



Learning for Monitoring and Control in Power Distribution Grids

Vassilis Kekatos (kekatos@vt.edu)

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Acknowledgements

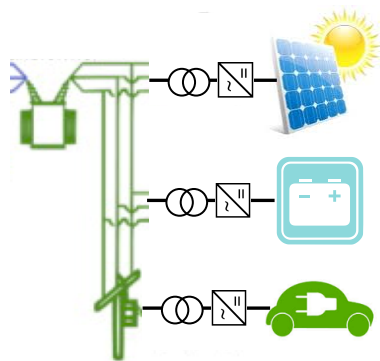
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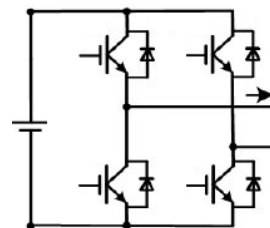
Learning in distribution grids

- Reduced observability due to sheer extent and limited real-time metering
- However, load estimates and topology information needed for grid optimization and control



- Smart inverters interfacing new technologies

- Adding a third functionality to smart inverters
 1. *energy conversion*
 2. *grid control*
 3. *grid monitoring*



Inverter Probing for Learning Distribution Grids



Guido Cavraro
[now with NREL]



Sid Bhela
[now with
Siemens]



Sina
Taheri

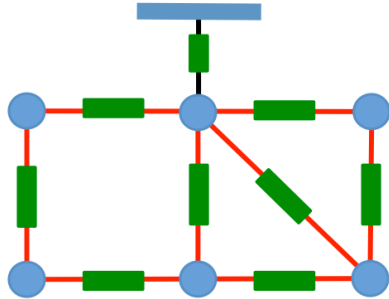


Manish
Singh



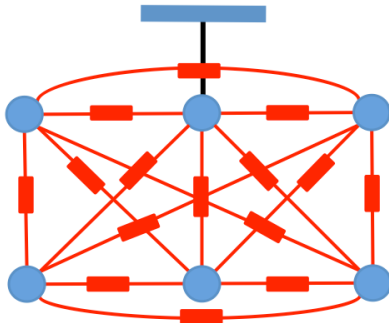
Harsha
Veeramachaneni
Next Era Analytics

Grid topology learning



topology detection

- Given data and existing line infrastructure, find which lines are energized



topology identification

- Given data alone, find grid topology and line impedances

Prior work

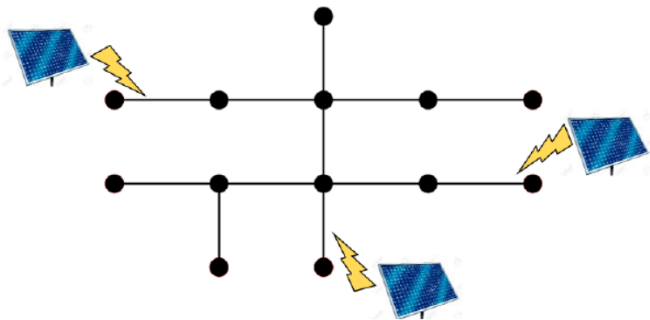
Passive data collection

- Voltage covariance [Bolognani'13], [Deka-Backhaus-Chertkov'15], [Li-Scaglione-Poor'15]
- Graphical models and DNN [Weng-Liao-Rajagopal'17], [Sevlian-Rajagopal'17], [Zhao-Poor'17]
- Micro-PMU data [Ardakanian et al'18]

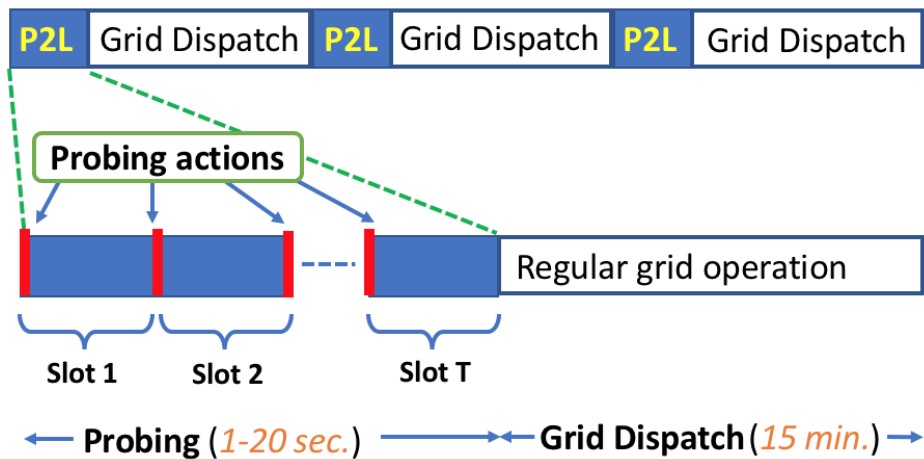
Grid perturbation for active data collection

- Oscillation modes in transmission grid dynamics [Trudnowski-Pierre'09]
- Identification of DC microgrids [Angelichinoski-Scaglione '16]
- Thevenin impedance for single inverter [Jaksic-Boroyevich-Burgos '17]

Grid probing using inverters

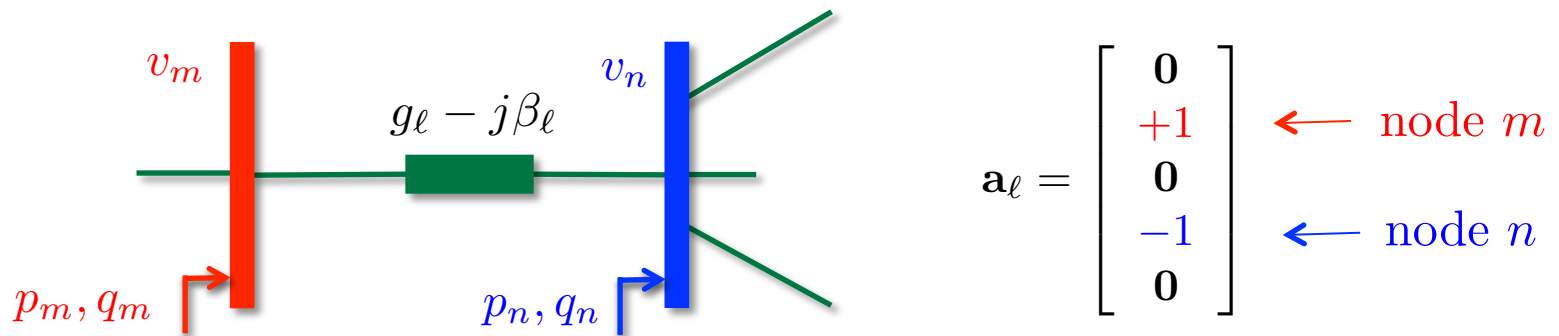


- Perturb power injections at probing buses [how?]
- Collect grid voltage response (magnitudes, phasors)
- Repeat over T probing actions spaced 1-2' apart



Approximate grid model

- Single-phase *radial* grid with $N+1$ nodes and N lines



- Linear distribution flow (LDF) model [Baran-Wu'89], [Deka et al'17]

$$\mathbf{v} \simeq \mathbf{R}\mathbf{p} + \mathbf{X}\mathbf{q} + \mathbf{1}_N$$

inverse graph $\mathbf{L} = \mathbf{A}^\top \text{dg}(\mathbf{g})\mathbf{A}$
Laplacian $\mathbf{R} = \mathbf{L}^{-1}$

- Differential quantities $\tilde{\mathbf{v}}_t = \mathbf{R}\tilde{\mathbf{p}}_t + \mathbf{X}\tilde{\mathbf{q}}_t + \mathbf{n}_t$

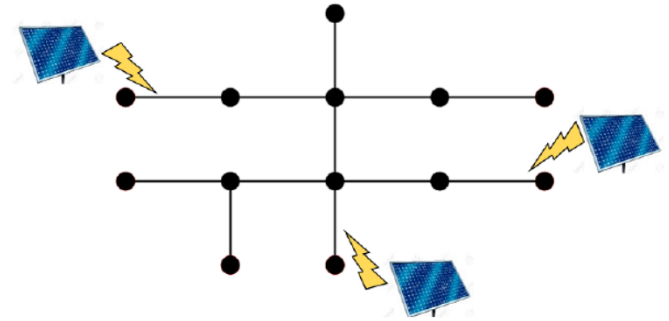
$$\tilde{\mathbf{p}}_t := \mathbf{p}_t - \mathbf{p}_{t-1}$$

- 1. modeling error
- 2. metering noise
- 3. unmodeled (load) variations

Probing for topology identification

- Active power probing ($\tilde{\mathbf{q}}_t = \mathbf{0}$)

$$\tilde{\mathbf{p}}_t = \begin{bmatrix} \tilde{\mathbf{p}}_{t,\mathcal{M}} \\ \tilde{\mathbf{p}}_{t,\mathcal{O}} \end{bmatrix} = \begin{bmatrix} \text{known} \\ \mathbf{0} \end{bmatrix} \quad \begin{array}{l} \text{probed buses } \mathcal{M} \\ \text{unchanged loads } \mathcal{O} \end{array}$$



