### **Does the spin "flow" in relativistic heavy-ion collisions?**

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#### **Early Universe**



#### figure: NASA

#### **Cores of neutron stars**



figure: D.E. A. Castillo, talk @RagTime 22





### **Relativistic heavy-ion collisions - a tool to study QGP**



The study of QGP possible only indirectly through the energy and momenta of emitted particles





figure: Nature Physics 16, 615–619(2020)

### How do we probe the properties of QGP?



figure: K. Fukushima, D. E. Kharzeev, H. J. Warringa, Phys. Rev. Lett. 104, 212001

### **Anisotropies in momentum distributions** suggest strongly coupled QGP

figure: T. Hirano, N. van der Kolk, A.Bilandzic, Lect.Notes Phys. 785 (2010) 139-178



 $\frac{dN}{d\phi} = \frac{N}{2\pi} \left[ 1 + 2\mathbf{v_1}\cos(\phi) + 2\mathbf{v_2}\cos(2\phi) + \dots \right]$ 



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### **QGP** is a <u>nearly</u> perfect fluid



**Extremely small viscosity is observed** 







### **QGP** precision studies era - new observables are welcome!



J. Bernhard, J. Moreland, S. Bass, *Nat. Phys.* **15**, 1113–1117 (2019)

### With the development of Bayesian analyses we are entering the precision studies era



#### **Can we find new observables?**

## Magnetization — rotation coupling - possible new insights for HIC?

#### classical ↔ quantum angular momentum transition



#### Einstein-de-Haas effect, 1915 magnetization induces rotation

Einstein A, de Haas WJ. K. Ned. Akad.Wet. Proc. Ser. B Phys. Sci. 18:696 (1915)



figure: Matsuo M, leda J and Maekawa S (2015) Front. Phys. 3:54.

### Barnett effect, 1915: rotation induces magnetization

Barnett SJ. Phys. Rev. 6:239 (1915)

### Spin polarization in heavy-ion collisions - new sensitive probe!

$$oldsymbol{L}_{
m init}~\sim 10^5 oldsymbol{\hbar}$$

# Part of the angular momentum can be

$$oldsymbol{J}_{ ext{init}} = oldsymbol{L}_{ ext{init}} = oldsymbol{L}_{ ext{final}} + oldsymbol{S}_{ ext{final}}$$



polarized along the system's angular momentum





### Spin current generation from a fluid rotation



Takahashi, R., Matsuo, M., Ono, M. et al. Nature Phys 12, 52–56 (2016)

$$abla^2oldsymbol{\mu}^{\mathrm{s}} = rac{1}{\lambda^2}oldsymbol{\mu}^{\mathrm{s}} - rac{4e^2}{\sigma_0oldsymbol{\hbar}}oldsymbol{\xi}oldsymbol{\omega}$$

**Measurement of the** inverse spin Hall effect (ISHE) reveals the polarization in a flowing **Ihyquid Mercury** 



 $\mathbf{E}_{ ext{ISHE}} = -rac{2|e|}{2|e|}$  ,  $rac{1}{\sigma_0 \hbar} heta_{ ext{SHE.}}$  $\mathbf{\sigma} \times \boldsymbol{\sigma}$ 

## Measurement of $\Lambda$ and $\Lambda$ spin polarization in heavy-ion collisions

L. Adamczyk et al. (STAR) (2017), Nature 548 (2017) 62-65  $\overline{\mathcal{P}}_{\mathrm{H}} \left( \% \right)$ Au+Au 20-50%  $\bigstar$   $\Lambda$  this study •  $\overline{\Lambda}$  this study Λ PRC76 024915 (2007) 6 O A PRC76 024915 (2007) 4 S U B A T D W I C S W I R L S 2 PARIS AGREEMENT SUMMER SELECTION  $10^{2}$ 10 √s<sub>NN</sub> (GeV)

... the hottest, least viscous – and now, most vortical – fluid produced in the laboratory . . .  $\omega = (P_\Lambda + P_{ar{\Lambda}}) k_B T / \hbar \sim 0.6 - 2.7 imes 10^{22} ext{ s}^{-1}$  $P_{\Lambda} \approx \frac{1}{2} \frac{\omega}{T} + \frac{\mu_{\Lambda}B}{T} \qquad P_{\overline{\Lambda}} \approx \frac{1}{2} \frac{\omega}{T} - \frac{\mu_{\Lambda}B}{T}$ 



figure: T.Niida









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## How the spin is polarized in a rotating system?

