# The Machine Learning Approach to Dynamic Security Assessment

Simon Tindemans, TU Delft Jochen Cremer, Imperial College London

**TUDelft** Imperial College London

IEEE BDA Tutorial Series: Big Data & Analytics for Power Systems 10:00 am-12:00 pm, PST, Monday, Dec. 2, 2019

### Presenters





**TU**Delft Imperial College London

#### Simon Tindemans

- Assistant professor at Delft University of Technology (NL)
- Visiting researcher at the Alan Turing Institute (UK)
- Research interest: machine learning for risk assessment, efficient computation and apportioning of risks

#### **Jochen Cremer**

- PhD student (final year) at Imperial College London (UK)
- Research interest: intersection of machine learning and mathematical optimization applied to the operation of the power system

Disclaimer: the materials presented in this tutorial will be somewhat biased towards our own research.

2

## **Opening credits**

Collaborators and funders of our work in this area

- Imperial College London: Ioannis Konstantelos, Mingyang Sun, Federica Bellizio, Goran Strbac
- **RTE**: Jean Maeght, Nicolas Omont, Samir Issad, Patrick Panciatici, Antoine Marot, Benjamin Donnot







Disclaimer: the materials presented in this tutorial will be somewhat biased towards our own research.

### Outline

London



### Introduction

### Problem statement



### Powerline crossing at Ems river



#### double-circuit 380kV





CC-AT-SA 3.0 https://commons.wikimedia.org/wiki/File:Serenade\_on\_Ems.JPG by Frankee 67

### 4 November 2006 – cascading faults





### Pan-European disturbance





## Load shedding



#### **TU**Delft Imperial College London

Source: UCTE Final Report – System Disturbance on 4 November 2006

### The system operator's challenge



**TU**Delft Imperial College

ondon

System operators are responsible for the reliable supply of power to end users

- 1. Electricity markets 'propose' a solution
- 2. System operators check this solution and prepare for uncertainties
- Operators can override market outcomes, but this is expensive and/or carbon-intensive.
- 4. When multiple TSOs are involved, things get harder.

10

### **Uncertainties and decisions**

Uncertainties continuous (e.g. wind forecasts) ٠ discrete (sudden failures, aka contingencies) ٠ e.g. sudden outage ...... now forecast When to act? hour ahead 'corrective' actions day ahead 'no' uncertainty most uncertainty limited uncertainty most options restricted options very few actions and ٠ limited time

**TU**Delft Imperial College London

### Reliability, Security and Stability

- *"Reliability* of a power system refers to the probability of its satisfactory operation over the long run."
- "Security of a power system refers to the degree of risk in its ability to survive imminent disturbances (contingencies) without interruption of customer service."

"(..) **Stability** is the ability of an electric power system, for a given initial operating condition, to regain a state of operating equilibrium after being subjected to a physical disturbance, with most system variables bounded so that practically the entire system remains intact."

P. Kundur *et al.*, "Definition and classification of power system stability IEEE/CIGRE joint task force on stability terms and definitions," in *IEEE Transactions on Power Systems*, vol. 19, no. 3, pp. 1387-1401, Aug. 2004.

implies



### **Classification of stability**



**TU**Delft Imperial College London

P. Kundur *et al.*, "Definition and classification of power system stability IEEE/CIGRE joint task force on stability terms and definitions," in *IEEE Transactions on Power Systems*, vol. 19, no. 3, pp. 1387-1401, Aug. 2004.

### Foresight through simulations



Time (sec)

F. R. S. Sevilla and L. Vanfretti, "Static stability indexes for classification of power system time-domain simulations," 2015 IEEE Power & Energy Society Innovative Smart Grid Technologies Conference (ISGT), Washington, DC, 2015.