- Probe grid over $T \geq |\mathcal{M}|$ periods and ignore noise

$$\tilde{\mathbf{v}}_t = \mathbf{R}\tilde{\mathbf{p}}_t + \mathbf{X}\tilde{\mathbf{q}}_t + \mathbf{n}_t \quad \longrightarrow \quad \tilde{\mathbf{V}} = \mathbf{R}\tilde{\mathbf{P}} = \mathbf{R} \begin{bmatrix} \tilde{\mathbf{P}}_{\mathcal{M}} \\ \mathbf{0} \end{bmatrix}$$

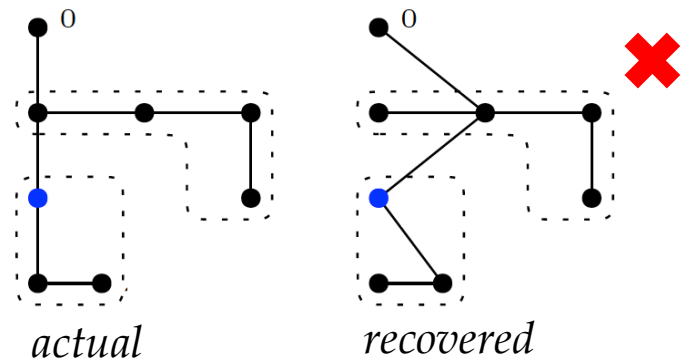
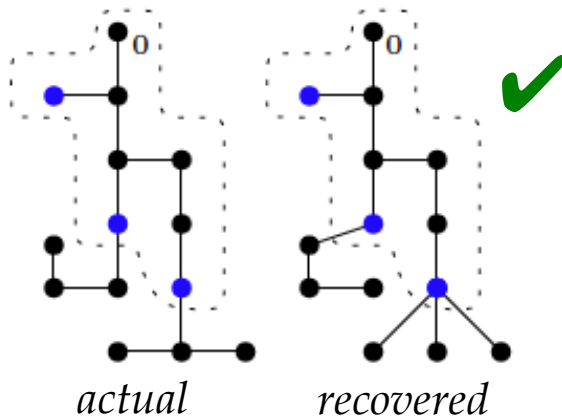
$$\mathbf{R} = \begin{bmatrix} \mathbf{R}_{\mathcal{M},\mathcal{M}} & \mathbf{R}_{\mathcal{O},\mathcal{M}}^\top \\ \mathbf{R}_{\mathcal{O},\mathcal{M}} & \mathbf{R}_{\mathcal{O},\mathcal{O}} \end{bmatrix}$$

matrix partition

- Complete data:* voltages collected at all buses, recover $\mathbf{R}_{\mathcal{M}} = \begin{bmatrix} \mathbf{R}_{\mathcal{M},\mathcal{M}} \\ \mathbf{R}_{\mathcal{O},\mathcal{M}} \end{bmatrix}$
- Partial data:* voltages collected only at probing buses, recover $\mathbf{R}_{\mathcal{M},\mathcal{M}}$

Topology identifiability

Theorem 1 (Complete data): Remove the descendants of probed buses. If you get a tree with all its leaves probed, this tree can be identified.

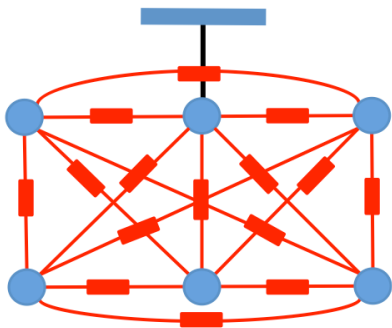
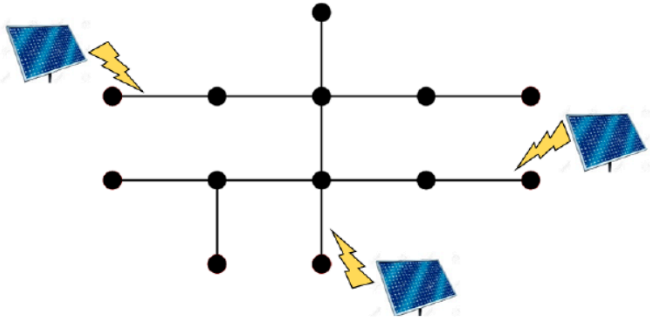


Corollary: If all leaf buses are probed, the entire grid topology can be identified.

Theorem 2 (Partial data): If all leaf nodes are probed, a reduced grid can be identified.

- Rich literature on recovering graphs; parallel results [Park-Deka-Chertkov'17]

From probing data to topology identification



- *Graph algorithms*

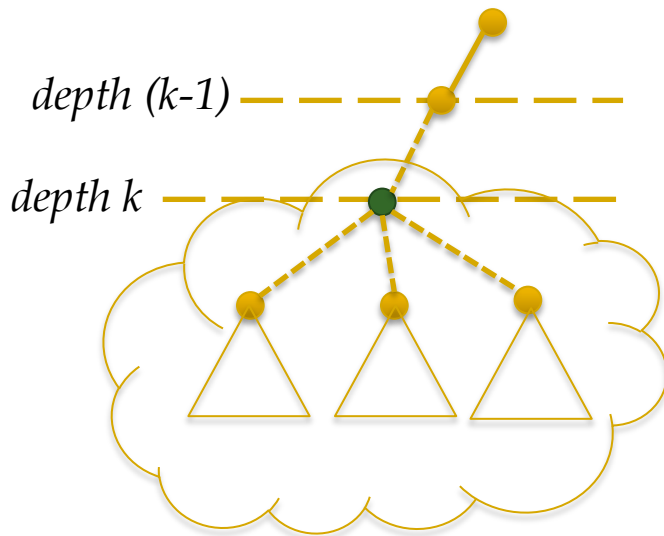
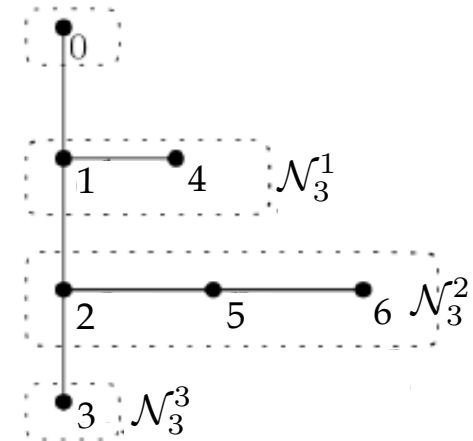
- *Convex relaxation*

- *Mixed-integer linear program (MILP) approach*

Root and Branch (R&B) algorithm

- Group entries of m -th column of $\mathbf{R}_{\mathcal{M}}$
- Buses grouped together comprise a *level set* \mathcal{N}_m^k

$$\mathbf{R}_{:,3} = \begin{bmatrix} 1 \\ 3 \\ 6 \\ 1 \\ 3 \\ 3 \end{bmatrix}$$



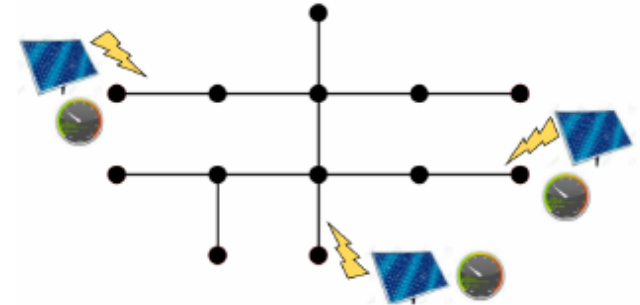
Recursive graph algorithm

- S1)** Find k -depth root as intersection of $\{\mathcal{N}_m^k\}$
- S2)** Connect k - to $(k-1)$ -depth root with resistance
- S3)** Group buses with identical \mathcal{N}_m^k and recurse

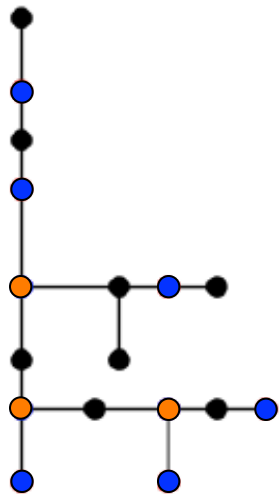
R&B with partial voltage data

- What if voltages are collected only at \mathcal{M} ?