#### polarization via spin-orbit coupling (perturbative QCD-inspired model)

Liang ZT, Wang XN. Phys. Rev. Lett. 94:102301 (2005). Gao JH, et al. Phys. Rev. C 77:044902 (2008)

Betz B, Gyulassy M, Torrieri G. Phys. Rev. C 76:044901 (2007) Becattini F, Piccinini F, et al. J. Phys. G 35:054001 (2008)



 $H = H_0 - \boldsymbol{\omega} \cdot \boldsymbol{S}$ 



### Spin polarization in equilibrated QGP - spin-thermal approach

### In local thermodynamic equilibrium at $\mathcal{O}((\varpi^{\mu\nu})^2)$ one can establish a link between spin and thermal vorticity

Becattini F, Piccinini F. Ann. Phys. 323:2452 (2008) Becattini F, Chandra V, Del Zanna L, Grossi E. Ann. Phys. 338:32 (2013) Fang R, Pang L, Wang Q, Wang X. Phys. Rev. C 94:024904 (2016)

$$S^{\mu}(p) = -\frac{1}{8m} e^{\mu\rho\sigma\tau} p_{\tau} \frac{\int d\Sigma_{\lambda} p^{\lambda} n_F \left(1 - n_F\right) (\overline{\varpi}_{\rho\sigma})}{\int d\Sigma_{\lambda} p^{\lambda} n_F}$$
$$\overline{\varpi}_{\mu\nu} = -\frac{1}{2} \left(\partial_{\mu} \beta_{\nu} - \partial_{\nu} \beta_{\mu}\right) \qquad \beta^{\mu} = \frac{u^{\mu}}{T}$$

 $n_F = (1 + \exp[\beta \cdot p - \mu Q/T])^{-1}$ 

Allows to extract polarisation at the freeze-out hypersurface in <u>any</u> model which provides  $u^{\mu}$ , T and  $\mu$ 



### **Global polarization data supports the** spin-thermal approach

### Signal is pretty robust and agrees for both multiphase transport model (AMPT) and viscous hydrodynamics (UrQMD+vHLLE)

#### **Azimuthal modulation is not captured**







### **Global polarization**

J. Adam, et al., Phys. Rev. C 98, 014910 (2018)



### Local (momentum-differential) polarization



Flow structure in the transverse plane (jet, ebe fluctuations etc.) may generate **longitudinal polarization** 

F. Becattini and I. Karpenko, PRL120.012302 (2018) S. Voloshin, EPJ Web Conf.171, 07002 (2018)

$$\frac{dN}{d\Omega^*} = \frac{1}{4\pi} (1 + \alpha_{\rm H} \mathbf{P}_{\mathbf{H}} \cdot \mathbf{p}_p^*)$$

$$\frac{dN}{d\Omega^*} = \frac{1}{4\pi} (1 + \alpha_{\rm H} \mathbf{P}_{\mathbf{H}} \cdot \mathbf{p}_p^*)$$

$$\langle \cos \theta_p^* \rangle = \int \frac{dN}{d\Omega^*} \cos \theta_p^* d\Omega^*$$

$$= \alpha_{\rm H} P_z \langle (\cos \theta_p^*)^2 \rangle$$

$$\therefore P_z = \frac{\langle \cos \theta_p^* \rangle}{\alpha_{\rm H} \langle (\cos \theta_p^*)^2 \rangle}$$

$$= \frac{3 \langle \cos \theta_p^* \rangle}{\alpha_{\rm H}} \quad \text{(if perfect detector)}$$

 $\theta_{p}^{*}$ :  $\theta$  of daughter proton in  $\Lambda$  rest frame

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### Local (momentum-differential) polarization



T. Niida, NPA 982 (2019) 511514



#### thermal model with projected vorticity $\omega_{\mu\nu} = \overline{\varpi}_{\alpha\beta} \overline{\Delta}^{\alpha}_{\mu} \overline{\Delta}^{\beta}_{\nu}$

W.Florkowski, A. Kumar, A. Mazeliauskas, R.R., [1904.00002]



**3D VH + AMPT IC with** *T*-vorticity  $\omega_{\mu\nu}^{(T)} = -\frac{1}{2} \left[ \partial_{\mu} (Tu_{\nu}) - \partial_{\nu} (Tu_{\mu}) \right]$ H-Z Wu, L-G Pang, X-G Huang, Q. Wang [1906.09385]