14

### System response to a disturbance

**ŤU**Delft

Imperial College London



### **Transient stability**



**TU**Delft Imperial College London

- 1. steady-state stable and trajectory stable in b
- 2. steady-state unstable in b'
- 3. steady-state stable in b", however the trajectory is unstable

### Security



Security is operator-defined:

#### Example: N-1 security

- Post-fault stability for any *single* equipment fault.
- All operational constraints are satisfied at all times

In the remainder, we will assume a **secure contingency** list.



### Security vs cost



*"survive imminent disturbances (contingencies)"* 

There is a trade-off:

- 'the smaller' the region the more secure
- 'the larger' the region the cheaper to operate



### Introduction

Machine learning for dynamic security assessment



### **Computational burden**



Time Horizon |1 hr

00.00

06:00

12:00

12:00

00.00

- Dynamic simulations are carried out with a detailed model that accounts for <u>each asset.</u>
- These simulations must be considered for <u>each outage</u> and <u>each operation</u> <u>condition</u>
- **Result:** Too many cases to be simulated in real time

### Security assessment: analysis tools

**1. Actual experiments** 



2. Time-domain simulations

10k+ coupled ODEs ~minutes

tool of choice ... but slow

3. Quasi-steady state simulations with AC, linearised AC or DC power flows

10k+ nonlinear equations ~seconds

quick ... but biased

4. Proxy (aka emulator) for time-domain simulator

e.g. decision tree or NN ~ms

based on data + mathematics, not physics (watch this space)

Imperial College

London

### The general idea

#### Not a new idea. See e.g.:

Wehenkel, L., (1998). *Automatic Learning Decision trees and Techniques in Power Systems*, ISBN 978-0-7923-8068-9.

#### **Offline analysis**





### **Online analysis**





proxies of dynamic stability

improved decision-making

**TU**Delft Imperial College London

### Using machine learning for DSA



### **Offline workflow**

### Classifier training and evaluation



### Using machine learning for DSA



### **Extracting indicators from simulations**



F. R. S. Sevilla and L. Vanfretti, "A small-signal stability index for power system dynamic impact assessment using time-domain simulations," 2014 IEEE PES General Meeting

#### **Examples**

- Small stability [S&V 2014]
  - Mode identification
- Static [s&v 2015]
  - Overload
  - Voltage
- Dynamic [S&V 2015]
  - Integrated square generator angle

F. R. S. Sevilla and L. Vanfretti, "Static stability indexes for classification of power system time-domain simulations," 2015 IEEE Power & Energy Society Innovative Smart Grid Technologies Conference (ISGT) 26

## Mapping onto classification problem

#### **Features**

- Nodal voltages angles, active/reactive injections
- Line active/reactive power
- Topological features

#### Outcomes

- Secure/insecure, with respect to each contingency [classification]
- Distance to security boundary [regression]



### Decision trees for power system security





**TU**Delft Imperial College London

#### Decision trees:

- Limited expressive power
- Fantastic interpretability

### Example rule

#### Security rule for N-2 outage for Launay - Taute line in Normandy





**TU**Delft Imperial College London

### Alternative: random forest (Breiman, 2001)

Use an *ensemble* of decision trees. For condition *x*:

- Good expressive power
- Limited interpretability
- Very few hyperparameters

Classifier:

(a personal favourite)

$$\hat{f}_c(x) = \begin{cases} 0 \ if \ s_c(x) \le 0.5 \\ 1 \ if \ s_c(x) > 0.5 \end{cases}$$

Individual decision trees  $\hat{f}_c^k(x)$  are randomized in two ways:

 $s_{c}(x) \cong \frac{1}{K} \sum_{k=1}^{K} \hat{f}_{c}^{k}(x)$  $\hat{f}_{c}^{k}(x) \in \{0,1\}$ 

- Random subset of features for training
- Bootstrap aggregation ('bagging'), i.e. random resampling of training data with replacement.

30



### Alternative: Neural networks

- Great expressive power
- Limited interpretability
- Many hyperparameters

Arteaga, J-M. H., Hancharou, F., Thams, F., & Chatzivasileiadis, S. *Deep Learning for Power System Security Assessment*. In *Proceedings of IEEE Powertech 2019* IEEE.