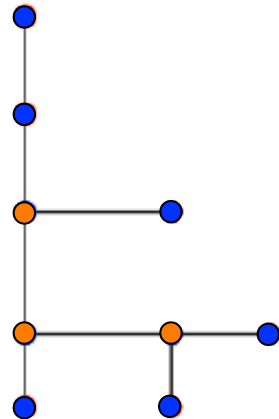
$$\tilde{\mathbf{V}}_{\mathcal{M}} = \mathbf{R}_{\mathcal{M}\mathcal{M}} \tilde{\mathbf{P}}_{\mathcal{M}} \quad \text{where} \quad \mathbf{R} = \begin{bmatrix} \mathbf{R}_{\mathcal{M},\mathcal{M}} & \mathbf{R}_{\mathcal{M},\mathcal{O}} \\ \mathbf{R}_{\mathcal{O},\mathcal{M}} & \mathbf{R}_{\mathcal{O},\mathcal{O}} \end{bmatrix}$$



- Level sets of probing nodes are *partially observed*



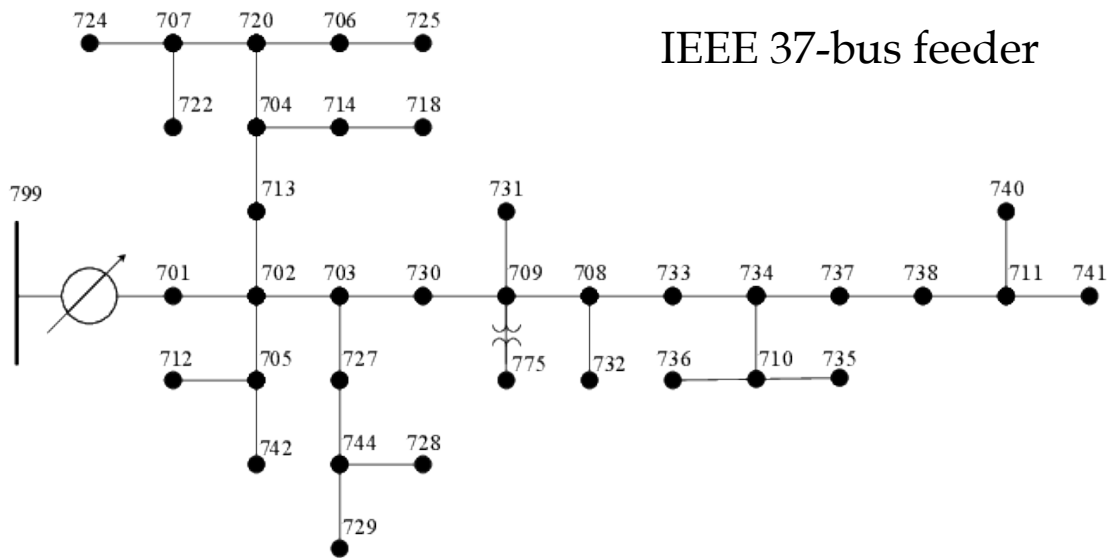
actual



recovered

- Modified R&B recovers a *reduced grid*
 - ✓ radial grid
 - ✓ recovers non-metered buses having two children each one with a probed descendant
 - ✓ correct pair-wise path resistances

Numerical tests



IEEE 37-bus feeder

Probability of Erroneous Topology

Complete voltage data

T_m	1	10	20	40	90
Error Prob. [%]	98.5	55.3	20.9	3.1	0.2

Partial voltage data

T_m	1	5	10	20	39
Error Prob. [%]	97.2	45.8	26.3	18.9	0.1

- Each inverter is probed T_m times to average out noise

Convex relaxation heuristic

- Graph algorithms rely on noiseless estimates of $\mathbf{R}_{\mathcal{M}}$ ($\mathbf{R}_{\mathcal{M},\mathcal{M}}$)
- For complete voltage data, invert probing data model

$$\tilde{\mathbf{V}} = \mathbf{R}\tilde{\mathbf{P}} + \mathbf{N} \quad \mathbf{L} = \mathbf{R}^{-1} \quad \longrightarrow \quad \tilde{\mathbf{P}} = \mathbf{L}\tilde{\mathbf{V}} + \mathbf{E}$$

- Topology identification via data fitting

$$\begin{array}{ll} \min_{\mathbf{L}} & \|\tilde{\mathbf{P}} - \mathbf{L}\tilde{\mathbf{V}}\|_F^2 \\ \text{s.to} & \mathbf{L} \succ \mathbf{0} \\ & L_{m,n} \leq 0, \quad \forall m \neq n \\ & \|\mathbf{L}\|_{0,\text{off}} = 2N \end{array} \quad \begin{array}{l} \text{convex} \\ \text{relaxation} \end{array} \quad \longrightarrow \quad \begin{array}{ll} \min_{\mathbf{L}} & \|\tilde{\mathbf{P}} - \mathbf{L}\tilde{\mathbf{V}}\|_F^2 + \lambda\|\mathbf{L}\|_1 - \mu \log |\mathbf{L}| \\ \text{s.to} & \mathbf{L} \succeq \mathbf{0} \\ & L_{m,n} \leq 0, \quad \forall m \neq n \end{array}$$

- Recover tree through heuristics (e.g., minimum spanning tree)

Topology detection vs. identification

- Similar formulation if Laplacian is parameterized in terms of lines

$$L(\mathbf{b}) = \sum_{\ell \in \mathcal{L}} \frac{b_\ell}{r_\ell} \mathbf{a}_\ell \mathbf{a}_\ell^\top \quad \text{where } b_\ell = \begin{cases} 1 & , \text{ line } \ell \text{ is energized} \\ 0 & , \text{ otherwise} \end{cases}$$

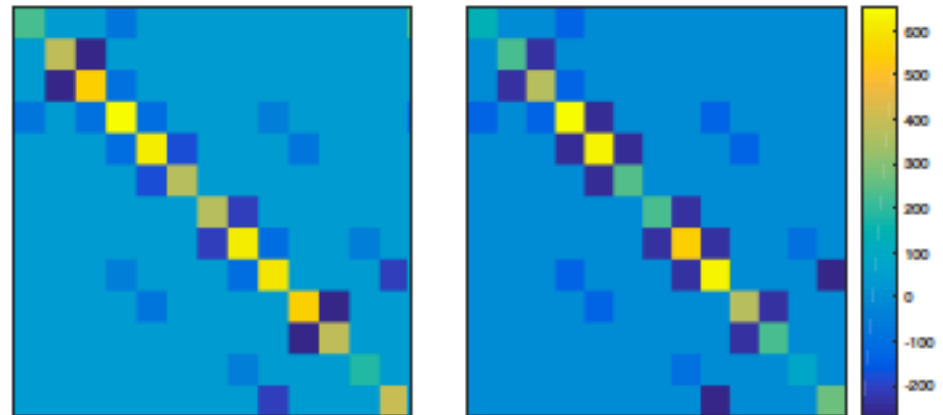
- Topology detection through data fitting

$$\begin{array}{ccc} \min_{\mathbf{b}} & \|\tilde{\mathbf{P}} - \mathbf{L}(\mathbf{b})\tilde{\mathbf{V}}\|_F^2 & \xrightarrow{\text{convex relaxation}} & \min_{\mathbf{b}} & \|\tilde{\mathbf{P}} - \mathbf{L}(\mathbf{b})\tilde{\mathbf{V}}\|_F^2 - \mu \log |\mathbf{L}(\mathbf{b})| \\ \text{s.to} & \mathbf{b} \in \{0, 1\}^{\bar{L}} & \longrightarrow & \text{s.to} & \mathbf{b} \in [0, 1]^{\bar{L}} \\ & \mathbf{b}^\top \mathbf{1} = N & & & \mathbf{b}^\top \mathbf{1} = N \\ & \mathbf{L}(\mathbf{b}) \succ \mathbf{0} & & & \end{array}$$

- Related formulations with covariance matrices for smart meter data analytics

Numerical tests

- Resistive Laplacian matrix for *IEEE 13-bus feeder*



actual

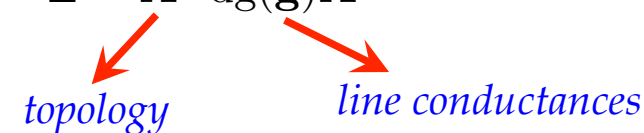
recovered

- Identification/detection results for *IEEE 37-bus feeder*

AVERAGE NUMBER OF LINE STATUS ERRORS FOR THE 37-BUS FEEDER

	$T = 1$	$T = 2$	$T = 5$	$T = 10$
Identification task of (22)	5.07	3.92	3.73	2.69
Verification task of (32)	0.32	0.21	0.08	0.01

Exact model fitting

- Recall grid Laplacian $\mathbf{L} = \mathbf{A}^\top \text{dg}(\mathbf{g})\mathbf{A}$


- Vectorize probing data model

$$\tilde{\mathbf{P}} = \mathbf{L}\tilde{\mathbf{V}} + \mathbf{E} \quad \longrightarrow \quad \mathbf{p} = \mathbf{H}\mathbf{g} + \mathbf{e} \quad \text{where} \quad \mathbf{H} = \tilde{\mathbf{V}}^\top \mathbf{A}^\top \star \mathbf{A}^\top \quad \textit{Khatri-Rao product}$$