### Local (momentum-differential) polarization



T. Niida, NPA 982 (2019) 511514







### **Global polarization at low beam energies**



Credit: F. Kornas, International Workshop XLVII on Gross Properties of Nuclei and Nuclear Excitations, 2019



0.12

#### there seems to be a threshold effect at very low energies

Au+Au → b=5.0 fm 0.1 ← b=8.0 fm  $\left< - \omega_y \right> (\text{fm}^{-1})$ 0.08 -**▼**- b=10.0 fm 0.06 0.04 0.02 20 30 40 3 4 5 6 7 10 2 ∖s<sub>NN</sub> (GeV)



## How to describe dynamics of spin?

### **Spin-thermal approach does not capture** differential observables

Is spin polarization always enslaved to thermal vorticity?

**Non-trivial space-time dynamics of spin?** 





### **Relativistic fluid dynamics forms** the basis of HIC models



### Fluid dynamics with spin?

Most of the time close to equilibrium but the dissipation is also important



## **Spinless relativistic fluid dynamics - basics**

Ideal fluid dynamics = local equilibrium + conservation laws



**Caution: Eckart-Landau theory is acausal!** 

- For particles with spin the conservation of angular momentum implies introduction of new hydrodynamic (polarization) variables
- Fluid dynamics with spin should tell how the polarisation variables evolve but not their origin!

## **Conservation of angular momentum and spin chemical potential**

Noether's theorem: for each continuous symmetry of the action there is a corresponding conserved (canonical) current **Conservation of charge (baryon number, electric charge, ...)** 

**Conservation of energy and momentum** 

 $\widehat{J}_{C}^{\mu,\alpha\beta}(x) = x^{\alpha} \widehat{T}_{C}^{\mu\beta}(x) - x^{\beta} \widehat{T}_{C}^{\mu\alpha}(x) + \widehat{S}_{C}^{\mu,\alpha\beta}(x)$ 

 $\widehat{L}_{C}^{\mu,\alpha\beta}(x)$ 

 $\partial_{\mu}\widehat{T}_{C}^{\mu\alpha}(x)=0$ 

**Conservation of total angular momentum** 





 $\partial_{\mu} \widehat{N}^{\mu}(x) = 0$  (1 equation/charge)



(4 equations)

 $T, u^{\nu}$ 

W. Florkowski, B. Friman, A. Jaiswal, E. Speranza, Phys. Rev. C97 (4) (2018) 041901 W. Florkowski, B. Friman, A. Jaiswal, R. R., E. Speranza, PRD 97 (2018) 116017 F.Becattini, W. Florkowski, E. Speranza, PLB 789 (2019) 419-425

$$\partial_{\mu}\widehat{S}_{C}^{\mu,\alpha\beta}(x) = \widehat{T}_{C}^{\beta\alpha}(x) - \widehat{T}_{C}^{\alpha\beta}(x)$$



### Pseudogauges and the problem of energy and spin localization

#### **Pseudo-gauge transformation**

W. Hehl, Rept. Math. Phys. 9 (1976) 55-82; F. Becattini, L. Tinti, PRD 84 (2011) 025013; PRD 87(2) (2013) 025029

$$\widehat{T}'^{\mu\nu} = \widehat{T}^{\mu\nu} + \frac{1}{2}\partial_{\lambda}\left(\widehat{\Phi}^{\lambda,\mu\nu} - \widehat{\Phi}^{\mu,\lambda\nu} - \widehat{\Phi}^{\nu,\lambda\mu}\right)$$

$$\widehat{S}'^{\lambda,\mu\nu} = \widehat{S}^{\lambda,\mu\nu} - \widehat{\Phi}^{\lambda,\mu\nu}$$

$$\sim \text{ preserve } \widehat{P}^{\mu} = \int d^{3}\Sigma_{\lambda} \widehat{T}^{\lambda\mu}(x) \qquad \widehat{J}^{\mu\nu} = \int d^{3}\Sigma_{\lambda} \widehat{J}^{\lambda,\mu\nu}(x)$$