TABLE IRepresentation of CNN architecture.

Layer	Shape	Weights size	Bias size	# param
Input	[b,162,162,3]			
Conv1	[b,162,162,20]	[9,9,3,20]	[20]	4.880
Max-pool1	[b,81,81,20]			
Conv2	[b,81,81,40]	[7,7,20,40]	[40]	39.240
Max-pool2	[b,40,40,40]			
Conv3	[b,40,40,80]	[5,5,40,80]	[80]	80.080
Max-pool3	[b,20,20,80]			
Flatten	[b,32000]			
FC1	[b,250]	[32000,250]	[250]	8.000.250
FC2 (output)	[b,2]	[250,2]	[2]	502
Total				8.124.952

### **Prediction = making mistakes**



**TU**Delft Imperial College London

(Simple) classification error =  $\frac{N_{FP} + N_{FN}}{N_{FP} + N_{TP} + N_{FN} + N_{TN}}$ 



### **HPC** implementation

10,000 operating points

1980 contingencies

CURIE Supercomputer (10,000 cores)



11 stability indicators

<0.5% average classification error

#### Histogram of test errors for four indices



I. Konstantelos, G. Jamgotchian, S. Tindemans, P. Duchesne, S. Cole, C. Merckx, G. Strbac and P. Panciatici, "Implementation of a Massively Parallel Dynamic Security Assessment Platform for Large-Scale Grids", IEEE Transactions on Smart Grid, May 2017.

### **Offline workflow**

### Selection and generation of training data



### Using machine learning for DSA



### Challenge

Generate a set of training scenarios, such that:

- the classifier has a low error rate, ...
- for known and unknown scenarios, ...
- with finite computational resources.


# Three approaches in the literature

All imaginable states







# Approach 1: Use all imaginable states

- E.g. upper/lower bounds for injections
- Generates *many* infeasible or unlikely states
- Need clever methods to 'zoom in' (see table). But is it enough?

UNCLASSIFIEI	O INPUT	VOLUMES I	FOR PGL	IB-OPF NE	TWORKS
case	x	$V^{BT}$	HP	$V^{HP}$	$\frac{-\log_{10}(V)}{ x }$
AC-OPF v	without 1	N-1 security	and with	nout uncerta	unty
case3_lmbd	4	6.3e-02	28	3.3e-02	37.0%
case5_pjm	7	1.0e+00	99	6.9e-03	30.9%
case14_ieee	6	2.4e-01	54	6.9e-04	52.7%
case24_ieee_rts	20	9.2e-01	184	2.3e-06	28.2%
case30_ieee	7	6.2e-03	61	8.8e-06	72.2%
case39_epri	19	9.9e-02	203	7.0e-08	37.7%
case57_ieee	10	3.8e-02	231	4.9e-06	53.1%
case73_ieee_rts	62	1.0e+00	608	6.1e-16	24.5%
case118_ieee	72	1.7e-02	1000	1.6e-17	23.3%
case162_ieee_dtc	23	6.1e-04	371	1.5e-11	47.1%
case200_tamu	69	9.3e-01	1000	6.0e-11	14.8%
case300_ieee	125	1.0e-12	1000	3.4e-40	31.6%
case500_tamu	111	8.6e-02	1000	5.4e-26	22.8%
AC-OPI	F consid	ering N-1 se	ecurity ar	nd uncertain	ty
case39_epri	25	2.6e-01	271	2.0e-05	18.8%
case162_ieee_dtc	29	2.2e-04	394	6.0e-10	31.8%
Median all cases	23	8.6e-02	271	7.0e-08	31.6%

TABLE I

**TU**Delft Imperial College London A. Venzke, D.K. Molzahn, S. Chatzivasileiadis,(2019). Efficient Creation of Datasets for Data-Driven Power System Applications, arXiv:1910.01794

# Approach 2: Use historical data

- Historical states are (almost) guaranteed to be relevant
- They may not be *sufficient* 
  - in volume
  - in variety
- We need to 'enrich' (interpolate/extrapolate) the historical data



### Challenge: complex dependency patterns

(a) (b) 0.025 200 0.02 150 (MM) Probability 0.015 ш 100 Load 0.01 50 0.005 0 n 100 150 50 300 0 0 100 200 Load B (MW) Load A (MW)

Fig. 1. (a) Marginal probability distributions of 5-minute load measurements over 3 months from a bus in the region of Nancy, France (March 2012). (b) Non-linear dependence between load measurements of two other buses in the same region.