- Pretending topology \mathbf{A} is known, find conductances \mathbf{g} through LS fit
- Optimal \mathbf{g}_{LS} provides LS fit error $f(\mathbf{A}) = -\mathbf{p}^\top \mathbf{H} (\mathbf{H}^\top \mathbf{H})^{-1} \mathbf{H}^\top \mathbf{p}$
- Find topology \mathbf{A} attaining smallest LS fit $f(\mathbf{A})$

Topology identification

selection matrix

- Select from candidate lines $\mathbf{A} = \mathbf{S}\bar{\mathbf{A}}$ $\mathbf{S}\mathbf{S}^\top = \mathbf{I}_N$, $\mathbf{S}^\top\mathbf{S} = \text{dg}(\mathbf{b})$

- Reformulate LS fit $f(\mathbf{b}) = \bar{\mathbf{p}}^\top \text{dg}(\mathbf{b})\bar{\mathbf{p}} + \underbrace{\bar{\mathbf{p}}^\top \text{dg}(\mathbf{b}) (\mathbf{C} - \text{dg}(\mathbf{b}))^{-1} \text{dg}(\mathbf{b})\bar{\mathbf{p}}}_{\mathbf{z}}$
- Solve problem

$$\begin{aligned} \min_{\mathbf{z}, \mathbf{b} \in \{0,1\}^{\bar{L} \times 1}} \quad & f'(\mathbf{b}, \mathbf{z}) = \bar{\mathbf{p}}^\top \text{dg}(\mathbf{b})\bar{\mathbf{p}} + \bar{\mathbf{p}}^\top \text{dg}(\mathbf{b})\mathbf{z} \\ \text{s.to} \quad & (\mathbf{C} - \text{dg}(\mathbf{b}))\mathbf{z} = \text{dg}(\mathbf{b})\bar{\mathbf{p}} \\ & \mathbf{1}_{\bar{L}}^\top \mathbf{b} = N \\ & |\bar{\mathbf{A}}|^\top \mathbf{b} \geq \mathbf{1}_{N+1} \end{aligned}$$

*every bus connected
to at least one line*

- Products handled by *McCormick linearization* to yield MILP
- *Caveat:* If $(\mathbf{C} - \text{dg}(\mathbf{b}^*))$ is *singular*, the relaxation is *not exact!*

Ensuring connectivity

Lemma: Matrix $(\mathbf{C} - \text{dg}(\mathbf{b}^*))$ is invertible iff $\mathbf{A} = \mathbf{S}\bar{\mathbf{A}}$ yields a connected grid

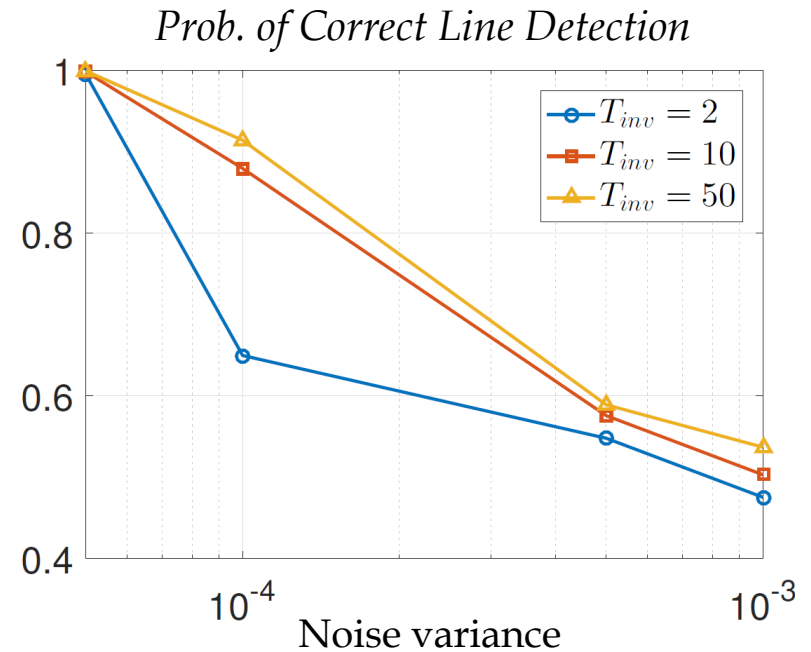
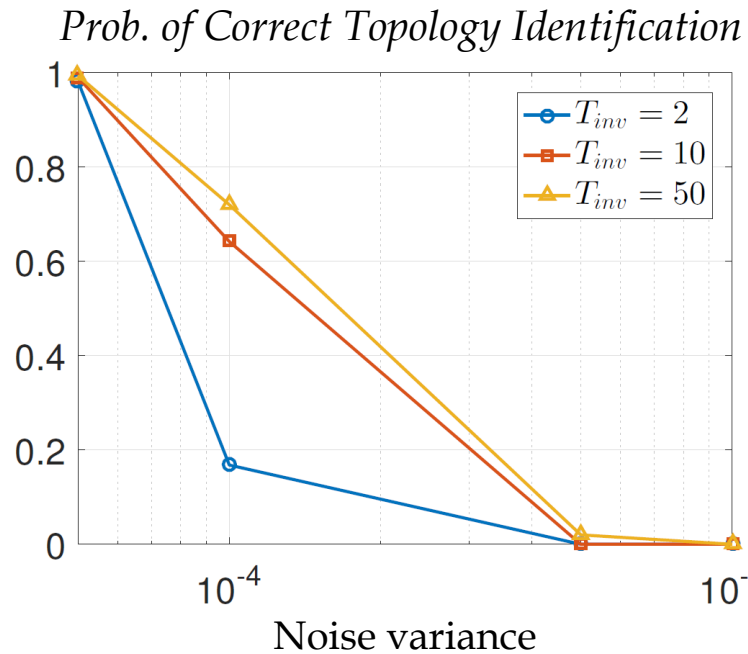
- *Key question:* How to guarantee a connected topology?
- Introduce optimization vector of *virtual* line flows $\mathbf{f} \in \mathbb{R}^L$

add these constraints to previous formulation

$$\begin{aligned}\bar{\mathbf{A}}^\top \mathbf{f} &= \mathbf{1} \\ -N\mathbf{b} &\leq \mathbf{f} \leq N\mathbf{b}\end{aligned}$$

- *Intuition:* find topology that can deliver 1 pu injected at each bus and N pu received by substation
- Comparison to formulation of [Lei-Chen-Song-Hou'19]

Numerical tests

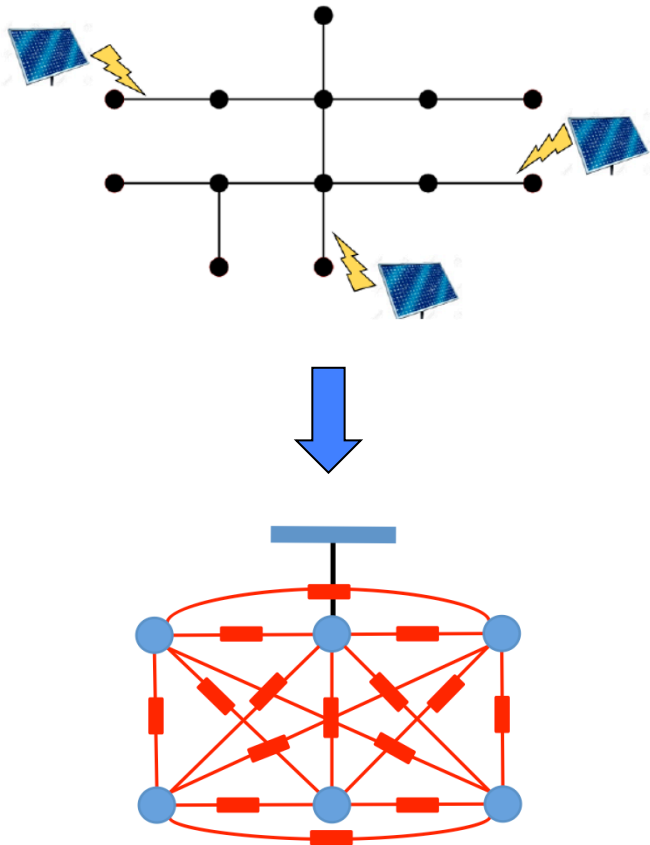


- Each inverter probed T times to average out noise

RUNNING TIME FOR MILPs [SEC]