$$\sim \text{ conservation laws unchanged}$$

**Belinfante-Rosenfeld pseudo-gauge** (choosing superpotential  $\widehat{\Phi} = \widehat{S}_{C}^{\lambda,\mu\nu}$ ) Belinfante, F. J. (1939): Physica 6. 887-898, (1940); Rosenfeld, L. (1940): Mem. Acad. Roy. Belgique, cl. SC., tome 18, fasc. 6

$$\widehat{T}_{B}^{\mu\nu} = \widehat{T}_{C}^{\mu\nu} + \frac{1}{2} \partial_{\lambda} \left( \widehat{S}_{C}^{\lambda,\mu\nu} + \widehat{S}_{C}^{\mu,\nu\lambda} - \widehat{S}_{C}^{\nu,\lambda\mu} \right) \qquad \widehat{S}_{B}^{\lambda,\mu\nu} = 0$$

- $\rightarrow$  gives exactly symmetric Hilbert  $T^{\mu\nu}$  acting as the source of gravity in GR
- $\rightarrow$  long-standing problem of physical significance of the spin tensor
- $\rightarrow$  spin tensor is used by the community that studies the spin of proton X.S. Chen, X.F. Lu, W.M. Sun, F. Wang, T. Goldman, PRL 100 (2008) 232002; E. Leader, C. Lorce, Phys. Rep. 541 (2014) 163.



### Ideal fluid dynamics with spin

Prog. Part. Nucl. Phys. 108 (2019) 103709

$$\partial_{\mu}T^{\mu\nu} = 0, \quad \partial_{\lambda}S^{\lambda,\mu\nu} = 0, \quad \partial_{\mu}N^{\mu} = 0$$

$$T^{\mu\nu} = T^{\mu\nu}[\beta, \omega, \xi], \quad S^{\mu, \lambda\nu} =$$

If the <u>energy-momentum tensor is symmetric</u> the hydrodynamics with spin is given by

What are the constitutive relations which enter equations of motion?

 $= S^{\mu,\lambda\nu}[\beta,\omega,\xi], \quad N^{\mu} = N^{\mu}[\beta,\omega,\xi]$ 

### **Relativistic kinetic theory formulation of ideal fluid equations**

For dilute systems, the derivation of fluid dynamics can be done starting from the underlying kinetic theory

classical **RKT** 

 $p^{\mu}\partial_{\mu}f(x,p) = C[f(x,p)]$ 

quantum RKT

semi-classical expansion

$$\left( \gamma_{\mu} K^{\mu} - m \right) \mathscr{W}(x,k) = C[\mathscr{W}(x,k)]$$

$$K^{\mu} = k^{\mu} + \frac{i}{2} \left( \hbar \partial^{\mu} \right)$$



 $k^{\mu}\partial_{\mu}\mathscr{A}^{\nu}_{\mathrm{eq}}(x,k) = 0$ 

 $\partial_{\mu}T^{\mu\nu} = 0$  $\partial_{\lambda}S^{\lambda,\mu\nu} = 0$ 

### Local equilibrium distributions

#### System without spin

$$f^{\pm} = \exp\left[\pm\xi(x) - \beta_{\mu}(x)p^{\mu}\right]$$



De Groot, van Leeuwen, van Weert: Relativistic Kinetic Theory. Principles an W. Florkowski, A. Kumar, R. R., PRC 98 (2018) 044906

$$egin{aligned} \mathcal{W}^+_{ ext{eq}}(x,k) &= rac{1}{2} \sum_{r,s=1}^2 \int dP \delta^{(4)}(k-p) u^r(p) ar{u}^s(p) f^+_{rs}(x,p) \ \mathcal{W}^-_{ ext{eq}}(x,k) &= -rac{1}{2} \sum_{r,s=1}^2 \int dP \delta^{(4)}(k+p) v^s(p) ar{v}^r(p) f^-_{rs}(x,p) \ \mathcal{W}_{ ext{eq}}(x,k) &= \mathcal{W}^+_{ ext{eq}}(x,k) + \mathcal{W}^-_{ ext{eq}}(x,k) \end{aligned}$$