I. Konstantelos, M. Sun, S. H. Tindemans, S. Issad, P. Panciatici and G. Strbac, "Using Vine Copulas to Generate Representative System States for Machine Learning," in *IEEE Transactions on Power Systems*, vol. 34, no. 1, pp. 225-235, Jan. 2019.



### Decoupling marginal distributions from dependence



**ŤU**Delft

Imperial College London

41

41

# The modelling pipeline

**TU**Delft Imperial College

London



- Construct multivariate C-Vine copula (Bedford and Cooke, 2001) using pair copula construction (Joe, 1996)
- We truncate the C-Vine to limit impact of dimension

42

# Does it work?

- 128 variables (118 loads, 10 wind generators)
- 3 months data, 5-minute intervals
- 10 clusters; 97.5% variance used to select truncation; C-vine parametrised using Clayton, Frank, Gaussian, Gumbel, Student-t copulas (and rotations)
- Generated 40,000 samples
- Test on 1000 random subsets of 200 observations of sample and historical data
- Test metrics
  - Kolmogorov-Smirnov for marginals
  - Energy test (Aslan & Zech, 2005)



### Statistical match to historical data



# **Application test**

### Model

- IEEE 118 bus system
- Set of four line outages, analyses independently
- Dispatch determined using OPF
- Post-fault generation redispatch of +- 10% permitted

### **Training and testing**

- For a given state, verify whether post fault solution exists
- Classification using decision tree (Matlab 2017a default parameters)
- Training on bus angles and post-fault violations (true/false)
- 10-fold cross-validation

**TU**Delft Imperial College London

### Impact on machine learning four different contingencies



Fig. 7: F-score boxplots for contingencies (a) L148 (b) L139 (c) L54 (d) L71.

MGC = multivariate Gaussian copula ; MGD = multivariate Gaussian distribution



# Approach 3: Improving sample efficiency

#### **Classifiers are computed based on point samples**



### **Obvious bright ideas**

- Don't analyse situations that would never occur
- Don't analyse situations for which the outcome is obvious

# Parametric approaches

# Approaches typically rely on three assumptions:

- Meaningful definition of 'distance' from the security boundary.
- 'Easy' sampling distributions.
- 'Nice' properties of the security boundary.

#### Chengxi Liu et al. (2014), IEEE Transactions on Power Systems



### **TU**Delft Imperial College London





# Research: the *active learning* approach

- Passive learning
  - Learner does not influence data gathering process
  - Inherently linear



- Active learning (e.g. Settles, Active Learning, 2012)
  - Generate data that is useful to the Learner
  - Machine learning equivalent of 'optimal design of experiments'



- Applied when sample generation **and/or** analysis is expensive

### Active learning process



# **Defining importance**

1. For condition x and contingency c, predict score using ensemble method (e.g. random forest)

$$s_{c}(x) \cong \frac{1}{K} \sum_{k=1}^{K} \hat{f}_{c}^{k}(x)$$
$$\hat{f}_{c}^{k}(x) \in \{0,1\}$$



2. Define importance I(x, c) by measuring *ensemble disagreement* (entropy)  $I(x; c) = -\frac{1}{\log_2 2} [s_c(x) \log_2 s_c(x) + (1 - s_c(x)) \log_2(1 - s_c(x))] \longleftarrow$ 