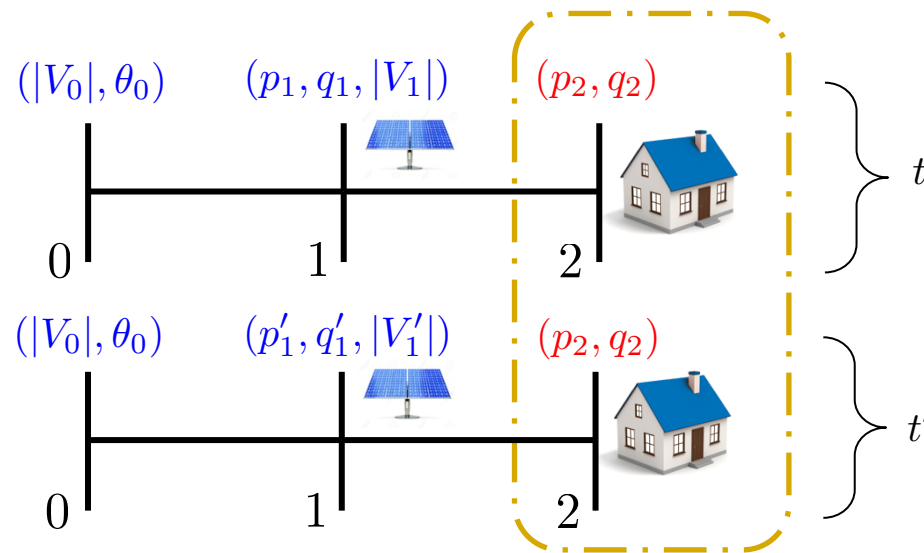
# of candidate lines \bar{L}	24	36	48
MILP formulation	1	27	200

Topology identification algorithms



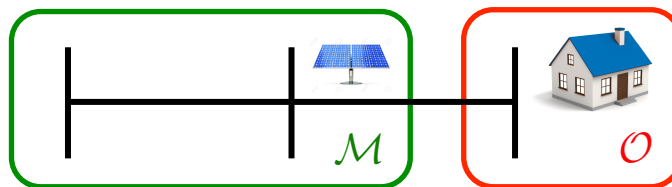
- *Graph algorithms*
 - complete or partial voltage data
 - exact for noiseless data
- *Convex relaxation*
 - complete voltage data
 - noisy data but heuristic
- *Mixed-integer linear program (MILP) approach*
 - complete voltage data
 - computationally more demanding yet exact

Probing for learning loads



Coupled power flow (CPF) problem

Problem statement: Given inverter data on metered buses \mathcal{M} and assuming time-invariant injections at buses \mathcal{O} , find states $\{\mathbf{v}_t\}_{t=1}^T$ and non-metered loads on \mathcal{O}



probing (metered) buses non-metered buses

$$\left. \begin{aligned} p_n(\mathbf{v}_t) &= \hat{p}_n^t & \forall n \in \mathcal{M} \\ q_n(\mathbf{v}_t) &= \hat{q}_n^t & \forall n \in \mathcal{M} \\ u_n(\mathbf{v}_t) &= \hat{u}_n^t & \forall n \in \mathcal{M} \end{aligned} \right\} 3MT$$

$$\left. \begin{aligned} p_n(\mathbf{v}_t) &= p_n(\mathbf{v}_{t+1}) & \forall n \in \mathcal{O} \\ q_n(\mathbf{v}_t) &= q_n(\mathbf{v}_{t+1}) & \forall n \in \mathcal{O} \end{aligned} \right\} 2O(T-1)$$

- Counting equations and unknowns yields $|\mathcal{M}| \geq \frac{2|\mathcal{O}|}{T}$

Q1) Can non-metered loads be recovered by probing T slots?

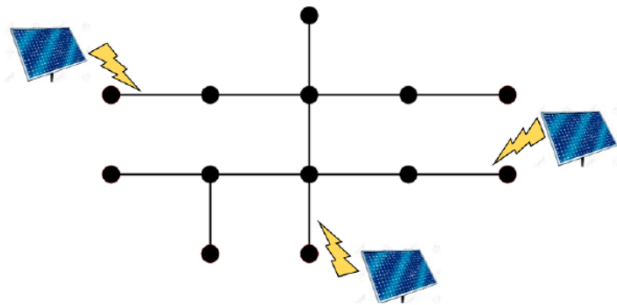
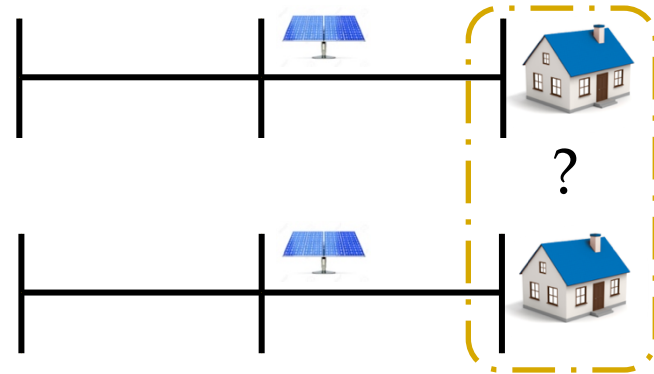
Q2) How to optimally design probing actions?

Q3) How to solve the CPF problem?

Conclusions

Take-home: *Inverter probing as active data collection paradigm for grid learning*

- ✓ identifiability
- ✓ topology ID algorithms
- ✓ probing for load learning



- multiphase configurations
- partial and noisy data
- 'probing' by regulators/capacitors

Kernel-Based Learning for Smart Inverter Control



Mana Jalali



Aditie Garg
[now with EPRI]

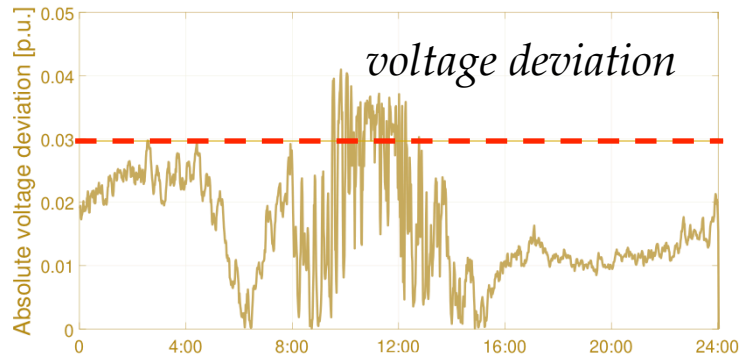
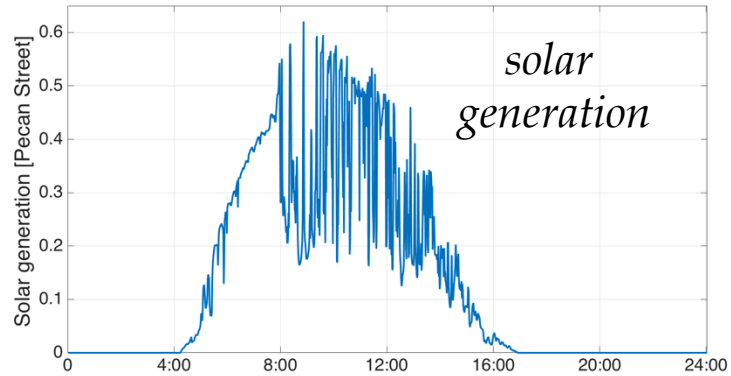


Nikolaos Gatsis
Un. of Texas San Antonio



Deep Deka
Los Alamos National Lab

Motivation



- Voltage fluctuations due to renewables

- Inefficiency of voltage control devices

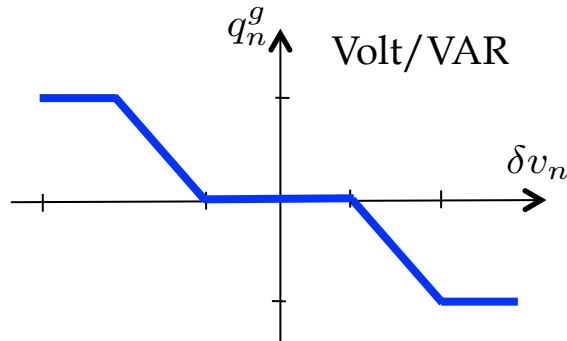


- Reactive power control with inverters



Finding reactive power setpoints

- Local control curves [Turitsyn'11], [Kekatos-Zhang-Giannakis'15], [IEEE 1547]



- ✓ no cyber cost
- ✗ suboptimal

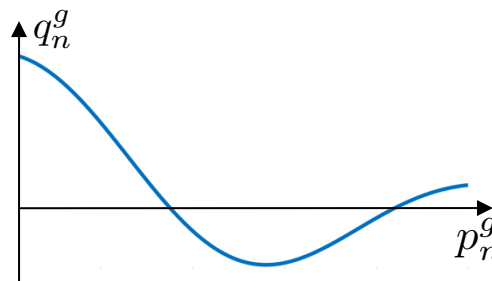
- Centralized OPF [Lavaei-Low'14], [Farivar-Low'15]