#### System with spin

F. Becattini, V. Chandra, L. Del Zanna, E. Grossi, Annals Phys. 338 (2013) 32 W. Florkowski, B. Friman, A. Jaiswal, E. Speranza, PRC 97 (4) (2018) 041901 W. Florkowski, B. Friman, A. Jaiswal, R. R., E. Speranza, PRD 97 (11) (2018) 116017

$$f_{rs}^{+}(x,p) = \frac{1}{2m} \bar{u}_{r}(p) X^{+} u_{s}(p) \qquad \text{This is}$$

$$f_{rs}^{-}(x,p) = -\frac{1}{2m} \bar{v}_{r}(p) X^{-} v_{r}(p) \qquad \text{vortion}$$

$$X^{\pm} = \exp\left[\pm \xi(x) - \beta_{\mu}(x) p^{\mu} \pm \frac{1}{2} \omega_{\mu\nu}(x) \Sigma^{\mu\nu}\right]$$

$$\hat{\Sigma}^{\mu\nu} = (i/4)$$

 $T_{\rm eq}^{\beta\alpha}(x) = T_{\rm eq}^{\alpha\beta}(x)$ 

**Spin is conserved separately!** 





## **Classical approach to spin hydrodynamics**

In the classical treatments of particles with spin-1/2 one introduces internal angular momentum tensor of particles [M. Mathisson, APPB 6 (1937) 163-2900]

$$s^{lphaeta} = rac{1}{m} \epsilon^{lphaeta\gamma\delta} p_{\gamma} s_{\delta}.$$

 $s^{\alpha\beta}$  is antisymmetric *i.e.*  $s^{\alpha\beta} = -s^{\beta\alpha}$  and satisfies Frenkel (or Weyssenhoff)  $\mathcal{D}_{\alpha} s^{\alpha\beta} = 0.$ 

The spin four vector can be obtained by above equation,

$$s^{lpha} = rac{1}{2m} \epsilon^{lphaeta\gamma\delta} p_{eta} s_{\gamma\delta}$$

In particle rest frame (PRF) where  $p^{\mu} = (m, 0, 0, 0)$ ,  $s^{\alpha} = (0, \mathbf{s}_*)$  with the length of spin vector given by  $-s^2 = -s^{\alpha}s_{\alpha} = |\mathbf{s}_*|^2 = \hat{\mathbf{s}}^2 = \frac{1}{2}(1 + \frac{1}{2}) = \frac{3}{4}$ .







## **Classical approach to spin hydrodynamics - perfect fluid**

W. Florkowski, R. R., A. Kumar, Prog. Part. Nucl. Phys. 108 (2019) 103709 ; J.-W. Chen, J.-y. Pang, S. Pu, Q. Wang, PRD 89 (9) (2014) 094003

$$f_{\rm eq}^{\pm}(x,p,s) = \exp\left(-p \cdot \beta(x) \pm \xi(x) + \frac{1}{2}\omega_{\alpha}\right)$$

$$\int dS \dots = \frac{m}{\pi \mathfrak{B}} \int d^4s \, \delta(s \cdot s + \mathfrak{B}^2) \, \delta(p \cdot s) \dots$$

$$N_{\rm eq}^{\mu} = \int dP \int dS \ p^{\mu} \left[ f_{\rm eq}^{+}(x,p,s) - f_{\rm eq}^{-}(x,p,s) \right]$$
$$T_{\rm eq}^{\mu\nu} = \int dP \int dS \ p^{\mu}p^{\nu} \left[ f_{\rm eq}^{+}(x,p,s) + f_{\rm eq}^{-}(x,p,s) \right]$$
$$S_{\rm eq}^{\lambda\mu\nu} = \int dP \int dS \ p^{\lambda} s^{\mu\nu} \left[ f_{\rm eq}^{+}(x,p,s) + f_{\rm eq}^{-}(x,p,s) \right]$$

For  $|\omega_{\mu\nu}| < 1$  one obtains the formalism that agrees with that based on the quantum description of spin (in the GLW version).



### **Classical approach to spin hydrodynamics - dissipation**

#### Use the relaxation time approximation for the collision terms in the classical kinetic equations

[S. Bhadury, W. Florkowski, A. Jaiswal, A. Kumar, R. R., Phys.Lett.B 814 (2021) 136096. Phys.Rev.D 103 (2021) 1. 014030

$$p^{\mu}\partial_{\mu}f^{\pm}_{s}(x,p,s) = C[f^{\pm}_{s}(x,p,s)]$$

# Simple Chapman-Enskog expansion of the single particle distribution function around its equilibrium value in powers of space-time gradients

$$\left| \delta f_{s}^{\pm} = -\frac{\tau_{\mathrm{eq}}}{(u \cdot p)} e^{\pm \xi - p \cdot \beta} \left[ \left( \pm p^{\mu} \partial_{\mu} \xi - p^{\lambda} p^{\mu} \partial_{\mu} \beta_{\lambda} \right) \left( 1 + \frac{1}{2} s^{\alpha \beta} \omega_{\alpha \beta} \right) + \frac{1}{2} p^{\mu} s^{\alpha \beta} (\partial_{\mu} \omega_{\alpha \beta}) \right] \right]$$