# Sample filter

### Accept/reject algorithm

$$Pr(accept|x,c) = b + (1-b)I(x,c)$$

**Results in:** 

$$f_{bias}(x,c) = e f_0(x) + (1-e) f_{int}(x,c)$$

where

 $f_0(x)$  = unbiased distribution  $f_{int}(x,c) \propto I(x,c)$ e = effective exploration

**TU**Delft Imperial College London

# Small 'proof of concept'- IEEE 118 bus model

#### Procedure

Delft

Imperial College

London

- 1. Check DC load flow feasibility
- Map actual measurements from French transmission grid onto network
- 3. Generate 500,000 random load samples
- 4. For each sample, analyse the impact of every single line outage (186)



Рис.1. IEEE тестовая схема, состоящая из 118 узлов

# Study details

- Offline simulation of importance sampling
  - 450,000 states are classified as 'good' or 'bad' in combination with 186 contingencies
  - Use results as an unbiased 'pool' of samples
- Importance sampling parameters
  - Exploration fraction e = 0.5 (conservative choice: max 2x slowdown)
  - Minimum acceptance rate 1%
  - Update importance functions in batches
- Validation using 50,000 states x 186 contingencies
  - Compare classification errors against unbiased samples using identical computational budget





### Results

- Measure performance across all decision trees for given number of evaluations
- Robust improvement, for various importance functions
- Active learning advantage improves with learning



### **TU**Delft Imperial College London

### **Online workflow**

# Using machine learning to effectively operate simulations



# Using machine learning for DSA



# Challenge

- Quantifying the risk of relying on a Machine Learning approach is not trivial
- When moving these Machine Learning approaches toward practical tools it is important to understand and manage the risk involved
- In comparison: Physics-based methods typically offer insights analytically or numerically for assessing the confidence of the output



# The machine learning approach

#### **Close to online**

- Study more potential operating conditions instead of only a few
- Replace dynamic simulations (slow) with a machine-learning-based estimator (fast)

### Offline

• Prepare (train) an estimator on actual dynamic simulations using similar operating conditions



### The estimation can be inaccurate



Estimated and actual stability limits are different!

#### Two types of inaccurate predictions:

FP: Is stable but we think it is unstable (BAD)FN: Is unstable but we think it is stable (VERY BAD!)

This can have a severe effect!



# **Combined** approach



• Sometimes inaccurate







### Understanding the costs of inaccurate predictions



Cost skew:  $C_{FN} \gg C_{FP}$ 



# What a classifier can do

#### **Classify points**

• is *x* positive?

#### **Rank points**

• Is x 'more positive' than x'?

#### Output a score s(x)

• 'How positive' is x?



### Output a probability estimate $\widehat{p}(x)$

• What is the (estimated) probability that x is positive?



Nikos Nikolaou, "Cost-sensitive learning with AdaBoost", 2017

# Probability estimation is not trivial

- Typically, classifiers don't output probability estimates.
  Scores can be used
- E.g. decision tree

**TU**Delft Imperial College

London



Nikos Nikolaou, "Cost-sensitive learning with AdaBoost", 2017

### Calibration

- $s(x) \in [0,1]$  score for operating condition x
- A classifier is **calibrated** if  $\widehat{p}(x) \rightarrow s(x)$ , as  $N \rightarrow \infty$
- An intuition for a calibrated classifier: E.g., 70% of the operating points with s(x) = 0.7 should belong to the 'stable' class



# The risk of relying on machine learning

### **Machine-learning**

 $R_{stable} = p_o p_c \widehat{\boldsymbol{p}}(\boldsymbol{x}) \boldsymbol{C}_{FN}$ 

$$R_{unstable} = p_o(1-p_c)(1-\hat{p}(x))C_{FP}$$

Predict class with lower risk





# **Combined** approach



High risk Medium risk Low risk

Perform simulations on the operating conditions with high risk





# **Multiple contingencies**



### Perform simulations according to risks



### A case study

System: IEEE 6 bus system, 1500 conditions (stable 1322, unstable 178) Machine-Learning: AdaBoost ensemble, cross-validation, train/test 70/30