- ✓ optimal
- ✗ cyber, obsolete

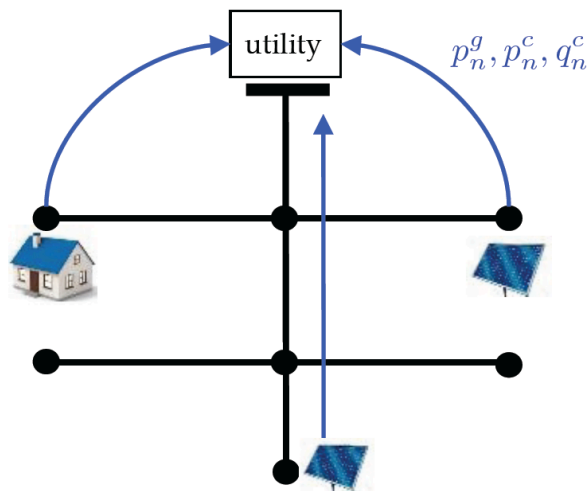
- Decentralized OPF
[Dallanese-Dhople-Giannakis'15], [Peng-Low'16]

- ✓ cyber
- ✗ iterations

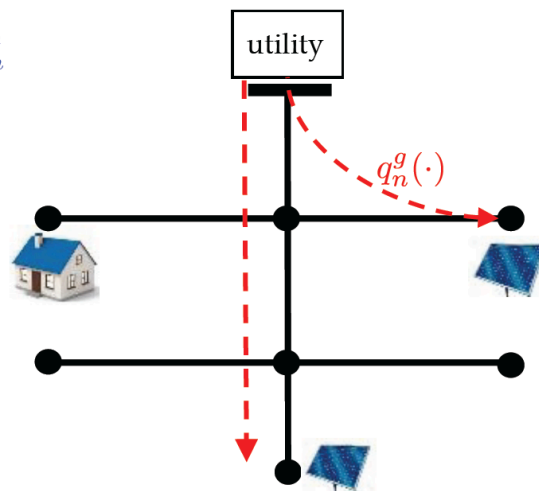
- Customize control curves on a quasi-stationary basis



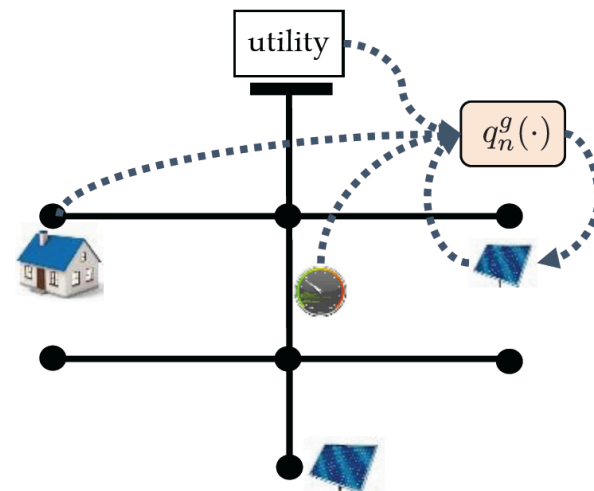
Designing control rules



Data collection
[30-min basis]



Design inverter rules
[30-min basis]



Real-time operation
[5-sec basis]

- Control rules as *linear* policies
 - Chance-constrained [Ayyagari-Gatsis-Taha'17]
 - Robust approaches [Jabr'18]; [Lin-Bitar'18]
 - Closed-loop approach [Baker, Bernstein, Dall'Annese, Zhao'18]
 - OPF-then-Fit [Dobbe-Callaway'18], [Karagiannopoulos-Hug'18]

*Control rules do not
have to be linear!*

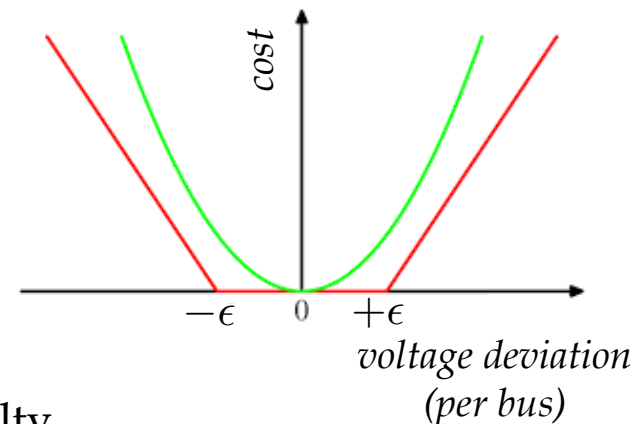
Problem formulation

- Approximate grid model
$$\tilde{\mathbf{v}} \simeq \mathbf{R}(\mathbf{p}^g - \mathbf{p}^c) + \mathbf{X}(\mathbf{q}^g - \mathbf{q}^c)$$
$$= \mathbf{X}\mathbf{q}^g + \mathbf{y}$$

- Options for voltage deviation penalties

- least-squares $\Delta_s(\mathbf{q}^g) = \|\mathbf{X}\mathbf{q}^g + \mathbf{y}\|_2^2$

- epsilon-insensitive $\Delta_\epsilon(\mathbf{q}^g) = \sum_{n=1}^N [\mathbf{e}_n^\top (\mathbf{X}\mathbf{q}^g + \mathbf{y})]_\epsilon$



- Inverter setpoints to minimize voltage deviation penalty

$$\min_{\mathbf{q}^g} \Delta(\mathbf{q}^g; \mathbf{y})$$

$$\text{s.to } -\bar{\mathbf{q}}^g \leq \mathbf{q}^g \leq \bar{\mathbf{q}}^g$$

OPF

- Inverter setpoints as policies $q_n^g(\mathbf{z}_n) = f_n(\mathbf{z}_n)$

- remote and local inputs $\mathbf{z}_n = [p_n^g - p_n^c \quad \bar{q}_n^g \quad q_n^c]^\top$

Kernel-based learning

- Given data $\{(x_t \in \mathcal{X}, z_t \in \mathbb{R})\}_{t=1}^T$, and kernel function $K : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$

$$f^* = \arg \min_{f \in \mathcal{H}_K} \sum_{t=1}^T (z_t - f(x_t))^2 + \mu \|f\|_K$$

where $\mathcal{H}_K := \left\{ f(x) = \sum_t K(x, x_t) a_t \right\}$

- Representer's Theorem*: Minimizing function depends only on training data

$$f^*(x) = \sum_{t=1}^T K(x, x_t) a_t^*$$

- Functional minimization as vector optimization

$$\arg \min_{\mathbf{a}} \|\mathbf{z} - \mathbf{K}\mathbf{a}\|_2^2 + \mu \sqrt{\mathbf{a}^\top \mathbf{K}\mathbf{a}}$$

Least-squares inverter control

- Control rule design as function fitting using T scenario data

$$\begin{aligned} \min \quad & \sum_{t=1}^T \Delta(\mathbf{q}_t^g; \mathbf{y}_t) + \mu \sum_{n=1}^N \|q_n^g\|_{\mathcal{K}_n} \\ \text{s.to} \quad & |q_{n,t}^g| \leq \bar{q}_{n,t}^g \quad \forall n, t \end{aligned}$$

- Jointly learning inverter functions can be solved as QP or SOCP

$$q_{n,t}^g(\mathbf{z}_n) = \sum_{t=1}^T K(\mathbf{z}_n, \mathbf{z}_{n,t}) a_{n,t}^* \quad \leftarrow \text{rule described by } \{\mathbf{z}_{n,t}, a_{n,t}^*\}_{t=1}^T$$

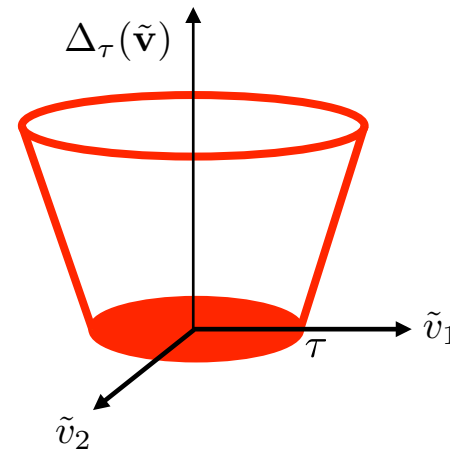
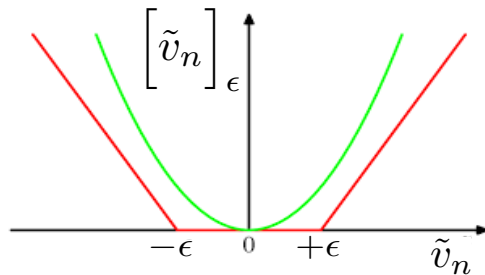
- Increasing μ unselects some inverters from reactive control (*spatial sparsity*)
- Policy output heuristically projected within feasible range