#### **Dissipative corrections**

$$\delta N^{\mu} = \int dP \, dS \, p^{\mu} (\delta f_{s}^{+} - \delta f_{s}^{-}),$$

$$\delta T^{\mu\nu} = \int dP \, dS \, p^{\mu} p^{\nu} (\delta f_{s}^{+} + \delta f_{s}^{-}),$$

$$\delta S^{\lambda,\mu\nu} = \int dP \, dS \, p^{\lambda} s^{\mu\nu} (\delta f_{s}^{+} + \delta f_{s}^{-}).$$

$$\delta N^{\mu} = \nu^{\mu} = \tau_{eq} \beta_{n} (\nabla^{\mu} \xi),$$

$$\delta T^{\mu\nu} = \pi^{\mu\nu} - \Delta^{\mu\nu} \Pi, \quad \pi^{\mu\nu} = 2\tau_{eq} \beta_{\pi} \sigma^{\mu\nu}, \quad \Pi = -\tau_{eq} \beta_{\Pi} \theta$$

$$\delta S^{\lambda,\mu\nu} = \tau_{eq} \Big[ B^{\lambda,\mu\nu}_{\Pi} \theta + B^{\kappa\lambda,\mu\nu}_{n} (\nabla_{\kappa} \xi) + B^{\alpha\kappa\lambda,\mu\nu}_{\pi} \sigma_{\alpha\kappa} + B^{\kappa\lambda\beta\alpha,\mu\nu}_{\Sigma} (\nabla_{\kappa} \xi) + B^{\alpha\kappa\lambda,\mu\nu}_{\pi} \sigma_{\alpha\kappa} + B^{\kappa\lambda\beta\alpha,\mu\nu}_{\Sigma} (\nabla_{\kappa} \xi) \Big]$$
There are non-equilibrium corrections to spin tensor

$$C[f_s^{\pm}(x,p,s)] = p \cdot u \frac{f_{s,eq}^{\pm}(x,p,s) - f_s^{\pm}(x,p,s)}{\tau_{eq}}$$



### Other developments towards hydrodynamics with spin

#### Lagrangian effective field theory approach

D. Montenegro, G. Torrieri, Phys.Rev. D94 (2016) no.6, 065042 D. Montenegro, L. Tinti, G. Torrieri, Phys. Rev. D 96(5) (2017) 056012; Phys. Rev. D 96(7) (2017) 076016 D. Montenegro, G. Torrieri, Phys. Rev. D 100, 056011 (2019)

#### Hydrodynamics with spin based on entropy-current analysis

K. Hattori, M. Hongo, X-G Huang, M. Matsuo, H. Taya, PLB 795 (2019) 100-106

#### Hydrodynamics of spin currents using presence of torsion

D. Gallegos, U. Gursoy, A. Yarom arXiv:2101.04759

#### **Relativistic viscous hydrodynamics with spin using Navier-Stokes type gradient expansion analysis**

D. She, A. Huang, D. Hou, J. Liao, arXiv:2105.04060

#### **Relativistic viscous spin hydrodynamics from chiral kinetic theory**

S. Shi, C. Gale, and S. Jeon, Phys. Rev. C 103, 044906 (2021)

#### Spin polarization generation from vorticity through nonlocal collisions

N. Weickgenannt, E. Speranza, X.-I. Sheng, Q. Wang, and D. H. Rischke, arXiv:2005.01506, arXiv:2103.04896

#### **Spin polarisation due to thermal shear**

F. Becattini, M. Buzzegoli, and A. Palermo, arXiv:2103.10917 S. Y. F. Liu and Y. Yin, arXiv:2103.09200 28



- The spin polarization provides a new probe of the QGP properties
  - The disagreements between spin-thermal approach and data motivates developments of dynamical models
- The fluid dynamics with spin is a natural framework one should seek for QGP
  - **Presented ideal spin hydro formulation is readily applicable** 
    - The theory is developing fast future looks interesting!

### Thank you for your attention!