### Summary

 Combining Machine Learning and current DSA methods results in fast and accurate security assessment

• Zero-risk can be achieved – allowing for no disadvantage when using Machine Learning

• Parameter estimations are uncertain


### **Online workflow**

# Using machine learning to ensure stability in operations



### Using machine learning for DSA



# Challenge

- Compute appropriate measures to re-establish stability once an unstable operating condition is detected
- How conservative do we need to be? Cost versus risk
- Stability is a complex system-level attribute
- Finding cost-effective measures to ensure stability is even more complex





# Our approach

 Using Machine Learning to train a proxy implementable in a control approach



High risk Medium risk

Low risk



High risk of instability

Medium risk

Low risk Find low-risk regions

Move operating condition to 'low risk' region





**ŤU**Delft

### **Classifier in control**



Imperial College London Jochen Cremer, Ioannis Konstantelos, Simon Tindemans, Goran Strbac, "Sample-Derived Disjunctive Rules for Secure Power System Operation," 2018 IEEE International Conference on Probabilistic Methods Applied to Power Systems (PMAPS), Boise, USA 2018

# Using a classifier in control is not trivial

- DT tries to approximate the true stability boundary
- Typical measure of DT's quality: classification error



Class. error < 10% Control error > 90%

Classification error cannot predict a rule's performance when used for inferring suitable mitigation control actions.



Jochen Cremer, Ioannis Konstantelos, Simon Tindemans, Goran Strbac, "Data-driven Power System Operation: Exploring the Balance between Cost and Risk", IEEE Transactions on Power Systems, 2018

### Four different approaches

#### Asymmetric weighting

Single-E





Probabilistic



**TU**Del Imperial ( London

Jöchen Cremer, Ioannis Konstantelos, Simon Tindemans, Goran Strbac, "Data-driven Power System Operation: Exploring the Balance between Cost and Risk", IEEE Transactions on Power Systems, 2018

### **Combination approach**



#### **Optimal Power Flow**

 $\begin{array}{ll} \min & (1-\alpha)\,\hat{\mathbb{E}}(\mathrm{cost}) - \alpha\,\hat{\mathbb{E}}(\mathrm{stability}) \\ \mathrm{s.t.} & h(x) = 0 \\ & g(x) \leq 0 \\ & x^L < x \leq x^U, \end{array}$ 

#### Extension by index I for each learner

$x \le a_{l,d} + m_d(1 - y_{l,d})$	$\forall d \in D_l,  \forall l \in L$
$x > \tilde{a}_{l,d} + \tilde{m}_d(1 - y_{l,d})$	$\forall d \in D_l,  \forall l \in L$
$\sum_{d \in D_l} y_{l,d} = 1$	$\forall l \in L$
$y_{l,d} = \{0,1\}$	$\forall d \in D_l,  \forall l \in L$
$m_d = \max\{a_{d'} : d' \in D_l\} - a_{l,d}$	$\forall d \in D_l,  \forall l \in L$
$\tilde{m}_d = \min\{\tilde{a}_{d'} : d' \in D_l\} - \tilde{a}_{l,d}$	$\forall d \in D_l.  \forall l \in L,$

#### Probability estimate for each learner

$$h_l = \sum_{d \in D_l} p_{l,d} y_{l,d} \quad \forall l \in L,$$
  
Soft voting  
 $\hat{\mathbb{E}}(\text{stability}) = F = \sum_{l \in L} w_l h_l(x)$ 

**TU**Delft Imperial College London

80

## The balance of cost and risk

• This approach balances economic cost of dispatching with the risk of relying on Machine Learning

• Each operating point has a unique solution

• This approach is a MILP in DC or MINLP in AC



# Case study

- IEEE 39 bus system
- Considering steady state security allows for SCOPF comparison
- Kumaraswamy distribution in loads
- Implemented in Python 3.5.2, scikit-learn