Support vector inverter control

Lemma: Voltage deviation penalties and *sparsity across scenarios*

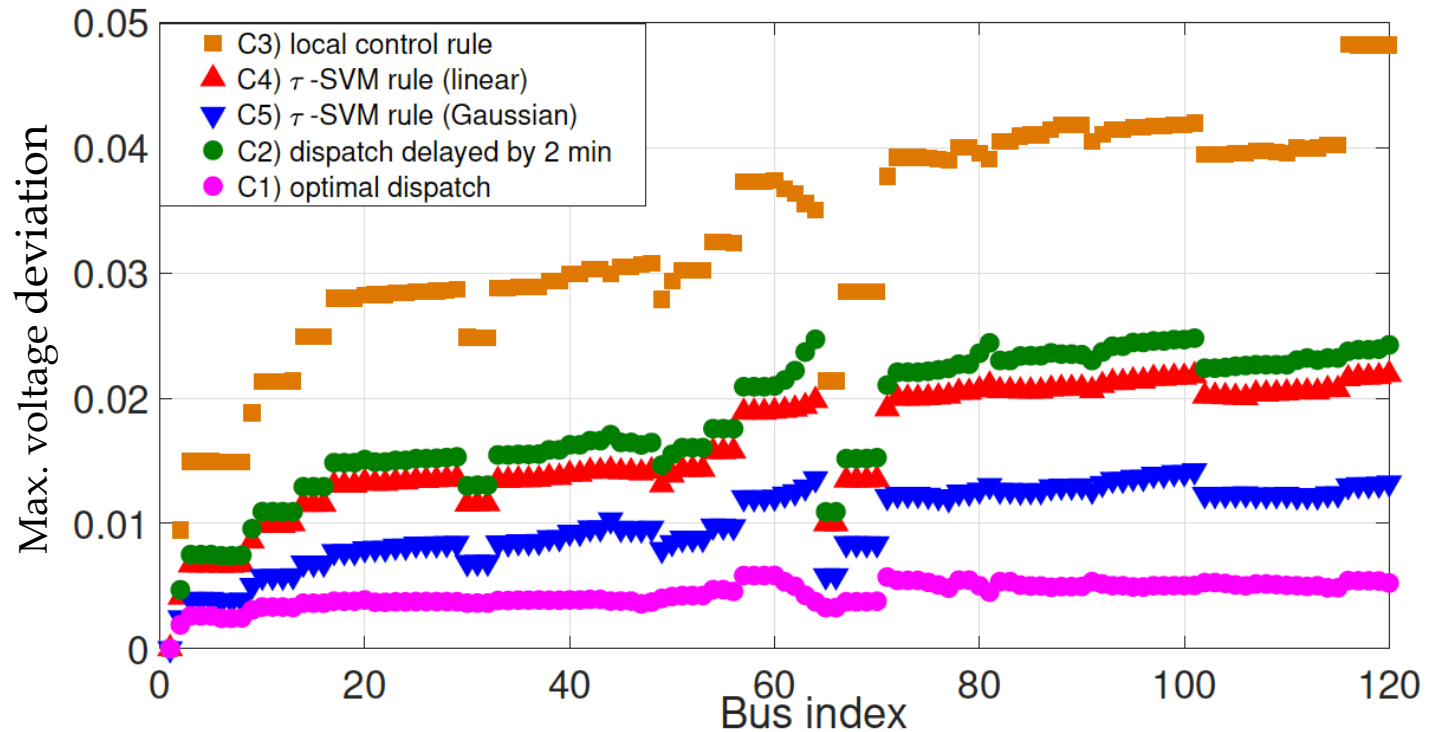
$$\Delta_{\epsilon}(\mathbf{q}^g) = \sum_{n=1}^N \left[\tilde{v}_n \right]_{\epsilon} : \text{ if } \|\tilde{\mathbf{v}}_t\|_{\infty} > \epsilon, \text{ then } a_{n,t} \neq 0 \quad \forall n$$

$$\Delta_{\tau}(\mathbf{q}^g) = \left[\|\tilde{\mathbf{v}}\|_2 \right]_{\tau} : \text{ if } \|\tilde{\mathbf{v}}_t\|_2 \leq \tau, \text{ then } a_{n,t} = 0 \quad \forall n \text{ with } |q_{n,t}^g| < \bar{q}_{n,t}^g$$



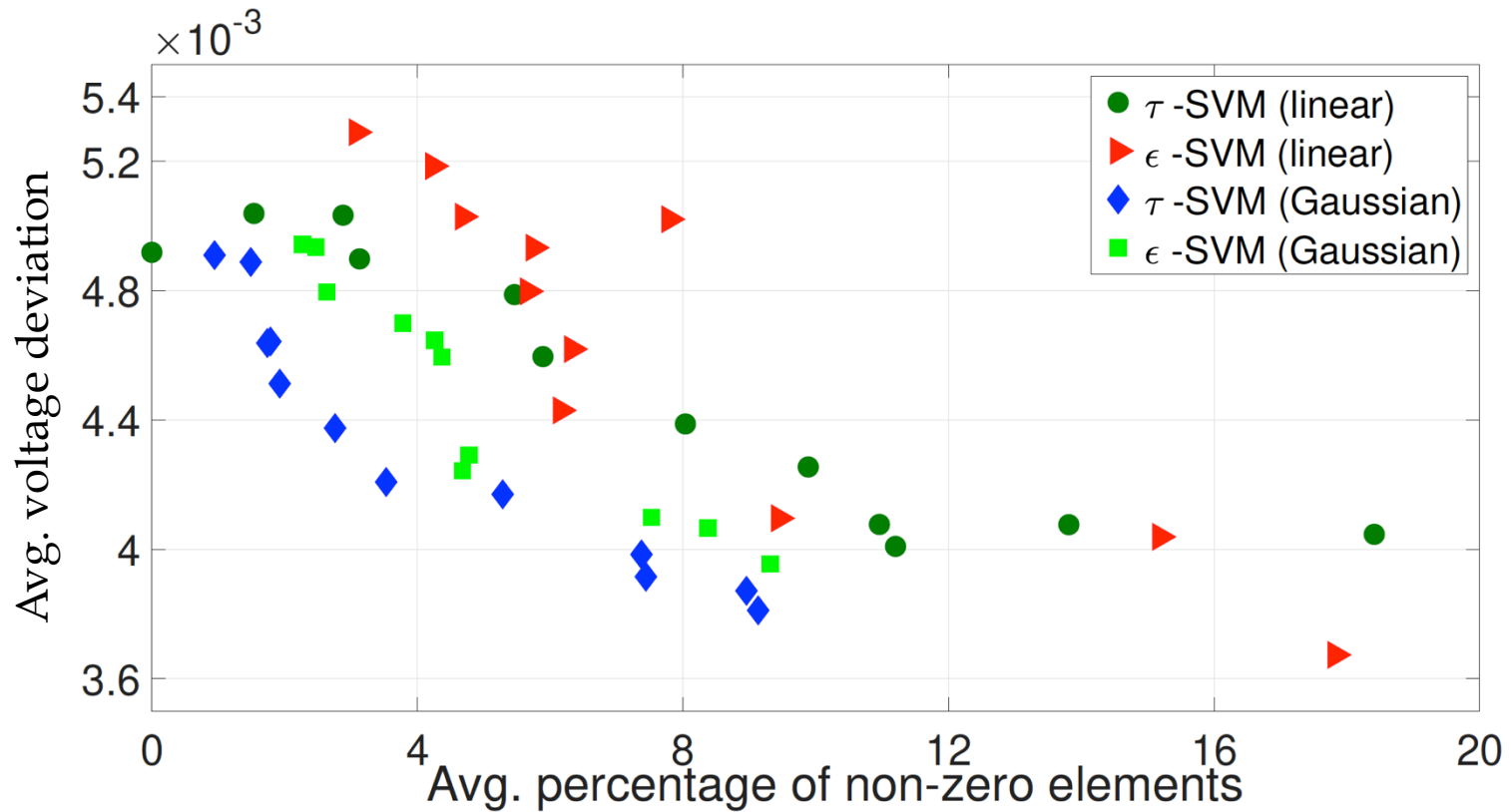
- Different from SVMs, *block* voltage penalties yield *support feeder scenarios*

Numerical tests

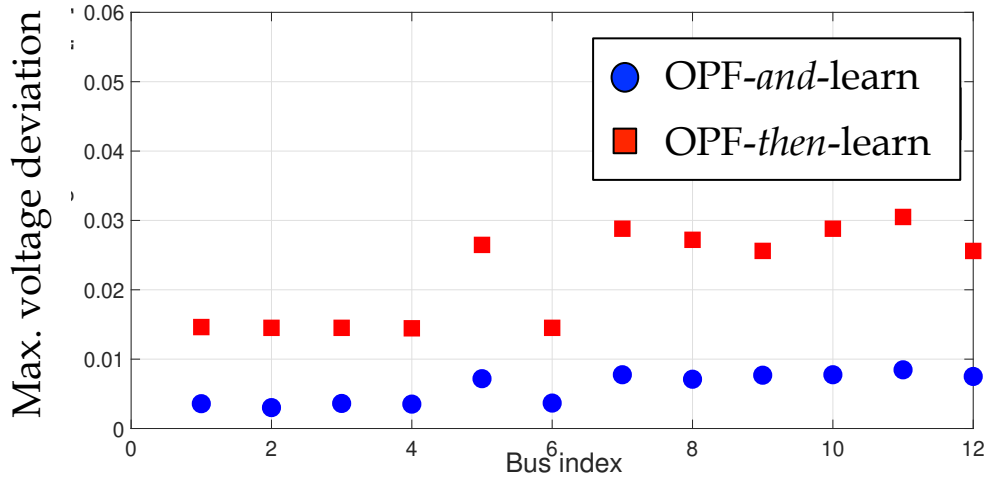


- Pecan Street data (8am-8pm) on IEEE 123-bus feeder (1-phase)
- 50% solar penetration with 1.1 inverter oversizing
- Train for $T=30$ one-min data; validate on next 30 one-min data

