chi_{\parallel} = \lim_{\mathbf{k} \rightarrow 0} \lim_{\omega \rightarrow 0} G^R(B_z, B_z), \quad \chi_{\perp} = \lim_{\mathbf{k} \rightarrow 0} \lim_{\omega \rightarrow 0} G^R(B_x, B_x)$$

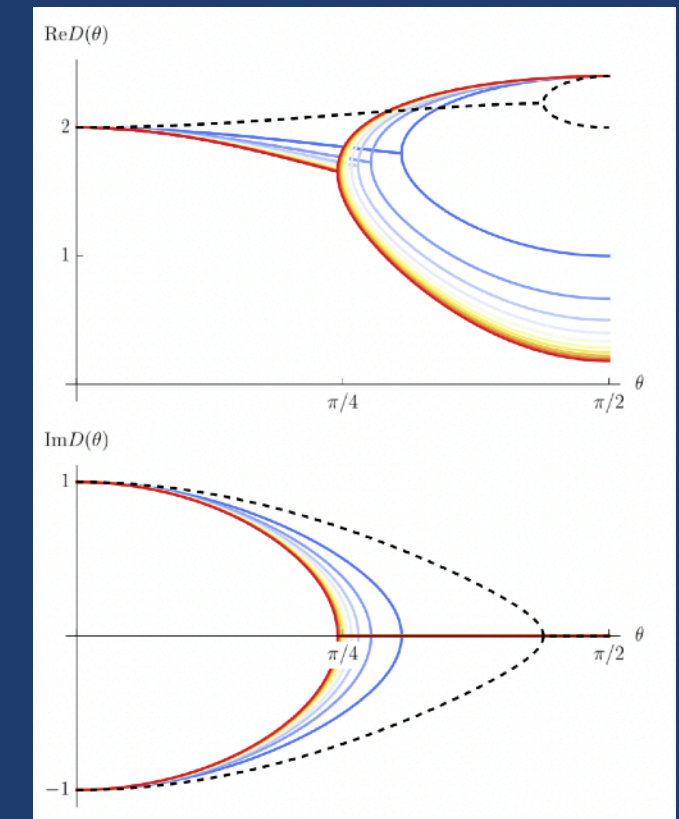
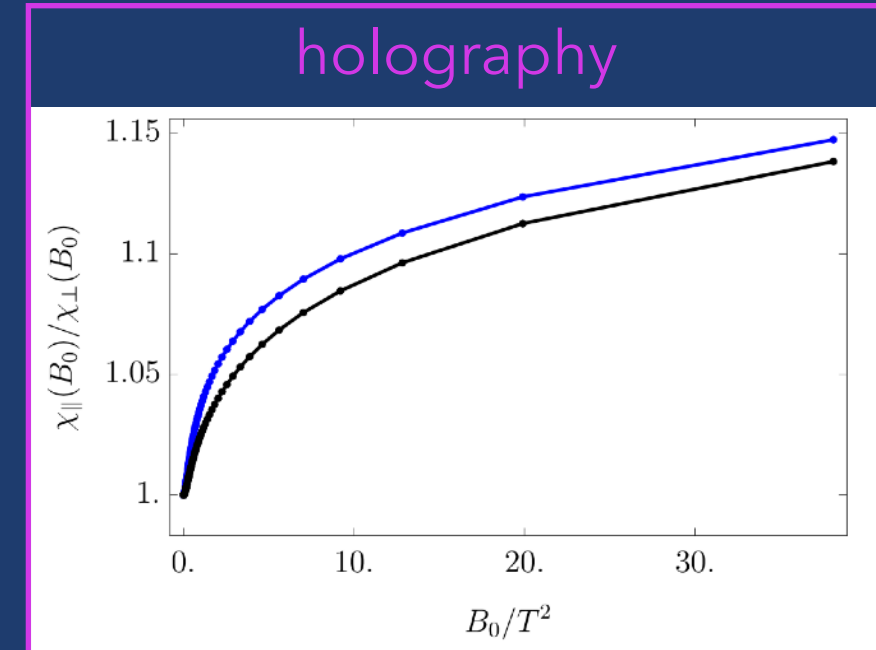
$$\sigma^{\parallel} = \lim_{\omega \rightarrow 0} \lim_{\mathbf{k} \rightarrow 0} \frac{1}{i\omega} G^R(E_z, E_z), \quad \sigma_1^{\perp} = \lim_{\omega \rightarrow 0} \lim_{\mathbf{k} \rightarrow 0} \frac{1}{i\omega} G^R(E_x, E_x), \quad \sigma_2^{\perp} = \lim_{\omega \rightarrow 0} \lim_{\mathbf{k} \rightarrow 0} \frac{1}{i\omega} G^R(E_x, E_y)$$

- 'corrected' diffusive dispersion relation

$$\omega = -i \frac{\sigma_1^{\perp}}{\chi_{\perp}} k_z^2 - \frac{i}{2} \left(\frac{\sigma^{\parallel}}{\chi_{\perp}} + \frac{\sigma_1^{\perp}}{\chi_{\parallel}} \right) k_{\perp}^2$$

$$\mp \frac{i}{2} \sqrt{\left(\frac{\sigma^{\parallel}}{\chi_{\perp}} - \frac{\sigma_1^{\perp}}{\chi_{\parallel}} \right)^2 k_{\perp}^4 - 4 \left(\frac{\sigma_2^{\perp}}{\chi_{\perp}} \right)^2 \left(k_z^2 + \frac{\chi_{\perp}}{\chi_{\parallel}} k_{\perp}^2 \right) k_z^2}$$

$$\omega = -iD(\theta)k^2$$



SUMMARY AND FUTURE DIRECTIONS

- formal approach to QFTs enables new physical insights
- plasma can be understood as a string fluid
- higher-form symmetries and new developments in EFTs allow for a new, general formulation of magnetohydrodynamics applicable to strong \mathbf{B} fields
- new predictions, including a new theory of magnetic diffusion in neutron stars
- next step: non-linear evolution of the (diffusion) equation (best variables?)
- include other effects: superfluidity, ...
- how large are new effects in realistic neutron stars or other realistic plasmas?



THANK YOU!