Optimization environment: Pyomo, Solver: Gurobi 7.02



### **Computational results**

- MILP condition-specific approach: 82 binaries
- MILP probabilistic approach: 21 binaries

• Solver time for all approaches: <0.1sec



### Summary

- All approaches ensure security (zero risk)
- **Cost-risk balance:** Probabilistic approach & conditionspecific approach are best
- Condition-specific approach requires iterations in training
- Calibrated probabilistic approach outperforms all other approaches in the combination of time, robustness and cost-risk balance

**TU**Delft Imperial College London

### Summary and outlook



### Using machine learning for DSA



# Major open challenges

- Optimal balance between online and offline
  - Offline sample distribution
  - Dealing with topological changes
- Combination of physical models and data-driven approaches
- Coordination with complex control actions

Thank you! We are happy to answer questions



### References

- P. Kundur *et al.*, "Definition and classification of power system stability IEEE/CIGRE joint task force on stability terms and definitions," in *IEEE Transactions on Power Systems*, vol. 19, no. 3, pp. 1387-1401, Aug. 2004.
- Wehenkel, L., (1998). Automatic Learning Decision trees and Techniques in Power Systems, ISBN 978-0-7923-8068-9.
- F. R. S. Sevilla and L. Vanfretti, "A small-signal stability index for power system dynamic impact assessment using time-domain simulations," 2014 IEEE PES General Meeting
- F. R. S. Sevilla and L. Vanfretti, "Static stability indexes for classification of power system time-domain simulations," 2015 IEEE Power & Energy Society Innovative Smart Grid Technologies Conference (ISGT), Washington, DC, 2015.
- Arteaga, J-M. H., Hancharou, F., Thams, F., & Chatzivasileiadis, S. Deep Learning for Power System Security Assessment. In Proceedings of IEEE Powertech 2019 IEEE.
- I. Konstantelos, G. Jamgotchian, S. Tindemans, P. Duchesne, S. Cole, C. Merckx, G. Strbac and P. Panciatici, "Implementation of a Massively Parallel Dynamic Security Assessment Platform for Large-Scale Grids", IEEE Transactions on Smart Grid, May 2017.
- A. Venzke, D.K. Molzahn, S. Chatzivasileiadis, (2019). Efficient Creation of Datasets for Data-Driven Power System Applications, arXiv:1910.01794
- I. Konstantelos, M. Sun, S. H. Tindemans, S. Issad, P. Panciatici and G. Strbac, "Using Vine Copulas to Generate Representative System States for Machine Learning," in *IEEE Transactions on Power Systems*, vol. 34, no. 1, pp. 225-235, Jan. 2019.
- C. Liu et al., "A Systematic Approach for Dynamic Security Assessment and the Corresponding Preventive Control Scheme Based on Decision Trees," in IEEE Transactions on Power Systems, vol. 29, no. 2, pp. 717-730, March 2014
- Krishnan, V., McCalley, J. D., Henry, S., & Issad, S. (2011). Efficient Database Generation for Decision Tree Based Power System Security Assessment. *IEEE Transactions on Power Systems*, 26(4), 2319–2327.
- Settles, B. (2012). Active Learning. https://doi.org/10.2200/S00429ED1V01Y201207AIM018
- Jochen Cremer, Ioannis Konstantelos, Goran Strbac, "From Optimization-based Machine Learning to Interpretable Security Rules for Operation", IEEE Transactions on Power Systems, 2019
- Nikos Nikolaou, "Cost-sensitive learning with AdaBoost", 2017
- Jochen Cremer, Ioannis Konstantelos, Simon Tindemans, Goran Strbac, "Sample-Derived Disjunctive Rules for Secure Power System Operation," 2018 IEEE International Conference on Probabilistic Methods Applied to Power Systems (PMAPS), Boise, USA 2018
- Jochen Cremer, Ioannis Konstantelos, Simon Tindemans, Goran Strbac, "Data-driven Power System Operation: Exploring the Balance between Cost and Risk", IEEE Transactions on Power Systems, 2018