Performance vs. sparsity

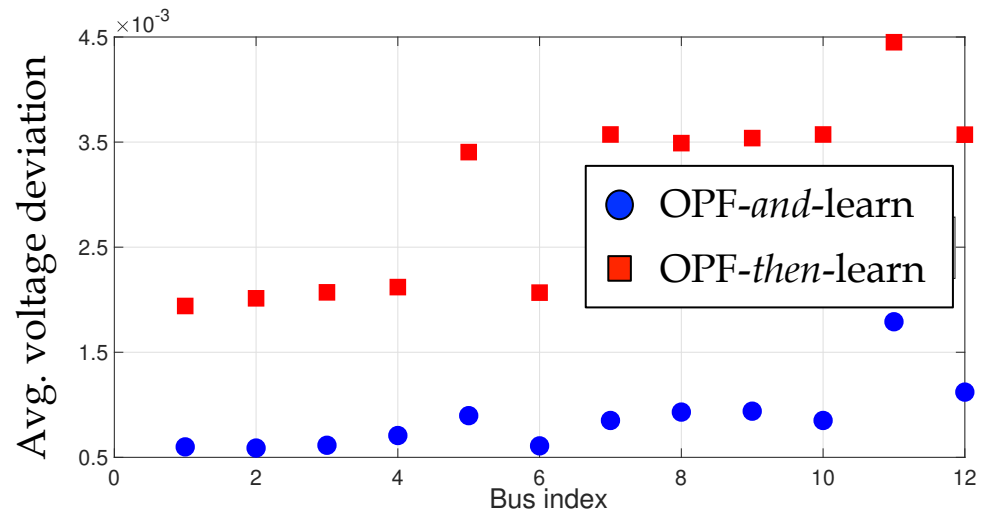


OPF-then-learn vs. OPF-and-learn



- OPF-then-learn: 2-step approach
- solve multiple OPFs
- fit input-minimizer pairs

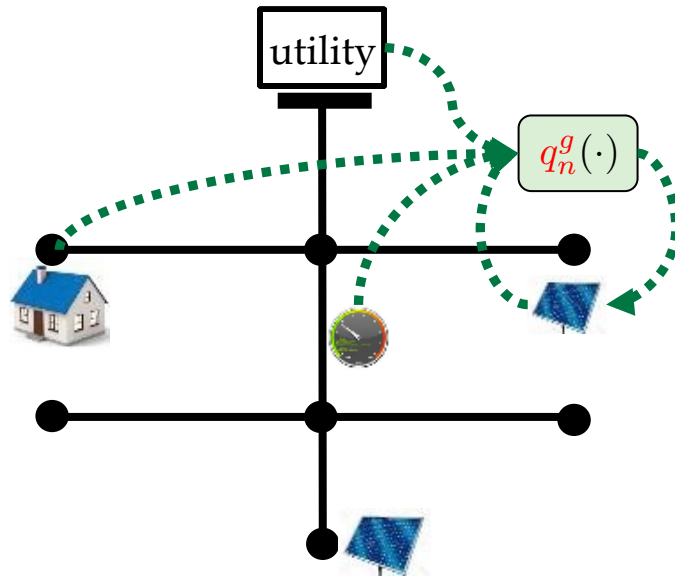
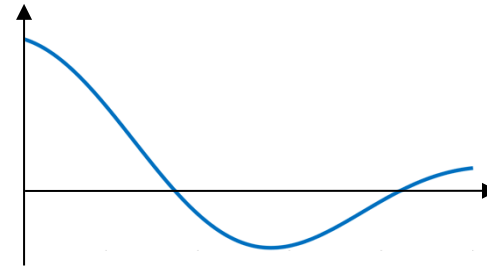
- Linear rules on IEEE 13-bus grid



Conclusions



- ✓ learning non-linear inverter rules
- ✓ data-based feeder-wide designs
- ✓ SVM costs for communication savings



- closed-loop control
- remote input and kernel selection
- constrained kernel learning
- DNN-based rules

Thank you!

Grid IoT data analytics



Tools

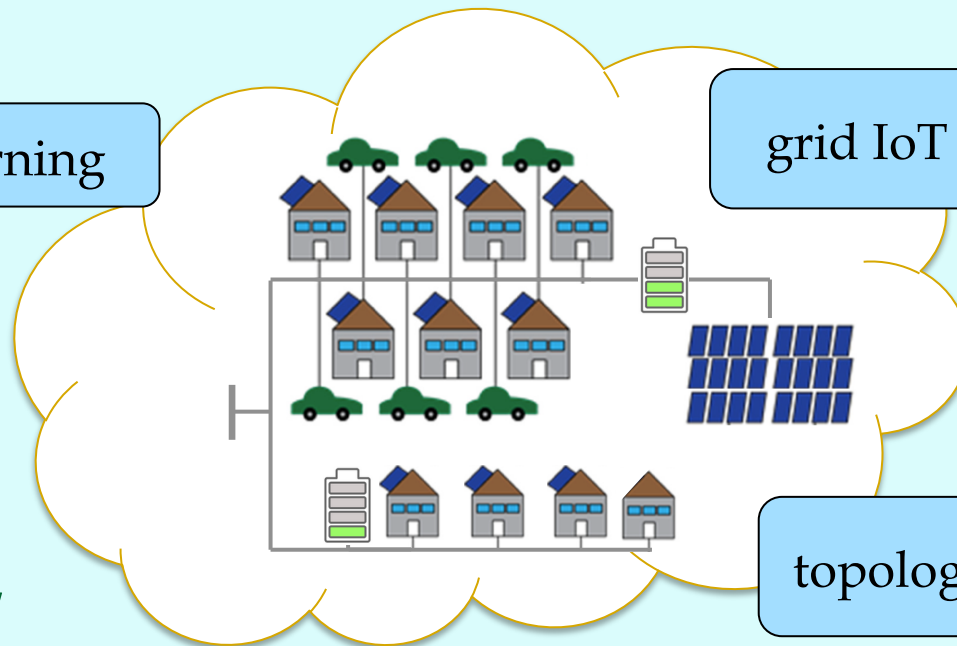
inverter probing

machine learning for
grid control

Problems

load learning

grid IoT control



Thank You!

Related publications



- G. Cavraro and V. Kekatos, "Inverter Probing for Power Distribution Network Topology Processing," *IEEE Trans. on Control of Network Systems*, Sep 2019.
- G. Cavraro and V. Kekatos, "Graph Algorithms for Topology Identification using Power Grid Probing," *IEEE Control Systems Letters*, Oct 2018.
- G. Cavraro, A. Bernstein, V. Kekatos, and Y. Zhang, "Real-Time Identifiability of Power Distribution Network Topologies with Limited Monitoring," *IEEE Control Systems Letters*, Apr 2020.
- G. Cavraro, V. Kekatos, and S. Veeramachaneni, "Voltage Analytics for Power Distribution Network Topology Verification," *IEEE Trans. on Smart Grid*, Jan. 2019.
- S. Taheri, V. Kekatos, and G. Cavraro, "An MILP Approach for Distribution Grid Topology Identification using Inverter Probing," *IEEE PES PowerTech*, Milan, Italy, June 2019.
- M. K. Singh, V. Kekatos, S. Taheri, K. P. Schneider, and C.-C. Liu, "Enforcing Radiality Constraints for DER-Aided Power Distribution Grid Reconfiguration," in *Proc. PSCC*, Porto, Portugal, June 2020.
- S. Bhela, V. Kekatos, and S. Veeramachaneni, "Smart Inverter Grid Probing for Learning Loads: Part I -- Identifiability Analysis," *IEEE Trans. on Power Systems*, Sep 2019.
- S. Bhela, V. Kekatos, and S. Veeramachaneni, "Smart Inverter Grid Probing for Learning Loads: Part II -- Probing Injection Design," *IEEE Trans. on Power Systems*, Sep 2019.
- S. Bhela, V. Kekatos, and S. Veeramachaneni, "Enhancing Observability in Distribution Grids using Smart Meter Data," *IEEE Trans. on Smart Grid*, Nov 2018.
- M. Jalali, V. Kekatos, N. Gatsis, and D. Deka, "Designing Reactive Power Control Rules for Smart Inverters using Support Vector Machines," *IEEE Trans. on Smart Grid*, (early access).
- A. Garg, M. Jalali, V. Kekatos, and N. Gatsis, "Kernel-Based Learning for Smart Inverter Control," in *Proc. IEEE GlobalSIP*, Anaheim, CA, Nov. 2018.